# NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

## **TECHNICAL NOTE 2214**

FORMULAS AND TABLES OF COEFFICIENTS FOR NUMERICAL
DIFFERENTIATION WITH FUNCTION VALUES GIVEN AT
UNEQUALLY SPACED POINTS AND APPLICATION TO
SOLUTION OF PARTIAL DIFFERENTIAL EQUATIONS

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FORMULAS AND TABLES OF COEFFICIENTS FOR NUMERICAL DIFFERENTIATION
WITH FUNCTION VALUES GIVEN AT UNEQUALLY SPACED POINTS AND
APPLICATION TO SOLUTION OF PARTIAL DIFFERENTIAL EQUATIONS

#### SUMMARY

By Chung-Hua Wu

General differentiation formulas for successive derivatives of a function are obtained in terms of the values of the function at unequally spaced arguments and the corresponding distances between the successive arguments using Lagrangian polynomials of various degrees. The remainder term is also obtained. Tables of coefficients in the formulas for the first four derivatives are given in intervals of 0.01 for the special case where only one spacing at either end is different from the others, as is often encountered near a curved boundary, for different ratios of this spacing to the others.

A general discussion of applying these formulas to the numerical solution of partial differential equations is made. In particular, the application to the equations of the elliptic type is illustrated with a problem involving derivatives of both first and second order and with the value of the function given on a circular boundary. After replacing the derivatives by the formulas based on fourth-degree polynomials, the resulting set of equations is solved by both relaxation and matrix methods. Similar application to problems of compressible flow past isolated and cascade airfoils and through turbomachines, and temperature distribution and thermal stress in cooled turbine blades, is indicated.

#### INTRODUCTION

In recent years, use of numerical methods in the solution of partial differential equations that are intractable by exact analytical methods increased. In these methods, a network of pivotal points over the domain of the problem is considered and the differential equation is replaced by its finite-difference expressions that involve the values of the "wanted function" at these points.

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In general, the accuracy of the solution depends on the fineness of the network and on the accuracy of the finite-difference expressions used. For the case where the spacing between the points is everywhere the same, differentiation formulas based on polynomials up to the ninth degree are available (reference 1). In most practical problems, however, a part of or the whole boundary line of the domain is often curved, which renders the spacing near the boundary different from that elsewhere. In the past, a linear or higher-order extrapolation formula was usually used to obtain, from the given boundary value, the value at a fictitious point outside the boundary at a distance from the first point inside the boundary equal to that between all the other points (references 2 and 3). In reference 4, a differentiation formula based on unequal distances between the points is obtained for the second-order derivative using a seconddegree polynomial, but the error term is not given. It is felt that a need exists for general formulas for computing different orders of derivatives by using the values of functions at nonequidistant points based on polynomials of various degrees. Such formulas will not only help to solve more conveniently those problems with curved boundaries, especially for computation on large-scale digital computing machines, but will also help to reduce the number of points involved in a problem by using relatively small spacings only where needed. The formulas will also help to determine more accurately the non-homogeneous terms in the differential equation that are not given but are to be obtained through differentiation during the calculation.

In connection with the theoretical investigation being conducted at the NACA Lewis laboratory on fluid flow past cascades of arbitrary airfoils and through turbomachines with arbitrary hub and casing shapes, general differentiation formulas are obtained in terms of the values of the function at non-equidistant points and the corresponding distances between the successive points by using Lagrangian polynomials of various degrees. The error term is also obtained. Tables of coefficients for the first four derivatives for the special case where only one spacing at one end is different from the others, as often encountered near a curved boundary, are computed for different ratios of the unequal distance to the equal distances from 0.1 to 1.29 in intervals of 0.01.

A general discussion of the application of these formulas to the numerical solutions of partial differential equations is presented, including the advantages of using a higher-degree polynomial. The method is illustrated with a problem involving a second-order partial differential equation with a circular boundary, which is treated in reference 3 by the use of a difference-correction method. After the

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derivatives are replaced by fourth-degree differentiation formulas, the resulting equations are solved by both relaxation and matrix methods. The application to fluid flow past isolated and cascade airfoils and through turbomachines and to temperature distribution and thermal stress in cooled turbine blades are indicated.

### SYMBOLS

The following symbols are used in this report:

m <sub>A</sub> i n j	differentiation coefficients in equation (15) used to multiply function value at point $x_j$ to give $m^{th}$ derivative at $x_j$ using $n^{th}$ -degree polynomial
a,b,c,d	successive distances between $x_0$ , $x_1$ , $x_2$ , $x_3$ , and $x_4$
m <sub>B</sub> i n j	$n^{m}A_{j}^{i}/II_{n+1}(x_{j})$
${}^{\mathrm{m}}_{\mathbf{n}}{}^{\mathbf{c}}\mathbf{j}$	$\frac{m}{n}B_{j}^{i}$ $b^{m}$
$D^m y$	$\mathtt{m}^{ ext{th}}$ derivative of y with respect to x
[d]	diagonal matrix
E	first term in R
F,G,H,J,K	functions of $\eta$ and $\zeta$
[I]	unit matrix
$J_{o}$	Bessel function of first kind of order zero
[L]	lower triangular matrix
[1]	lower triangular matrix with unit diagonal elements
[M]	coefficient matrix
m	order of derivative

number of grid points

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degree of polynomial
{P},{Q},{S},
               column matrices
               velocity
q
{^m\!R^i}_n
               remainder term of mth derivative at point xi
                 obtained by using nth-degree polynomial
               polar coordinates
r,z
               upper triangular matrix with unit diagonal elements
[u]
               composite matrix
v
               independent variable
x
               dependent variable
y
               submatrix
order of [a]
β
γ
               ratio of specific heats
η, ξ
               rectangular coordinates
               constant
               value of x lying between greatest and least of x
\Pi_{n+1}(x)
               product of (n+1) factors, (x-x_0), (x-x_1), . . .
                 (x-x_n)
               density
               dependable variable
               stream function
```

Superscripts:

1,2, . . . N interior points

a,b,c,d, . . . boundary points

', ", "', iv first to fourth-order derivatives

n n<sup>th</sup> derivative

Subscripts:

i,j,k,l,p,q denote value at given arguments

0 stagnation value

#### GENERAL DIFFERENTIATION FORMULAS

If y = f(x) is a function of x and the value of y at n+1 arguments or points  $x_0, x_1, \dots, x_i, \dots, x_n$  are known, the general Lagrangian interpolation polynomial of degree n is (reference 5)

$$y = \frac{(x-x_1)(x-x_2) \cdot (x-x_n)}{(x_0-x_1)(x_0-x_2) \cdot (x_0-x_n)} y_0 + \frac{(x-x_0)(x-x_2) \cdot (x-x_n)}{(x_1-x_0)(x_1-x_2) \cdot (x_1-x_n)} y_1 + \cdots + y_n$$

$$\frac{(x-x_0)(x-x_1) \cdot (x-x_{n-1})}{(x_n-x_0)(x_n-x_1) \cdot (x_n-x_{n-1})} y_n + \frac{f^{(n+1)(\xi)}(x-x_0)(x-x_1)}{(n+1)!} (x-x_0)(x-x_1) \cdot (x-x_n) (1)$$

in which the last term is the remainder term with the value of lying between the least and the greatest of the numbers x,  $x_0$ ,  $x_1$ , . .  $x_n$ . By using

$$\Pi_{n+1}(x) = (x-x_0)(x-x_1) \dots (x-x_n)$$
 (2)

and its first derivative

$$\Pi_{n+1}'(x) = \Pi_{n+1}(x) \sum_{k=0}^{n} \frac{1}{x-x_k}$$
 (3)

equation (1) can be written as

$$y = \sum_{j=0}^{n} \frac{II_{n+1}(x)}{x-x_{j}} \frac{y_{j}}{II_{n+1}(x_{j})} + {}_{n}^{0}R$$
 (4)

where

$${}_{n}^{O}R = \frac{\Pi_{n+1}(x)}{(n+1)!} f^{(n+1)}(\xi)$$
 (5)

and

$$\Pi'_{n+1}(x_j) = (x_j - x_0)(x_j - x_1) \dots (x_j - x_{j-1})(x_j - x_{j+1}) \dots (x_j - x_n)$$
 (6)

From equations (3), (4), and (5), the formulas for the successive derivatives of y with respect to x at any point x can be obtained as follows:

$$D^{1}y = \sum_{j=0}^{n} \left[ \frac{y_{j}}{\prod_{n+1}^{j}(x_{j})} \frac{\prod_{n+1}^{j}(x)}{x-x_{j}} \sum_{\substack{k=0 \ k \neq j}}^{n} \frac{1}{x-x_{k}} + \frac{1}{n}R \right]$$
 (7)

where

$$\frac{1}{n}R = \frac{II_{n+1}'(x)}{(n+1)!} f^{(n+1)}(\xi) + \frac{II_{n+1}(x)}{(n+1)!} f^{(n+2)}(\xi) \frac{d\xi}{dx} + \dots$$
 (8)

$$D^{2}y = 2! \sum_{j=0}^{n} \left[ \frac{y_{j}}{\prod_{n+1}^{i}(x_{j})} \frac{\prod_{n+1}^{i}(x)}{x-x_{j}} \sum_{\substack{k=0 \ k \neq j}}^{n} \left( \frac{1}{x-x_{k}} \sum_{\substack{l=k+1 \ l \neq j}}^{n} \frac{1}{x-x_{l}} \right) \right] + {}_{n}^{2}R \quad (9)$$

where

$$\frac{2}{n^{R}} = \frac{\prod_{n+1}^{"}(x)}{(n+1)!} f^{(n+1)}(\xi) + 2 \frac{\prod_{n+1}^{"}(x)}{(n+1)!} f^{(n+2)}(\xi) \frac{d\xi}{dx} + \dots (10)$$

$$D^{3}y = 3! \sum_{j=0}^{n} \left\{ \frac{y_{j}}{II'_{n+1}(x_{j})} \frac{II_{n+1}(x)}{x-x_{j}} \sum_{\substack{k=0\\k\neq j}}^{n} \left[ \frac{1}{x-x_{k}} \sum_{\substack{l=k+1\\l\neq j}}^{n} \left( \frac{1}{x-x_{l}} \sum_{\substack{p=l+1\\p\neq j}}^{n} \frac{1}{x-x_{p}} \right) \right] \right\} + {}_{n}^{3}R$$
(11)

where

$${}^{3}_{n}R = \frac{II_{n+1}^{"}(x)}{(n+1)!}f^{(n+1)}(\xi) + 3\frac{II_{n+1}^{"}(x)}{(n+1)!}f^{(n+2)}(\xi)\frac{d\xi}{dx} + \dots$$
 (12)

$$D^{4}y = 4! \sum_{j=0}^{n} \left( \frac{y_{j}}{II_{n+1}^{i}(x_{j})} \frac{II_{n+1}(x)}{x-x_{j}} \right)$$

$$\sum_{k=0}^{n} \left\{ \frac{1}{x-x_k} \sum_{\substack{l=k+1\\l\neq j}}^{n} \left[ \frac{1}{x-x_l} \sum_{\substack{p=l+1\\p\neq j}}^{n} \left( \frac{1}{x-x_p} \sum_{\substack{q=p+1\\q\neq j}}^{n} \frac{1}{x-x_q} \right) \right] \right\}^{+} {}_{n}^{4R}$$
(13)

where

$$\frac{4}{n^{R}} = \frac{\prod_{n+1}^{1}(x)}{(n+1)!} f^{(n+1)}(\xi) + 4 \frac{\prod_{n+1}^{"}(x)}{(n+1)!} f^{(n+2)}(\xi) \frac{d\xi}{dx} + \dots$$
 (14)

and so forth.

In the preceding formulas of the remainder terms, only the first two terms are given. The value of  $\xi$  is unknown. For the case where  $f^{(n+1)}(x)$  and  $f^{(n+2)}(x)$  do not vary much over the range of x, they may be estimated by the values at the point x in question by using appropriate differentiation formulas.

For the case where the derivatives are required only at the given arguments  $x_i$ , the fact that most of the terms containing  $\Pi_{n+1}(x_1)$  vanish greatly simplifies these formulas. The resulting expression for the first derivative agrees with that given in reference 5. For the present work, it is found to be more convenient to keep the general form as previously given, which enables the same operation at all points. Thus, the  $m^{th}$  derivative of y at  $x_i$  based on a polynomial of  $n^{th}$  degree  $(n \ge m)$  may be written as

$$(D^{m}y)_{x=x_{i}} = m! \sum_{j=0}^{n} \frac{{}_{n}^{m}A_{j}^{i} y_{j}}{II_{n+1}^{i}(x_{j})} + {}_{n}^{m}R^{i}$$
(15)

$$= \sum_{j=0}^{n} {}_{n}^{m} B_{j}^{i} y_{j} + {}_{n}^{m} R^{i}$$
 (16)

For m = 1

$${}_{n}^{1}A_{j}^{i} = \frac{II_{n+1}(x_{i})}{x_{i}-x_{j}} \sum_{\substack{k=0\\k\neq j}}^{n} \frac{1}{x_{i}-x_{k}}$$
(17)

$$\frac{1}{n}R^{i} = \frac{II_{n+1}^{i}(x_{1})}{(n+1)!}f^{(n+1)}(\xi) + \frac{II_{n+1}(x_{1})}{(n+1)!}f^{(n+2)}(\xi) \frac{d\xi}{dx} + \cdots$$
 (18)

For m = 2,

$${}_{n}^{2}A_{j}^{i} = \frac{II_{n+1}(x_{i})}{x_{i}-x_{j}} \sum_{\substack{k=0\\k\neq j}}^{n} \left(\frac{1}{x_{i}-x_{k}} \sum_{\substack{l=k+1\\l\neq j}}^{n} \frac{1}{x_{i}-x_{l}}\right)$$
(19)

and so forth. With this setup, the expression of the coefficients A in terms of the given unequal distances between the points can be obtained very easily; for example, if the successive spacings between five points  $x_0$ ,  $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$  are a, b, c, and d, resively, the coefficients A can be obtained in the following manner: First, the expressions of  $\Pi_5(x_1)$ , including the factor zero for i=0,1,2,3,4, are written. For example, at i=1,  $\Pi_5(x_1)$  is a(0)(-b)(-b-c)(-b-c-d). Coefficients  $\frac{1}{4}A_1^l$  for j=0,1,2,3,4 are then obtained simply by taking out the appropriate  $x_1-x_j$  factor from  $\Pi_5(x_1)$  and applying the summation operation. At all of the other points except at j=i=1, all of the terms except one vanish because of the factor zero in  $\Pi_5(x_1)$ , with the result  $\frac{1}{4}A_1^l$  equal to -b(b+c)(b+c+d); ab(b+c)+ab(b+c+d)+a(b+c)(b+c+d)-b(b+c+d); a(b+c)(b+c+d); ab(b+c)+ab(b+c+d)+a(b+c)(b+c+d)-b(b+c+d); ab(b+c+d); and ab(b+c) at j=0,1,2,3,4, respectively. The other coefficients can be obtained in a similar manner.

The expressions of the various coefficients in formula (15) in terms of the unequal spacings a,b, . . . between successive arguments, using three, four, and five points, respectively, are given in the following formulas:

General Three-Point Differentiation Formula

$$(D^{m}y)_{x=x_{1}} = m! \sum_{j=0}^{2} \frac{{}_{2}^{m}A^{j}_{j}}{II_{3}^{i}(x_{j})} + {}_{2}^{m}R^{j}$$

m	i	$A_{O}$	Al	A2	$E/f^{(3)}(\xi)$
	0	-(2a+b)	-(a+b)	<b>-</b> a	a(a+b)/6
1	1	<b>-</b> b	a-b	a	-ab/6
	2	ъ	a+b	a+2b	(a+b)b/6
	0	1	1	1	-(2a+b)/3
2	1	1	1	.1	(a-b)/3
	2	1	1	1	(a+2b)/3

 $II_{3}^{i}(x_{0}) II_{3}^{i}(x_{1}) II_{3}^{i}(x_{2})$ a(a+b) -ab (a+b)b

# General Four-Point Differentiation Formula

$$(D^{m}y)_{x=x_{1}} = m! \sum_{j=0}^{3} \frac{\sum_{j=0}^{m} j}{\sum_{j=0}^{m} x_{j}^{j}} + \sum_{j=0}^{m} R^{j}$$

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m	i	A <sub>O</sub>	A <sub>1</sub>	Az	A <sub>3</sub>	E/f <sup>(4)</sup> (ξ)
	0	[a(a+b)+a(a+b+c)+] (a+b)(a+b+c)	(a+b)(a+b+c)	a(a+b+c)	a(a+b)	$-\frac{a(a+b)(a+b+c)}{24}$
1	1	b(b+c)	-ab-a(b+c)+ b(b+c)	-a(b+c)	-ab	ab(b+c) 24
-	2	-bc	-(a+b)c	(a+b)b-(a+b)c-bc	d(d+a)	_ <u>(a+b)bc</u> 24
	3	(b+c)c	(a+b+c)c	(a+b+c)(b+c)	(a+b+c)(b+c)+ (a+b+c)c+ (b+c)c	(a+b+c)(b+c)c 24
	0	-a-(a+b)-(a+b+c)	-(a+b)-(a+b+c)	-a-(a+b+c)	-a-(a+b)	$\frac{1}{12} \begin{bmatrix} a(a+b)+\\ a(a+b+c)+\\ (a+b)(a+b+c) \end{bmatrix}$
2	1	-b-(b+c)	a-b-(b+c)	a-(b+c)	a-b	$\frac{1}{12}\begin{bmatrix} -ab-a(b+c)+\\ b(b+c) \end{bmatrix}$
٥	s	b-c	(a+b)-c	(a+b)+b-c	(a+b)+b	$\frac{1}{12} \begin{bmatrix} (a+b)b-\\ (a+b)c-bc \end{bmatrix}$
	3	(b+c)+c	(a+b+c)+c	(a+b+c)+(b+c)	(a+b+c)+(b+c)+c	$\frac{1}{.12} \begin{bmatrix} (a+b+c)(b+c)+\\ (a+b+c)c+\\ (b+c)c \end{bmatrix}$
	0	1	1	1	1.	- a+(a+b)+(a+b+c)
3	1	1	1	1	1	a-b-(b+c)
	2	1	1	1	1	(a+b)+b-c
	3	1	1	1	1	(a+b+c)+(b+c)+c

$\Pi_{4}^{\dagger}(\mathbf{x}_{\mathrm{O}})$	$\Pi_4^s(\mathbf{x}_1)$	$\Pi_4'(\mathbf{x}_2)$	Π <sub>4</sub> ( <b>x</b> <sub>3</sub> )
-a(a+b)(a+b+c)	ab(b+c)	-(a+b)bc	(a+b+c)(b+c)c

General Five-Point

$$(D^{m}y)_{x=x_{1}} = m! \sum_{j=0}^{4} \frac{\prod_{j=0}^{m-1} y_{j}}{\prod_{j=0}^{r} (x_{j})} + \prod_{j=0}^{m} R^{j}$$

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m	i	A <sub>O</sub>	A <sub>1</sub>	A <sub>2</sub>
	0	a(a+b)(a+b+c+d)+ a(a+b)(a+b+c+d)+ a(a+b+c)(a+b+c+d)+ (a+b)(a+b+c)(a+b+c+d)	-(a+b)(a+b+c)(a+b+c+d)	-a(a+b+c)(a+b+c+d)
	1	-b(b+c)(b+c+d)	[ab(b+c)+ab(b+c+d)+ a(b+c)(b+c+d)- b(b+c)(b+c+d)	a(b+c)(b+c+d)
1	2	bc(c+d)	(a+b)c(c+d)	[-(a+b)bc-(a+b)b(c+d)+ (a+b)c(c+d)+bc(c+d)
	3	-(b+c)cd	-(a+b+c)cd	-(a+b+c)(b+c)d
	4	(b+c+d)(c+d)d	(a+b+c+d)(c+d)d	(a+b+c+d)(b+c+d)d
	0	a(a+b)+a(a+b+c)+a(a+b+c+d)+ (a+b)(a+b+c)+(a+b)(a+b+c+d)+ (a+b+c)(a+b+c+d)	(a+b)(a+b+c)+ (a+b)(a+b+c+d)+ (a+b+c)(a+b+c+d)	[a(a+b+c)+a(a+b+c+d)+ (a+b+c)(a+b+c+d)
	1	[b(b+c)+b(b+c+d)+ (b+c)(b+c+d)	[-ab-a(b+c)-a(b+c+d)+ b(b+c)+b(b+c+d)+ (b+c)(b+c+d)	[-a(b+c)-a(b+c+d)+ (b+c)(b+c+d)
2	2	-bc-b(c+d)+c(c+d)	$\begin{bmatrix} -(a+b)c-(a+b)(c+d)+\\ c(c+d) \end{bmatrix}$	[(a+b)b-(a+b)c-(a+b)x (c+d)-bc-b(c+d)+c(c+d
	3	(b+c)c-(b+c)d-cd	(a+b+c)c-(a+b+c)d-cd	(a+b+c)(b+c)-(a+b+c)d- (b+c)d
	4	[(b+c+d)(c+d)+(b+c+d)d+] [(c+d)d	[(a+b+c+d)(c+d)+ (a+b+c+d)d+(c+d)d]	(a+b+c+d)(b+c+d)+ (a+b+c+d)d+(b+c+d)d
	0	-a-(a+b)-(a+b+c)-(a+b+c+d)	[-(a+b)-(a+b+c)-] (a+b+c+d)	-a-(a+b+c)-(a+b+c+d)
	1	-b-(b+c)-(b+c+d)	a-b-(b+e)-(b+c+d)	a-(b+c)-(b+c+d)
3	2	b-c-(c+d)	(a+b)-c-(c+d)	(a+b)+b-c-(c+d)
	3	(b+c)+c-d	(a+b+c)+c-d .	(a+b+c)+(b+c)-d
	4	(b+c+d)+(c+d)+d	(a+b+c+d)+(c+d)+d	(a+b+c+d)+(b+c+d)+d
	0	1	1	. 1
	1	1	1	1
4	2	1	1	1
	3	1	1	1
	4	1	1	<b>1</b> , , , , , , , ,
		Π <sub>1</sub> (x <sub>0</sub> )	п (x)	П <mark>'</mark> (ж <sub>2</sub> )

-ab(b+c)(b+c+d)

(a+b)bc(c+d)

a(a+b)(a+b+c)(a+b+c+d)

Differentiation Formula

-(a+b+c)(b+c)cd

$(D^m y)_{x=x_1} = m!$	$\sum_{j=0}^{4} \frac{\frac{m}{4}A_{j}^{1} y_{j}}{\prod_{5}^{i}(x_{j})} + \frac{m}{4}R^{1}$
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NACA A<sub>3</sub> -a(a+b)(a+b+c+d) -a(a+b)(a+b+c)  $\frac{1}{120}$  a(a+b)(a+b+c)(a+b+c+d) ab(b+c) ab(b+c+d)  $-\frac{1}{120}$  ab(b+c)(b+c+d) -(a+b)b(c+d)  $\frac{1}{120}$  (a+b)(bc(c+d) -(a+b)bc (a+b+c)(b+c)c-(a+b+c)x (b+c)d-(a+b+c)cd-(b+c)cd (a+b+c)(b+c)c  $-\frac{1}{120}$  (a+b+c)(b+c)cd  $\frac{1}{120}$  (a+b+c+d)(b+c+d)(c+d)d (&+b+c+d)(b+c+d)(c+d)+ (&+b+c+d)(b+c+d)d+ (&+b+c+d)(c+d)d+(b+c+d)(c+d)d (a+b+c+d)(b+c+d)(c+d)  $-\frac{1}{60} \left[ \frac{a(a+b)(a+b+c)+a(a+b)(a+b+c+d)+}{a(a+b+c)(a+b+c+d)+(a+b)(a+b+c)(a+b+c+d)} \right]$ a(a+b)+a(a+b+c+d)+ (a+b)(a+b+c+d) a(a+b)+a(a+b+c)+ (a+b) (a+b+c) -ab-a(b+c+d)+ b(b+c+d) 1 [ab(b+c)+ab(b+c+d)+a(b+c)(b+c+d)-]
b(b+c)(b+c+d) -ab-a(b+c)+b(b+c)  $\begin{bmatrix} (a+b)b-(a+b)(c+d)-\\ b(c+d) \end{bmatrix}$  $\frac{1}{60} \begin{bmatrix} -(a+b)bc-(a+b)b(c+d)+\\ (a+b)c(c+d)+bc(c+d) \end{bmatrix}$ (a+b)b-(a+b)c-bc  $\frac{1}{60} \left[ \frac{(a+b+c)(b+c)c-(a+b+c)(b+c)d-(a+b+c)cd-(a+b+c)cd}{(a+b+c)cd-(b+c)cd} \right]$  $\begin{bmatrix}
(a+b+c)(b+c)+(a+b+c)c-\\
(a+b+c)d+(b+c)c-(b+c)d-cd
\end{bmatrix}$ (a+b+c)(b+c)+(a+b+c)c+(b+c)c (a+b+c+d)(b+c+d)+(a+b+c+d)x (c+d)+(b+c+d)(c+d) (a+b+c+d)(b+c+d)+(b+c+d)(c+d)+ (a+b+c+d)(c+d)+(b+c+d)d+ (a+b+c+d)d+(c+d)d  $\frac{1}{60} \left[ \begin{array}{l} (a+b+c+d)(b+c+d)(c+d) + (a+b+c+d)(b+c+d)d+ \\ (a+b+c+d)(c+d)d + (b+c+d)(c+d)d \end{array} \right]$  $\frac{1}{20} \left[ \frac{a(a+b)+a(a+b+c)+a(a+b+c+d)+(a+b)(a+b+c)+}{(a+b)(a+b+c+d)+(a+b+c)(a+b+c+d)} \right]$ -a-(a+b)-(a+b+c+d) -a-(a+b)-(a+b+c)  $\frac{1}{20} \begin{bmatrix} -ab-a(b+c)-a(b+c+d)+b(b+c)+\\ b(b+c+d)+(b+c)(b+c+d) \end{bmatrix}$ a-b-(b+c+d) a-b-(b+c)  $\frac{1}{20} \begin{bmatrix} (a+b)b-(a+b)c-(a+b)(c+d)-\\ bc-b(c+d)+c(c+d) \end{bmatrix}$ (a+b)+b-(c+d) (a+b)+b-c (a+b+c)+(b+c)+c-d  $\frac{1}{20} \left[ \frac{(a+b+c)(b+c)+(a+b+c)c}{-(a+b+c)d+(b+c)c-(b+c)d-cd} \right]$ (a+b+c)+(b+c)+c (a+b+c+d)+(b+c+d)+(c+d)  $\frac{1}{20} \left[ (a+b+c+d)(b+c+d)+(b+c+d)(c+d)+(a+b+c+d)(c+d)+ \right]$ (a+b+c+d)+(b+c+d)+(c+d)+d 1  $-\frac{1}{5}$  [a+(a+b)+(a+b+c)+(a+b+c+d)] 1  $\frac{1}{5}$  [a-b-(b+c)-(b+c+d)]  $\frac{1}{5}[(a+b)+b-c-(c+d)]$  $\frac{1}{5}[(a+b+c)+(b+c)+c-d]$  $\frac{1}{5}$  [(a+b+c+d)+(b+c+d)+(c+d)+d] 1 (x ) П (x)

(a+b+c+d)(b+c+d)(c+d)d

The corresponding simplified expressions for the special case where only the first spacing is different from the rest, as often encountered near the boundary of a problem, are given in the following formulas: In these formulas, r is equal to the ratio of a to the other uniform spacings b=c=d . . . . For ready applications, the differentiation coefficients and the coefficient of the first remainder term of this special case are computed for a range of r from 0.10 to 1.29, in intervals of 0.01 and are given in the attached tables.

Three-Point Differentiation Formula for a=rb

$$(D^{m}y)_{x=x_{1}} = m! \sum_{j=0}^{2} \frac{{}_{2}^{m}A_{j}^{i}y_{j}}{II_{3}^{i}(x_{j})} + {}_{2}^{m}R^{i}$$

m	i	A <sub>O</sub>	Al	AZ	$E/f^{(3)}(\xi)$
,	0	-(1+2r)b	-(1+r)t	-rb	$\frac{1}{6}$ r(1+r)b <sup>2</sup>
1	1	<b>-</b> b	-(1-r)b	rb	$-\frac{1}{6}$ rb <sup>2</sup>
	2	ъ	(1+r)b	(2+r)b	$\frac{1}{6}$ (1+r)b <sup>2</sup>
	0	1	1	1	$-\frac{1}{3}$ (1+2r)b
2	1	1	ı	1	$-\frac{1}{3}$ (1-r)b
	2	1	1	1	$+\frac{1}{3}(2+r)b$

$\Pi_3^{!}(x_0)$	$\Pi_3^!(x_1)$	$\Pi_3'(x_2)$
r(1+r)b <sup>2</sup>	-rb <sup>2</sup>	(1+r)b <sup>2</sup>

# Four-Point Differentiation Formula for a=rb=rc

$$(D^{m}y)_{x=x_{1}} = m! \sum_{j=0}^{3} \frac{\sum_{j=0}^{m} i y_{j}}{\prod_{j=1}^{j} (x_{j})} + \sum_{j=0}^{m} R^{j}$$

	_		T	·	·	
m	i	A <sub>O</sub>	A <sub>1</sub>	A <sub>2</sub>	A3	E/f <sup>(4)</sup> (ξ)
	0	$\begin{bmatrix} r(2+r)+\\ 2(1+r)^2 \end{bmatrix} b^2$	(l+r)(2+r)b <sup>2</sup>	r(2+r)b <sup>2</sup>	r(1+r)b <sup>2</sup>	$-\frac{r(1+r)(2+r)b^3}{24}$
	1	252	(2-3r)b <sup>2</sup>	-2rb <sup>2</sup>	-rb <sup>2</sup>	$\frac{2rb^3}{24}$
1	2	-b <sup>2</sup>	-(1+r)b <sup>2</sup>	-b <sup>2</sup>	(1+r)b <sup>2</sup>	$-\frac{(1+r)b^3}{24}$
	3	2p2	(2+r)b <sup>2</sup>	2(2+r)b <sup>2</sup>	(8+3r)b <sup>2</sup>	$\frac{2(2+r)b^3}{24}$
	0	-3(l+r)b	-(3+2r)b	-2(1+r)b	-(1+2r)b	$\frac{[r(2+r)+2(1+r)^2]b^2}{12}$
	1	<b>-</b> 3b	-(3-r)b	-(2-r)b	-(1-r)b	(2-3r)b <sup>2</sup>
2	2	0	rb	(1+r)b	(2+r)b	- <u>b<sup>2</sup></u>
	3	3b	(3+r)b	(4+r)b	(5+r)b	(8+3r)b <sup>2</sup>
	0	1	1	1	1	_ <u>3(1+r)b</u>
3	1	1	1	1	1	$-\frac{(3-r)b}{4}$
	2	1	1	1	1	(1+r)b 4
	3	1	1	1	1	(5+r)b 4

$\Pi_4^{\prime}(\mathbf{x}_0)$	$\Pi_4^{\prime}(\mathbf{x}_1)$	Π <mark>((x</mark> 2)	Π <sub>4</sub> (x <sub>3</sub> )
-r(1+r)(2+r)b <sup>3</sup>	2rb <sup>3</sup>	-(1+r)b <sup>3</sup>	2(2+r)b <sup>3</sup>

Five-Point Differentiation Formula for ampharement

(Dmax) x=x1	=	m!	j=0	$\frac{4^{A_j}y_j}{\Pi_j(x_j)} +$	m <sub>R</sub> 1
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m	1	<b>A</b> <sub>0</sub>	Al	A <sub>2</sub>	A <sub>3</sub> .	A <sub>j4</sub>	E/r <sup>(5)</sup> (ξ)
	0	(1+r)(2+r)(3+r)+ r(2+r)(3+r)+ r(1+r)(3+r)+ r(1+r)(2+r) b3	-(1+r)(2+r)(3+r)b <sup>3</sup>	-r(2+r)(3+r)b3	-r(1+r)(3+r)b3	-r(1+r)(2+r)b <sup>3</sup>	1/120 r(1+r)(2+r)(3+r)b4
	1	-6b <sup>3</sup>	(-6+11r)b <sup>3</sup>	(6r)b <sup>3</sup>	(3r)b <sup>3</sup>	2rb3	- 1/20 rb4
1	2	2b <sup>3</sup>	2(1+r)b <sup>3</sup>	(1-r)b3	-2(1+r)b <sup>3</sup>	-(1+r)b <sup>3</sup>	1 (1+r)b4
	3	-2b <sup>3</sup>	-(2+r)b3	-2(2+r)b <sup>3</sup>	-(4+r)b3	2(2 <del>+r</del> )b3.	$-\frac{1}{60}$ (2+r)b4
	4	663	2(3+r)b <sup>3</sup>	3(3+r)b3	6(3+r)b3	(39+11r)b <sup>3</sup>	1 (3+r)bl4
	0	[(1+r)(5+2r)+ (2+r)(3+4r)]b <sup>2</sup>	[(1+r)(5+2r)+ (2+r)(3+r)]b <sup>2</sup>	$\begin{bmatrix} r(5+2r)+\\ (2+r)(3+r) \end{bmatrix} b^2$	$\begin{bmatrix} 2\mathbf{r}(2+\mathbf{r})+\\ (1+\mathbf{r})(3+\mathbf{r}) \end{bmatrix} b^2$	$\begin{bmatrix} \mathbf{r}(3+2\mathbf{r})+\\ (1+\mathbf{r})(2+\mathbf{r}) \end{bmatrix} \mathbf{b}^2$	$-\frac{1}{60}\begin{bmatrix} (1+r)(2+r)(3+r)+\\ r(2+r)(3+r)+\\ r(1+r)(3+r)+\\ r(1+r)(2+r) \end{bmatrix} 5^{3}$
	1	116 <sup>2</sup>	(11-6r)b <sup>2</sup>	(6-5r)b <sup>2</sup>	(3-4r)b <sup>2</sup>	(2-3r)b <sup>2</sup>	160 (-6+11r)b3
2	2	-b <sup>2</sup>	-(1+3r)b <sup>2</sup>	-(3+2r)b <sup>2</sup>	-(3+r)b <sup>2</sup>	-b <sup>2</sup>	$\frac{1}{60}(1-r)b^3$
	3	-b <sup>2</sup>	-b <sup>2</sup>	rb <sup>2</sup>	(3+2r)b <sup>2</sup>	(8+3r)b <sup>2</sup>	$-\frac{1}{60}(4+r)b^3$
	4	116 <sup>2</sup>	(11+3r)b <sup>2</sup>	(15+4r)b <sup>2</sup>	(21+5r)b <sup>2</sup>	(29+6r)b <sup>2</sup>	1 60 (39+11r)b <sup>3</sup>
	0	-(6+4r)b	-(6+3r)b	-(5+3r)b	-(4+3r)b	-3(1+r)b	$\frac{1}{20} \left[ \frac{(1+r)(5+2r)+}{(2+r)(3+4r)} \right] b^2$
	1	-6ъ	-(6-r)b	-(5-r)b	-(4 <b>-r</b> )b	-(3-r)b	$\frac{1}{20}$ (11-6r) $b^2$
3	2	<b>-</b> 2b	-(2-r)b	-(1-r)b	rъ	(1+r)b	$-\frac{1}{20}$ (3+2r)b <sup>2</sup>
	3	2ъ	(2+r)b	(3+r)b ·	(4+r)b	(5+r)b	1/20 (3+2r)b <sup>2</sup>
	4	6ъ	(6+r)b	(7+r)b	(8+r)b	(9+r)b ·	1/20 (29+6r)b <sup>2</sup>
	0	1	1	1	1	1	- ½ (6+4x)b
	1	1	1	1	1	1	- ½ (6-r)b
4	2	1	1	1	1	1	- \frac{1}{5} (1-r)b
	3	1	1	1	1	· 1	1/5 (4+r)b
	4	1	1	1	1	1	1 (9+r)b

In all formulas and tables, E denotes the first term in the remainder series. If the value of r of a given problem lies between computed intervals, either linear or higher-order interpolation, depending upon the value of r and the number of significant figures required, may be used to obtain the desired value. In the coefficient tables where r=1, the first term in the remainder series of some derivatives is equal to zero, therefore the second remainder term is required. Because of the unknown nature of  $d\xi/dx$  in the second remainder term, the error term listed in the coefficient tables is obtained by using a Taylor series expansion at the point  $x_i$  in question.

Although the tables of coefficients are computed for the case where the first interval is different from the others, they may also be used for the case where the last interval is different from the others by taking the coefficient in the reversed order and multiplying by (-1)<sup>m</sup>, as indicated by the headings at the bottom of these tables. These two headings could be used together to get a short interval for interpolation in the case of three-point formulas.

It may be noted that in the formulas, the coefficients A satisfy the following relation:

and that in the attached tables, the coefficients  ${}^m\!B^i_{\ j}$  satisfy the following relations

$$\sum_{\mathbf{j}=0}^{\mathbf{n}} \mathbf{n} \mathbf{B}_{\mathbf{j}}^{\mathbf{i}} = 0 \tag{22}$$

and

$$\sum_{j=0}^{n} (x_j - \lambda)^k {m \choose n} B_j^i = {1 \choose 0} {m = k \choose m > k}$$
(23)

where  $\lambda$  is any convenient constant.

#### APPLICATION TO SOLUTION OF PARTIAL DIFFERENTIAL EQUATIONS

The numerical solution of partial differential equations consists of two main steps; namely, replacing the differential equation by its finite-difference expression at a number of chosen nodal points and solving the unknowns from the resulting set of algebraic equations. The differentiation formulas are presented herein in order to obtain more accurate and convenient expressions of the finite-difference equations near a curved boundary and also to enable the use of a network of varying spacings, which may be very desirable in the machine computation of problems involving a large number of points, such as encountered in fluid-flow problems.

Consider the following type of partial differential equation of the second order frequently encountered in engineering problems:

$$F \frac{\partial^2 \varphi}{\partial \eta^2} + G \frac{\partial \varphi}{\partial \eta} + H \frac{\partial^2 \varphi}{\partial \zeta^2} + J \frac{\partial \varphi}{\partial \zeta} + K = 0$$
 (24)

where F, G, H, J, and K are functions of the two independent variables  $\eta$  and  $\zeta$ . In order to use the differentiation formula (16), it is convenient to choose a rectangular grid over the whole region. (See fig. 1.) Substituting equation (16) (without the remainder terms) into equation (24) in each direction at a point, the  $\phi$  value of which is  $\phi^i$ , results in the following algebraic equation:

$$\sum_{j=0}^{n} (F^{j} {}_{n}^{2}B_{j}^{i} + G^{j} {}_{n}^{1}B_{j}^{i}) \varphi^{j} + \sum_{k=0}^{n} (H^{j} {}_{n}^{2}B_{k}^{i} + J^{j} {}_{n}^{1}B_{k}^{i}) \varphi^{k} + K^{j} = 0$$
 (25)

where  $\phi^j$  and  $\phi^k$  denote  $\phi$  values along the  $\eta$  and  $\zeta$  directions, respectively. (See fig. 1 for a typical point near boundary with n = 4.)

Obviously, only when the remainder terms  ${}^2R^1$  and  ${}^1R^1$  are negligible, compared with the main terms in equation (16), will equation (25) represent the original equation (24) at these points with sufficient accuracy, and the solution obtained by solving the set of equations (25) covering the whole region will give a good approximate solution of the original differential equation (24). When formulas (18) and (20) and the E terms listed in the tables of coefficients are referred to, it is seen that the magnitude of the coefficient of the remainder term is controlled entirely by the degree of the polynomial used and the grid spacing chosen.

For nth-degree polynomial representation, derivatives of orders higher than n are involved in the remainder terms;  $\Pi'_{n+1}(x)$ ,  $\Pi''_{n+1}(x)$ , . . . are of the order of the spacing raised to the n, (n-1) . . . power, respectively; and the denominator (n+1)! increases rapidly with increasing values of n. Because numerical calculation is usually performed with dimensionless quantities, with the distance expressed in terms of a principal dimension of the problem, the spacing involved in actual calculation is usually less than 1. Hence the higher power on the spacing resulting from a higher-degree polynomial representation reduces the magnitude of the remainder term. Consequently, a higherdegree polynomial representation will always permit a smaller number of grid points necessary for a given accuracy, if the successive derivatives do not increase faster than the combined effect of a decreasing  $\mathrm{II}'_{n+1}(x)$  . . . in the numerator and an increasing (n+1)! in the denominator of the coefficient. For example, a comparison of the remainder term of the equally spaced fourth-degree or five-point formula at the off-center points  $x_1$  and  $x_3$  with the second-degree or three-point formula at the central point  $x_1$  indicates that, for the same accuracy, the five-point formula requires a grid spacing not smaller than that required by the three-point formula raised to twothirds power if the fifth derivative is not greater than the fourth derivative. Under such a condition, if the grid spacing required for a given desired accuracy by using the three-point formula is 0.1, the spacing required by using five-point formula is 0.215, which means a reduction in the number of grid points of four and eight times can be expected by going from three-point formula to five-point formula in a two-dimensional and three-dimensional problem, respectively. This saving certainly justifies the use of slightly more complicated formulas and is especially important for fluid-flow problems where a very large region must be included in the calculation. This situation is amply demonstrated in reference 3, where it is found in various problems that the inclusion of differences up to the fourth order with a relatively coarse grid gives more accurate results than using only seconddegree polynomial representation with a network four times as fine.

In most practical problems, the successive derivatives decrease in magnitude. There are, however, problems that include regions where the successive derivatives increase rapidly in magnitude. The only way to make the remainder term negligible then is to make the spacing small enough. One interesting example of this nature is given in reference 6, where the function  $y = (1+x^2)^{-1}$  has a successive even-order derivative that increases rapidly at x = 0. For a spacing of 1, it was shown that at x = 0 the accuracy of the computed derivative decreases with the increasing degree of polynomial representation. This decrease is due to

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the fact that the increase of the derivatives is greater than the increase in (n+1)! . With the spacing of 1, however, none of the three polynomials used is good enough for actual calculation. When the spacing is reduced to one-half, the fourth-degree polynomial gives better results in several places, but still none of them gives acceptable accuracy. (See table I.) When the interval is further reduced to one-fourth, the fourth-degree polynomial gives best results everywhere and is the only one that gives acceptable accuracy over the whole range. When the interval is still further reduced to one-eighth, the fourth-degree polynomial gives values accurate to within 1 percent everywhere except for y" at x = -1. The second-degree polynomials, however, give results not quite as good as those given by the fourth-degree polynomial with twice that spacing. Thus, when a small enough spacing (0.25 or 0.125) is used, the coefficient of the error term decreases with increasing order of polynomial representation (because of the higher power on the spacing term and the larger value of the factorial term in the denominator) at a rate sufficiently fast to overcome the increase of the successive derivatives at x = 0.

Before starting computation of a new problem, it is therefore always desirable to make a difference analysis of a known solution of a similar problem or of an approximate solution of the given problem to see approximately how the wanted function varies over the entire domain of the problem. In most practical problems, the successive derivatives usually decrease over most of the regions and it is always advantageous to use higher-degree polynomial representation with relatively coarse spacing. If successive derivatives are expected to increase rapidly in certain regions, however, it is essential to use very small spacings in those regions. In fluid-flow problems, where it is necessary to extend the domain of calculation far away from the object to take care of the boundary conditions, it would be desirable to use an increasingly large spacing away from the object.

After the number of nodal points of a given problem and the value of n at these points are chosen, the appropriate method of solving the resulting set of equations (25) is determined by the type of the given differential equation. If the original equation is of the elliptic type with the value of the function or its normal derivatives specified on a closed boundary, the set of equations (25) covering the whole region is to be solved simultaneously by either indirect or direct methods. If the original differential equation is of the parabolic or hyperbolic type where initial values of the function are given on a part of the boundary, the step-by-step forward integration procedure is appropriate (along characteristic lines in the case of hyperbolic equations).

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In problems of the boundary-value type, the relaxation method developed by Southwell (reference 2) has proved to be much superior to other iterative methods and has been used to solve many important engineering problems (references 2, 3, and 7 to 10). The differentiation formula obtained herein will help to obtain equation (25) more accurately and conveniently at the boundary and to reduce the labor of computation by adopting a network of varying spacing in problems involving large domains.

In problems such as fluid flow over an isolated airfoil or a cascade of airfoils including a large number of nodal points, the work involved is still great even with an increasingly large spacing away from the airfoils. Although this tremendous amount of hand computing may be avoided by solving the problems on a modern high-speed largescale digital computing machine, the machine can only be set up in a relatively simple way either with a straight iteration method of Liebmann or the faster relaxation method and many passes have to be made over the network to reduce error everywhere to an allowable limit. Because of the recent finding that the previous error estimate of the direct solution of a set of algebraic equations by the elimination technique is far too pessimistic (references 11 to 14), and because the coefficient matrix of equation (25), although of very large order, contains only a few nonzero elements in each row, thus giving a much smaller effective order of the matrix, it is quite conceivable that two- and three-dimensional-flow problems involving grid points up to a few hundred can be solved very rapidly with acceptable accuracy by this technique on the digital machines.

The simplest way of directly solving equations (25) seems to be as follows: Equations (25) are first written in the following matrix form: All the unknown  $\phi$ 's at the N interior points are denoted by superscripts 1, 2, . . . and the given boundary values are denoted with superscripts a, b, . . . w, as shown in figure 2. (The order of numbering is from top to bottom and from left to right.) Then at each interior point, there is one equation (25). When the combined coefficients of unknown  $\phi$ 's in the equation at  $\phi^{i}$  point are denoted by  $M^{i}_{j}$ , and the sum of  $K^{i}$  and the product of the known boundary  $\phi$ 's and the corresponding coefficient are denoted as  $P^{i}$ , the N sets of equation can be written in the compact matrix form

$$M_{j}^{i}$$
  $\phi^{j} = P^{i}$ 

or

$$[M] \quad \{\phi\} = \{P\} \tag{26}$$

where  $\left[ M \right]$  ,  $\left\{ \phi \right\}$  , and  $\left\{ P \right\}$  are square and column matrices of order N.

The nature of the coefficient matrix M, from the problem involving 29 unknown  $\,$   $\,$   $\,$  shown in figure 2, is indicated in figure 3. (The central-point five-point formula is used everywhere except at the points next to the boundary.) In general, the largest number in each row is located at the diagonal line. It is clearly indicated in figure 3 that the matrix M can be considered as composed of 6  $\times$  6 = 36 submatrices; the ones on the diagonal line are square matrices of order five and contains only four zero elements and the remaining ones are diagonal matrices also of order five. These submatrices are designated  $[\alpha]$  in figure 3. Wherever a curved boundary exists, a part of these submatrices is cut off, as is  $\alpha_{\bf j}^6$ . In case the three-point formula is used throughout, the order of matrix M necessarily becomes several times larger and there will be only one line of diagonal submatrices running along each side of the main ones on the main diagonal.

In equation (26), if the coefficient matrix M is nonsingular, a unique solution for  $\phi$  always exists. Although there are a number of methods to solve this matrix equation (references 12 and 13), the following method is found to be the best in taking advantage of the large number of zero elements in the given coefficient matrix M to reduce to a minimum the number of operations and recordings of the present problem. This method involves the resolution of the coefficient matrix M into the product of an upper triangular and a lower triangular matrix as follows: From the theorem of triangular resolution of a matrix (references 11 and 12),

$$[M] = [l] [d] [u]$$

where  $\begin{bmatrix} l \end{bmatrix}$  and  $\begin{bmatrix} u \end{bmatrix}$  are lower and upper triangular matrices both with unit elements along the diagonal, and  $\begin{bmatrix} d \end{bmatrix}$  is a diagonal matrix. It is found convenient to combine  $\begin{bmatrix} l \end{bmatrix}$  and  $\begin{bmatrix} d \end{bmatrix}$  into a lower triangular matrice  $\begin{bmatrix} L \end{bmatrix}$ , which yields

$$[M] = [L][u]$$
 (28)

The elements of matrices [L] and [u] can be obtained by the ordinary matrix multiplication rule as follows (superscripts and subscripts indicate the number of the row and the column, respectively):

(a) 
$$L_1^1 = M_1^1$$
  $L_1^2 = M_1^2$  . . . or  $L_1^1 = M_1^1$ 

(b) 
$$u_2^{\frac{1}{2}} = \frac{M_2^{\frac{1}{2}}}{L_1^{\frac{1}{2}}}$$
  $u_3^{\frac{1}{3}} = \frac{M_3^{\frac{1}{3}}}{L_1^{\frac{1}{3}}}$  . . . or  $u_3^{\frac{1}{3}} = \frac{M_3^{\frac{1}{3}}}{L_1^{\frac{1}{3}}}$ 

(c) 
$$L_2^2 = M_2^2 - L_1^2 u_2^1$$
  $L_2^3 = M_2^3 - L_1^3 u_2^1$  . . or  $L_2^1 = M_2^1 - L_1^1 u_2^1$ 

(d) 
$$u_3^2 = \frac{M_3^2 - L_1^2 u_3^1}{L_2^2}$$
  $u_4^2 = \frac{M_4^2 - L_1^2 u_4^1}{L_2^2} \dots$  or  $u_j^2 = \frac{M_j^2 - L_1^2 u_j^1}{L_2^2}$ 

(e) 
$$L_3^3 = M_3^3 - L_1^3 u_3^1 - L_2^3 u_3^2$$
  $L_3^4 = M_3^4 - L_1^4 u_3^1 - L_2^4 u_3^2 \dots$  or

$$L_3^{i} = M_3^{i} - L_1^{i} u_3^{1} - L_2^{i} u_3^{2}$$

(f) 
$$u_4^3 = \frac{M_4^3 - L_1^3 u_4^1 - L_2^3 u_4^2}{L_3^3}$$
  $u_5^3 = \frac{M_5^3 - L_1^3 u_5^1 - L_2^3 u_5^2}{L_3^3}$  ... or

$$u_{j}^{3} = \frac{M_{j}^{3} - L_{1}^{3} u_{j}^{1} - L_{2}^{3} u_{j}^{2}}{L_{3}^{3}}$$

and so forth. The sequence of operation is always (1) obtain L along a column, and (2) obtain u along a row. The general operation can simply be written as

(1) Operation along a column j:

$$L_{j}^{i} = M_{j}^{i} - \sum_{k=1}^{j-1} L_{k}^{i} u_{j}^{k} \quad (i \ge j)$$
 (29)

(2) Operation along a row i:

$$u_{j}^{i} = \frac{M_{j}^{i} - \sum_{k=1}^{i-1} L_{k}^{i} u_{j}^{k}}{L_{i}^{i}} \qquad (j > i)$$
(30)

The nature of [L] and [u] are indicated in figure 4. In fact, a composite matrix [V] = [L] + [u] - [T] can be used in place of separate matrices [L] and [u] to facilitate recording. Then both L and u in equations (29) and (30) are replaced by V. The composite matrix is called auxiliary matrix in reference 15, where formulas similar to equations (29) and (30) were obtained by an induction process. The composite matrix V is shown in figure 5. It may be noted that in the case of problems where there are more unknowns in the central region than shown in figure 2, matrix V will have more rows like those from row 11 to row 25. The difference between these typical rows from those above and below them is due to the unsymmetrical formulas at points near to the left and right boundaries.

When [L] and [u] are obtained, the solution of the set of equations involves the following forward and backward substitutions: Defining a column matrix Q of the same order N as P yields

$$[L] \{Q\} = \{P\}$$

$$(31)$$

giving

$$Q^{\frac{1}{2}} = \frac{P^{\frac{1}{2}}}{L_{1}^{\frac{1}{2}}}$$

$$Q^{2} = \frac{P^{2} - L_{1}^{2} Q^{1}}{L_{2}^{2}}$$

or, in general,

$$Q^{i} = \frac{P^{i} - \sum_{j=1}^{i-1} L_{j}^{i} Q^{j}}{L_{i}^{i}}$$
 (32)

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The unknown matrix  $\varphi$  is then obtained by

25

that is,

$$\omega_{M} = \omega_{M}$$

$$\phi^{N-1} \ = \ Q^{N-1} \ - \ u_N^{N-1} \ Q^N$$

or, in general,

$$\varphi^{i} = Q^{i} - \sum_{j=1}^{i+1} u^{i}_{j} Q^{j}$$
 (34)

When equation (32) is compared with equation (30), it is seen that  $Q^{i}$  is obtained in precisely the same manner as  $u^{i}$ . The column matrix P can therefore be added to the right of matrix M and treated in the same manner as the last column of M (fig. 6). In addition, it is advisable to add a checking column S to M defined by

$$S^{i} = \sum_{j=1}^{N} M_{j}^{i} + P^{i}$$
 (35)

Then one more column T is obtained behind Q, and W behind  $\phi$ . (See fig. 6.) The formulas for checking are

$$T^{i} = 1 + \sum_{j=i+1}^{N+1} V^{i}_{j}$$
 (36)

and

$$W^{i} = 1 + \varphi^{i} \tag{37}$$

If several sets of values of  $\{P\}$  are given at the same time, they can be placed behind [M] in the beginning of computation, thus obtaining several sets of  $\phi$  at the same time. This situation arises when solutions are required for different boundary values or different values

of  $K(\eta, \zeta)$  in the original differential equation (25). If solution is required for a different value of  $\{P\}$  any time after the first solution is obtained, the matrix V is always available and the work required is only the forward and backward substitution processes. In all cases, the principal work involved is the transformation of matrix M to matrix V. Once this transformation is done for a given problem, solutions for different  $\{P\}$ 's can be obtained very quickly.

This method can be extended to nonlinear differential equations, where the coefficients F, G, H, J, and K depend on  $\phi$ . One way of extending the method is to recompute the values of F, G, H, J, and K after a solution of  $\phi$  is obtained. Recomputing means, however, repetition of the whole process as shown in figure 6. For some types of elliptic differential equation such as the one encountered in subsonic flow, a much simpler method is possible. For example, the equations defining the irrotational motion of a compressible nonviscous fluid are

$$\frac{\partial}{\partial \eta} \left( \frac{1}{\rho} \frac{\partial \psi}{\partial \eta} \right) + \frac{\partial}{\partial \xi} \left( \frac{1}{\rho} \frac{\partial \psi}{\partial \xi} \right) = 0 \tag{38}$$

and

$$\frac{\rho}{\rho_0} = \left[1 - \frac{\gamma - 1}{2} \left(\frac{q}{a_0}\right)^2\right]^{\frac{1}{\gamma - 1}} \tag{39}$$

where  $\Psi$  is the stream function defined by

$$q_{\eta} = \frac{1}{\rho} \frac{\partial \psi}{\partial \xi} \qquad q_{\xi} = -\frac{1}{\rho} \frac{\partial \psi}{\partial \eta} \tag{40}$$

Equation (38) can be written as (reference 8)

$$\frac{\partial^2 \psi}{\partial \eta^2} + \frac{\partial^2 \psi}{\partial \xi^2} - \frac{1}{\rho} \left( \frac{\partial \rho}{\partial \eta} \frac{\partial \phi}{\partial \eta} + \frac{\partial \rho}{\partial \xi} \frac{\partial \psi}{\partial \xi} \right) = 0 \tag{41}$$

By taking the term involving density as constant for each calculation and as the K term in equation (25), a matrix M is obtained that is determined only by the geometric shape of the problem. The matrix V can then be used to compute successively improved values of  $\{\vec{V}\}$  using successively improved values of  $\{\vec{V}\}$ , which contains the successively improved values of K (or  $\rho$ ). For subsonic flow, the variation of density with velocity is limited, thus this process of treating the non-linearity converges rapidly (references 9 and 10). This method is

especially convenient when a large number of cases for a given isolated or cascade airfoil is required, such as with various stream Mach numbers in which case the matrices M and V remain fixed.

It is believed that the method described herein will find increasing use in problems of fluid flow past isolated and cascade airfoils, fluid flow through turbomachines, temperature distribution and thermal stress in a cooled turbine blade, and many other boundary-value problems. For an ordinary completely filled matrix of order N, the number of multiplication and division processes involved in the matrix solution is of

the order of  $\left(\frac{\mathbb{N}^3}{3} + \mathbb{N}^2\right)$  for obtaining [V], and  $\mathbb{N}^2$  for obtaining  $\{Q\}$  and  $\{\phi\}$ . Because of the large number of zero elements in [M], the corresponding number of multiplication and division processes involved using the five-point differentiation formula is of the order of

 $(4\beta^2$  N+4 $\beta$ N) for [V], and 4 $\beta$ N for {Q} and {\$\phi\$}, where \$\beta\$ is of the order of the submatrix \$\alpha\$. (If the three-point differentiation formula is used, there are  $(\beta^2$  N+4 $\beta$ N) and 2 $\beta$ N operations, respectively, with N necessarily several times larger.) This reduction in the effective order of the matrix is very helpful in reducing rounding-off errors. If the present digital computing machine is designed to handle an ordinary matrix of order of 100 (reference 11), it may therefore be expected to handle the special matrix of the present problems of the order of several hundred, which is sufficient for most fluid-flow problems.

#### Numerical Example

In reference 3, the function  $\,\phi$ , which satisfies the differential equation

$$\frac{\partial^2 \varphi}{\partial r^2} + \frac{1}{r} \frac{\partial \varphi}{\partial r} + \frac{\partial^2 \varphi}{\partial z^2} = 0 \tag{42}$$

and takes the values

$$\varphi = 10,000 J_0 (3r) e^{3z}$$
 (43)

on the boundary of a circle with center at r=1.5, z=0, and radius of 0.5 (fig. 7), is obtained by an improved relaxation method with difference correction. Accurate results were obtained in reference 3 by the inclusion of differences up to the fourth order, even with a relatively coarse network. Because of the curved boundary all around, it was felt that it

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would be more convenient to use the differentiation coefficients obtained herein in order to avoid the extrapolation for both  $\,\phi\,$  and high-order differences near the boundary. In order to compare the results on the same basis, the same network involving 16 interior points and the five-point differentiation formula (corresponding to the inclusion of differences up to the fourth order) are used. The solution is obtained by both relaxation and matrix methods.

Relaxation solution. - Basically, this problem involves only two values of a, (0.1 and 0.18990), differing from the uniform spacing b = 0.2 (fig. 7). The spacing ratio is therefore 0.5 and 0.94950, respectively. The differentiation coefficients for 0.5 can be obtained directly from the coefficient tables, and the coefficients for 0.94950 can be taken, for engineering accuracy, as equal to those for 0.95 given in the coefficient tables. For the present calculation, however, it is better to compute these coefficients more accurately from the formulas so that any difference in the result will not be attributed to this approximation. After the coefficients are obtained, they are combined according to equation (42) and are given in figure 8. The corresponding relaxation pattern is given in figure 9.

It is convenient to obtain the solution in two steps. In the first step only the five or seven larger coefficients of the nine coefficients at each point are used to compute the residual and to improve the  $\phi$  value at each point. After the required change of  $\phi$  at all points is reduced to the order of 10, new residuals are computed and  $\phi$  values are improved using all nine coefficients. The computation is stopped when the required change of  $\phi$  is less than 1.

Matrix solution. - Because of the possible accumulation of roundingoff error in the matrix calculation, the boundary values are computed to five significant figures and the elements of coefficient matrix M are given to five decimal places. Matrix P is given to two decimal places, giving at least six significant numbers. It was originally intended to keep five decimal places in the matrix V calculation also, but it later developed that some elements in u become very small and the computation was extended to seven decimal places, giving a minimum of three significant figures in one place. In spite of this decrease in significant figures, the substitution of the  $\phi$  values obtained into the original equation gives a new [P], [P], which checks with the original {P} to within two on the fifth significant number. The composite matrix V and the column matrices Q,  $\phi$ , and P' are all given in table II. Calculations were also made keeping five significant figures everywhere, which still gave  $\phi$  accurate to within 1.3 percent.

A comparison of solutions obtained by relaxation and matrix solutions using the differentiation formula (16), the relaxation solution with difference correction (reference 3), and the exact values are given in table III. The first two solutions agree very well and can be taken as the values the fourth-degree piece-wise polynomial approximation and the grid size used will give for this problem. Although these values are, in general, accurate enough for engineering purposes. some of them do not agree with the exact value as well as the solution obtained in reference 3. This difference is caused by the fact that in reference 3 the boundary values are obtained by extrapolation based on the approximate interior values and a constant fifth-order difference obtained from them is used in subsequent calculations. Also at points next. to the boundary, the relaxation coefficients seem to be based on a linear variation from those points to the boundary. Because of these variations, the procedure given in reference 3 will not always give more accurate answers than a strictly fourth-degree polynomial approximation as used herein.

#### CONCLUDING REMARKS

General differentiation formulas are obtained in terms of the values of the function at unequally spaced arguments and the corresponding distances between the successive arguments using Lagrangian polynomials of any degree. The remainder term is also obtained. The coefficients in the formulas for the first four derivatives at the given arguments are explicitly given. For the special case where there is only one spacing at either end of the arguments different from the others, as often encountered in many practical problems, the differentiation coefficients are computed for different ratios of this spacing to the others, varying from 0.1 to 1.29 and in intervals of 0.01, and are given in the coefficient tables.

The formulas and the coefficients obtained can be used to obtain the approximate values of the various derivatives at any point within the range of given arguments when the values of the function are given at a number of points unequally spaced. They can also be used in the numerical integration of partial differential equations where the starting value is given on a curve unequally spaced from the regular grid lines, or when the interval must be changed during calculation. In particular, in the numerical solutions of elliptic-type partial differential equations, they can be used to obtain the finite-difference expressions more accurately and conveniently at points near a curved boundary, to enable the use of a gradually increasing grid spacing away from the object if the boundary condition is given at infinity, and to render the solution of these problems practical on large-scale digital machines by either iterative or direct methods.

In most practical problems, use of differentiation formulas based on polynomials of higher degree than second is possible and advantageous to enable the use of a relatively coarse grid over most of the domain of the problem to reduce the amount of work.

Lewis Flight Propulsion Laboratory, National Advisory Committee for Aeronautics, Cleveland, Ohio, July 5, 1950.

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ABLE I - COMPARISON OF 3-, 4-, AND 5-POINT DIFFERENTIATION FORMULA WITH v = 1/1+x2

			TABLE :	COMP	ARISON OF	7 3-, 4-,	AND 5-PO	OINT DIFF	ERENTIATIO	ON FORMULA	A WITH y =	1/1+x <sup>2</sup>	N.	ACA
		-						у¹					-	
×	У							pacing						Exact
-	'		1.000			0.500			0.250			0.125	-	values
-	-					t 4 poin				t 5 point	3 point	4 point	5 point	1
-1.000	0.50000		1.40	1.70	0.700	0.500	0.200	0.520	0.468	0.493	0.50208	0.49741	0.5013	0,50000
875 750 625	.56638							(00	100	6-0	.56000 .61092	.56233	.5610	.56090
625	.7191				1			.600	.626	.618	.61092	.61587	.61456	.61475
500	. 8000C	ol			.500	.600	.700	.602	.628	.636	.64000 .63048	.64792	.6464	64767
375	.8767	3	ĺ							1.000	.56472	.57555	.57591	57692
250	.94118	3			-		1	.400	.442	.433	.43164	.57555 .44325 .24476	.44219	.44248
125 0	.98464	0	200	300	0	100	0	0	0.01		.56472 .43164 .23528	.24476	.24177	.24272
305	ADLCI.		200	300	1	.100	10	0	.024	0	10	,00349		0
.250 .375 .500 .625 .750 .875	.94118	<b>\$</b>						400	424	433	23528 43164	44325	24177	24272
- 375	.87673	s l		1		İ			,	1	56472	57555	57594	57692
.500	.80000				500	600	585	602	628	636	63048	63840	63985	64103
.625	.71911							-			64000	Chian	64643	64767
.875	.56638							600	607	616	61092	61325	61456	61475
1.000	.50000	400	400	500	492	485	523	4995	4975	5019	- 50000	56069	56151 50016	56090
1.167	.44130			"	,-	,	1,703	,,,,	1,4717	,019	- 43904	49963 43820	50016 43843	50000 43860
1.250	. 39024			1				3846	3805	3815	38172	38063	38075	38052
1.375 1.500 1.625	.34595				200	000		-00-	-011		61000 61092 56000 50000 43904 38172 33020 28508	38063 32916	32913	28409
1.625	.27468				300	287	290	2882	2844	2842	28508	28405	28405 24521 21210 18388 16000 13969	28409
1.750	.24615							2154	2125	2121	24010	24529 21215	24521 21210	24528
1.875	.22145							1227.			18460 16060 14020 12284	18393	18388	21212
2.000	.20000	200	200	100	1698	1626	1597	1624	1604	1599	16060	16007	16000	16000
2.125 2.250 2.375 2.500 2.625	.18130										14020	13972	13969	13971 12245
2.375	.15059							1241	1227	1224	12284	12245	12241	12245
2.500	.15059 .13793 .12673				1000	0928	0958	09632	09530	.09509	10808 09544 08456	10769 09512	10773 09515	10771
2.625	.12673					1	,,,	.0,052	0///	,09,09	08456	08432	08431	08432
2.750 2.875	.11679							07586	07484	07505	07520	07500	07498	07501
3.000	.10793	0	0	200	0517	0660	0550	0=016			06716	06696	06698	06698
3.000	.10000	U	1 0	.300	0517	0660	0573	05846	06050	05988	05972	06012	06006	06000
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-1.000	0.50000	-1.00	-2.20	-3.30	-0.400	0.800	3.00	0.320	0.941	0.579	0.46410	0.57505	0.46037	0.50000
875 750	.56638 .64000										.46410	.46311	.47381	.47083
625	.71911							. 320	.320	-353	.35192	. 35117	.36181	.36066
500	.80000				400	400	600	3011	3011	2682	26667	.11386	.12581	.12798
375	.87673				, , , , ,			- + 5011	5011	2002	- 78718	78550	25461 78277	25641 77985
250	.94118							-1.318	-1.318	-1.355	-1.34551	-1.34264	-1.35189	-1.35345
0.125	.98464	1 00	1 00								LACTOR L	-1.79744	-1.82235	-1.82252
.125	.98464	-1.00	~1.00	900	-1.60	-1.60	-1.80	-1.882	-1.882	-1.976	-1.96923	-1.96503	-1.99403	-2.00000
.250	.94118							-1.318	-1.318	3 255	-1.80128	-1.79744	-1.82235	-1.82252
.375	.87673	i						-1.310	-1.310	-1.355	-1.96923 -1.80128 -1.34551 78718 26667	-1.34264 78550	-1.35189 78277	-1.35345 77985
.500	.80000				400	400	369	3011	3011	2682	26667	26610	25461	25641
.625	.71911										.11410	.11386	.12580	.12798
.750	.64000							. 3200	.3200	.3581	.35192 .46410	.35117	.12580 .36181	. 36066
1.000	.50000	.200	.200	.300	.431	.431	.508	.4838	1.000	5015	.46410	.46311	1:6000	.47083
1.125	.44138	*200	.200	. 500	.431	.431	.500	.4030	.4838	.5015	.49744	.49638 .47846	.50091	.50000
1.250	. 39024 . 34595					i		.4354	.4354	.4396	43910	43817	74002A	.48129 .43805
1.375	34595							•			.43910 .38654	.38571	.38571	.38665
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1.750	.24615							.2462	01.60	01.1.	.28718	.28657	.28608	.28699
1.750	.22145	i			l		ļ	.2402	.2462	.2445	24551	24499	.244(5)	.24429
2.000	.20000	.200	.200	.300	.182	.182	.177	.17760	.17760	.17597	.20033	.20789	.20757	.20738
2.125	.18130			-					12,,50		.3654 .33654 .28718 .24551 .20833 .17628 .15064 .12756 .10897	.15032	.17547 .15019 .12699	.14956
2.250	.16495		ļ					.12848	.12848	. 12725	.12756	.15032	.12699	.12735
2.375	.15059		[		.0966	.0966	0007	001.00	001.50		.10897	.10874	.10853	.10873
2.500	.12673		]		.0900	.0900	.0907	.09408	.09408	.09325	.09359	.09339	.09323	.09316
2.750	.11679							.06960	.06960	.06877	.06923	.06908	.08053	.08009
2.875	.10793						ĺ				.05962	.05949	.05936	.05983
3.000	.10000	.200	.200	900	.0966	.0106	.0749	.06960	.04512	.05421	.05962	.04989	.05168	.05200

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-2.63605	37.14286	-112.61347	38.09525	0	0	16.06181	0	. 0	0
1.38890	-11.25000	62.50000	-265.97222	0	0	0	58.33333	0	0
41.66667	0	0	0	-111.04163	12.00307	8.10520	-2.01294	35.00000	0 /
0	33.77655	0	0	35.91529	-125.68808	31.41051	<b>-</b> 1.85290	0	33.47601
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-2.38095	0	0	0	35.00000	0	0	0	-111.04163	12.00307
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0	0	-2.10998	0	0	0	33.47601	0	-2.40380	35.83659
0	0	0	-2.38095	0	0	0	35.00000	-1.45640	4.75186
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-2.63605	36.5946346	-101.4521944	3685555	0281161	0554870	1583190	0	.0048199
1.38890	-10.9611473	59.1363106	-243.9638186	0038496	0065385	0383762	2391065	.0006599
41.66667	8.6655132	1.1917320	.4399293	-101.0958821	1325976	0822067	.0188707	3293410
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0	-1.79032	5416178	1656614	1835777	6.4329809	1.9337838	.4643078	.7306407
0	0	-1.79032	6598323	0528769	1106651	6.4156391	1.8493894	.1994372
0	0	0	1.19048	.0045829	.0083916	.0487252	-9.7003475	0821391

M, P, P', V, Q, AND Q	М,	Ρ,	Р',	ν.	Q.	AND	q
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0	0	1.19048	0	0	0
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0	-10.00000	0	0	0	1.19048
0	0	-2.38095	0	.0	0
Ο.	0	0	-2.10998	0	0
33.47601	0	0	0	-2.10998	0
0	35.00000	0	0	0	-2.38095
8.10520	-2.01294	41.66667	0	0	0
31.41051	<b>-1.8</b> 5290	0	33.77655	0	0
-125.60134	31.33227	0	0	33.77655	0
22.14991	-116.45913	0	0	0	41.66667
0	0	-267.12962	55.55556	-9.16667	1.05820
0	0	44.79167	-113.72955	33.12500	-2.15773
16.06181	0	-2.63605	37.14286	-112.61347	38.09525
0	<b>5</b> 8.33333	1.38890	-11.25000	62.50000	-265.97222

{P}
-10,633.95
16,192.25
12,948.37
210,879.21
-28,623.17
1,465.22
-5,985.97
39,737.87
-60,857.24
-19,234.20
-45,213.27
-10,311.87
<b>-</b> 12,593.27
279,277.63
362,314.27
1,767,582.26

	{P'}
5	-10,633.90
5	16,192.24
7	12,948.81
	210,879.16
7	-28,623.26
	1,465.38
·	-5,986.01
	39,737.77
1	-60,857.31
	~19,234.19
	-45,213.12
	-10,311.84
	-12,593.24
	279,277.65
	362,314.29
	1,767,582.19

0	0	0	-0.0044566	0	0	0
0647792	0	0	0019118		-	0
0233664	0666704	0	0005738	.0061848	.0176469	0
0027535	0161608	.0409897	0000786	.0007288	.0042776	0048797
0058400	0008562	.0001784	.0215436	.0015458	.0002266	0000212
3151405	0066747	.0011783	.0067811	.0245499	.0017667	0001403
1173240	3351118	.0051345	.0018929	.0105503	.0261707	0006113
0465208	0926545	3359990	.0005004	.0041868	.0085683	.0219044
1425472	0973574	.0186346	4129549	.0020374	.0013189	.0000935
-108.4001334	3614651	.0164546	1493731	3026124	.0036258	.0004802
39.9112882	-99.4336322	3416497	0539286	1177253	3290843	.0022621
6.1634932	27.3809686	-95.5275121	0199028	0518187	0911553	4274860
7.2470032	7.5376636	1.3861196	-242.7113753	2416465	.0272843	0067061
18.3115734	7.3 <b>85175</b> 9	2.3535394	48.2264553	-95.6904192	3587721	.0090153
.7883387	18.5566855	6.9388359	-1.3093557	39.5476886	-91.8021580	4424078
4513107	-1.0342833	54.6805588	2.3247851	- 8.0738959	64.2624144	-213.8575898

{Q}	{φ}
39.8082	-165.778
-138,0002	-973.204
-178.4462	-1526.881
-901.2153	-1592.452
281.6818	-299.186
2.8409	-1778.430
-106.9779	-2789.769
-814.0599	-2904.401
703.5440	-549.735
411.1965	-3247.006
502.6303	-5089.370
6088	-5294.207
228.7089	-1014.156
-2681.7607	-5923.307
-5012.7002	-9277.338
-9639.6072	-9639.607

TABLE III - COMPARISON OF RESULTS

		φ		NACA
At	Relaxation	Relaxation	Matrix	Exact
	solution with	solution with	solution with	value
	difference	fourth-degree	fourth-degree	
	correction	differentiation	differentiation	
	(reference 3)	formula (16)	formula (16)	
1	<b>-</b> 169	<del>-</del> 165	<b>-</b> 166	-168
2	<b>-</b> 981	-972	<b>-</b> 973	<b>-</b> 978
3	-1536	-1526	-1527	-1531
4	-1596	-1593	-1592	-1593
5	<b>-</b> 307	<b>-</b> 298	-299	-305
6	-1783	-1777	-1778	-1781
7 8	<b>-27</b> 91	-2790	-2790	-2790
8	-2901	-2905	-2904	-2902
9	<b>-</b> 560	<b>-5</b> 49	-550	-556
10	-3248	-3247	-3247	-3245
11	-5083	<b>-5</b> 090	<b>-</b> 50 <b>8</b> 9	<b>-</b> 5083
12	<b>-</b> 5283	-5295	-5294	-5288
13	-1019	-1014	-1014	-1014
14	<b>-</b> 5918	<b>-5</b> 9 <b>2</b> 3	-5923	-5914
15	-9264	-9278	-9277	-9262
16	-9628	-9640	-9640	-9636

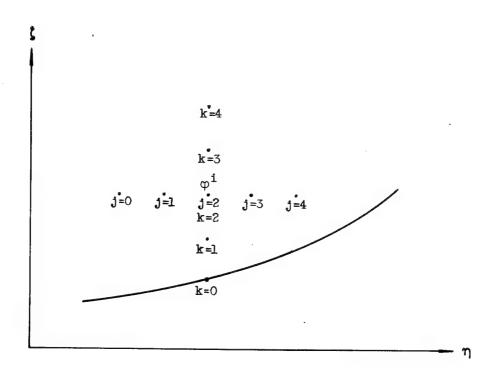


Figure 1. - Notation i, j, and k.

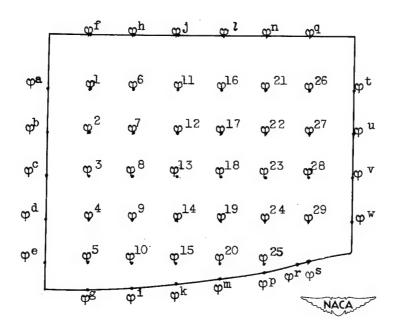
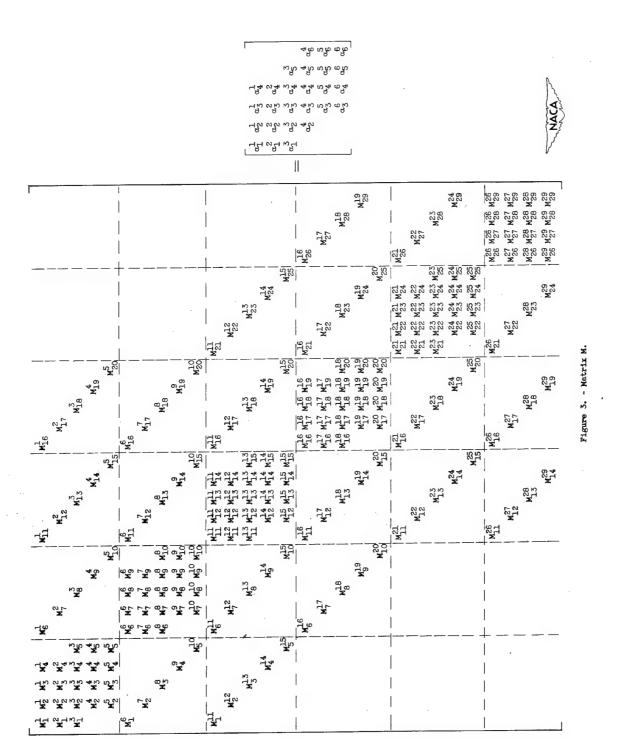
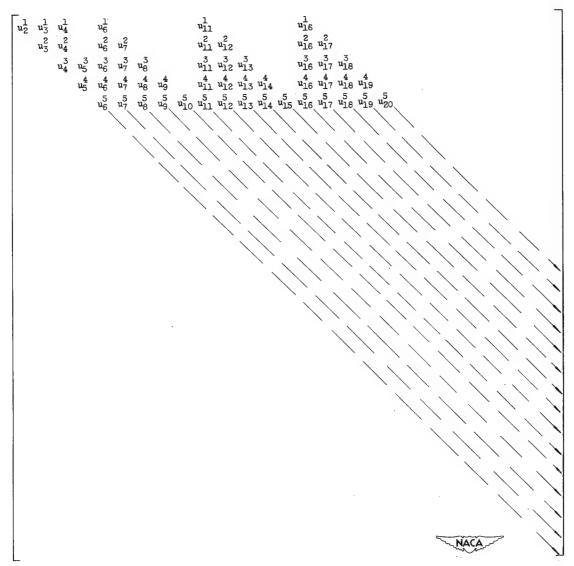


Figure 2. - Numbering system.



```
NACA
          (a) [L]
```

Figure 4. - Matrices L and u.



(b) [u]

Figure 4. - Concluded. Matrices L and u.

NACA

6

 $\begin{bmatrix} L_{1}^{1} & u_{2}^{1} & u_{3}^{1} & u_{4}^{1} \\ L_{1}^{2} & & & \\ L_{1}^{3} & & & \\ \end{bmatrix}$ 

L<sub>2</sub> L<sub>2</sub> L<sub>2</sub> L<sub>2</sub>

r<sub>e</sub> r<sub>e</sub>

 $L_1^{11} L_2^{11} L_3^{11} L_4^{11} L_5^{11}$ 

, , , ,

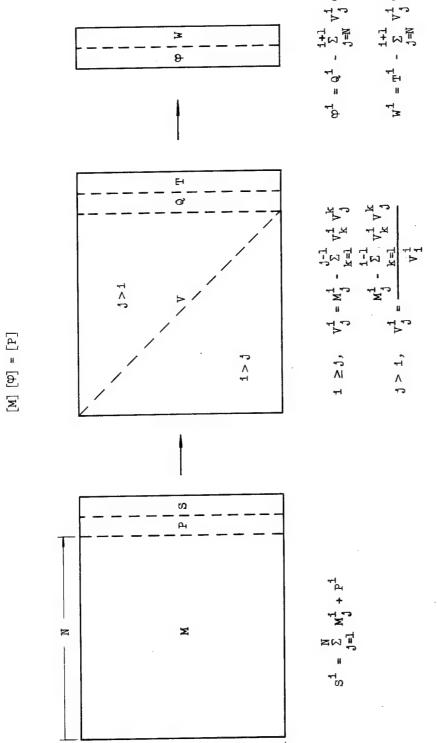
L<sup>26</sup> L<sup>26</sup> L<sup>26</sup> L<sup>26</sup> L<sup>26</sup> L<sup>26</sup> L<sup>26</sup>

[V] = [L] + [u] - [I]

ul6 ul6 ul6 ul6 ul6 ul6 ul6

u<sub>16</sub>

Figure 5. - Matrix V.



For checking:  $T^1 = 1 + \sum_{j=1+1}^{N+1} v_j^1$ 



Figure 6. - Operation diagram and operating formulas.

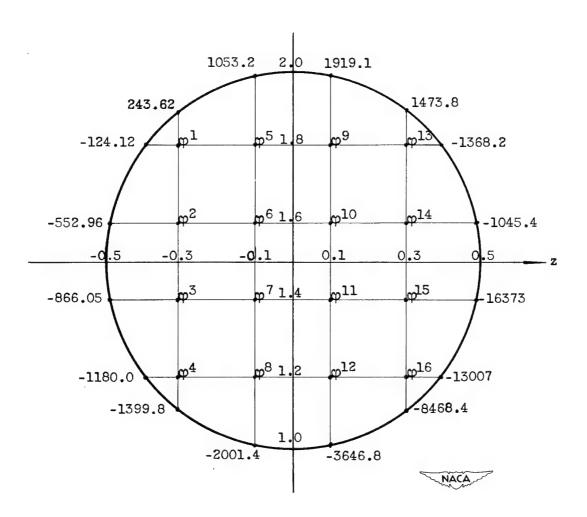


Figure 7. - Boundary values and order in which  $\boldsymbol{\phi}$  is numbered.



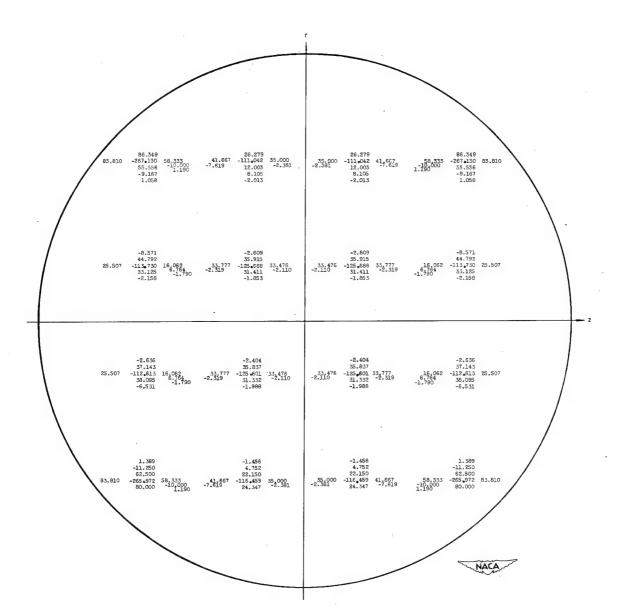


Figure 8. - Coefficients used to compute residuals.

Figure 9 - Improvement ----

(D <sup>t</sup> y) <sub>x=x</sub> ,•	$\sum_{j=0}^{2} {}_{2}^{1}B_{j}^{1} y_{j} + {}_{2}^{1}R^{1}$	(i=0,2)	NACA
	i *0 * J		and an

	(U'y) <sub>X=</sub>	=x ; Z 2 <sup>B</sup> j 3	′j * 2 <sup>K</sup> '	, I=U, Z)	NACA
$r = \frac{x_1 - x_0}{x_2 - x_1} = \frac{a}{b}$	2B <sub>0</sub> b	18° b	180 b	$\frac{{}_{2}^{1}E^{0}}{{b}^{2}f^{(3)}(\underline{z})}$	
0.10 .11 .12 .13	-10.90909091 - 9.99180999 - 9.22619048 - 8.57726344 - 8.02005012	11,00000000 10,09090909 9,33333333 8,69230769 8,14285714	-0.090909091 099099099 107142857 115044248 122807018	0.01.83 .0204 .0224 .0248 .0266	0.10 .11 .12 .13 .14
.15 .16 .17 .18 .19	- 7.53623188 - 7.11206896 - 6.73705380 - 6.40301318 - 6.10349403	7.66666667 7.25000000 6.88235294 6.55555556 6.26315789	130434783 137931034 145299145 152542373 159663866	.0288 .0309 .0332 .0354 .0377	.15 .16 .17 .18
.20	- 5.83333333	6.00000000	166666667	.0400	.20
.21	- 5.58835104	5.76190476	173553719	.0424	.21
.22	- 5.36512668	5.54545455	180327869	.0447	.22
.23	- 5.16083422	5.34782609	186991870	.0472	.23
.24	- 4.97311828	5.166666667	193548387	.0496	.24
.25	- 4.8000000	5.00000000	200000000	.0521	.25
.26	- 4.63980464	4.84615385	206349206	.0546	.26
.27	- 4.49110528	4.70370370	212598425	.0572	.27
.28	- 4.35267857	4.57142857	218750000	.0597	.28
.29	- 4.22346966	4.44827586	224806202	.0624	.29
.30 .31 .32 .33	- 4.10256410 - 3.98916523 - 3.88257576 - 3.78218273 - 3.68744513	4.33333333 4.22580645 4.12500000 4.03030303 3.94117647	230769231 236641221 242424242 248120301 253731343	.0650 .0677 .0704 .0732 .0759	.30 .31 .32 .33 .34
.35	- 3.59788360	3.85714286	259259259	.0788	.35
.36	- 3.51307190	3.77777778	264705882	.0816	.36
.37	- 3.43262971	3.70270270	270072993	.0845	.37
.38	- 3.35621663	3.63157895	275362319	.0874	.38
.39	- 3.28352702	3.56410256	280575540	.0904	.39
.40	- 3.21428571	3.50000000	285714286	.0933	.40
.41	- 3.14824425	3.43902439	290780142	.0964	.41
.42	- 3.08517773	3.38095238	295774648	.0994	.42
.43	- 3.02488209	3.32558140	300699301	.1025	.43
.44	- 2.96717172	3.27272727	305555556	.1056	.44
.45 .46 .47 .48	- 2.91187739 - 2.85884455 - 2.80793168 - 2.75900901 - 2.71195727	3.2222222 3.17391304 3.12765957 3.08333333 3.04081633	310344828 315068493 319727891 324324324 328859060	.1088 .1119 .1152 .1184 .1217	.45 .46 .47 .48 .49
.50	- 2.66666667	3.00000000	333333333	.1250	.50
.51	- 2.62303597	2.96078431	337748344	.1284	.51
.52	- 2.58097166	2.92307692	342105263	.1317	.52
.53	- 2.54038722	2.88679245	346405229	.1352	.53
.54	- 2.50120250	2.85185185	350649351	.1386	.54
•55	- 2.46334311	2.81818182	354838710	.1421	•55
•56	- 2.42673993	2.78571429	358974359	.1456	•56
•57	- 2.39132864	2.75438596	363057325	.1492	•57
•58	- 2.35704932	2.72413793	367088608	.1527	•58
•59	- 2.32384607	2.69491525	371069182	.1564	•59
.60	- 2.29166667	2.66666667	375000000	.1600	.60
.61	- 2.26046227	2.63934426	378881988	.1637	.61
.62	- 2.23018718	2.61290323	382716049	.1674	.62
.63	- 2.20079852	2.58730159	386503067	.1712	.63
.64	- 2.17225610	2.56250000	390243902	.1749	.64
.65	- 2.14452214	2.53846154	393939394	.1788	.65
.66	- 2.11756115	2.51515152	397590361	.1826	.66
.67	- 2.09133971	2.49253731	401197605	.1865	.67
.68	- 2.06582633	2.47058824	404761905	.1904	.68
.69	- 2.04099134	2.44927536	408284024	.1944	.69
	- 182 a	- 182 a	- 182 a	$\frac{{}_{2}^{1}E^{2}}{a^{2}f^{(3)}(E)}$	$\rho = \frac{x_2 - x_1}{x_1 - x_0} = \frac{b}{a}$

(D <sup>1</sup> y) <sub>x-x;</sub>	$=\sum_{j=0}^{2}$	12Bj	у <sub>ј</sub>	+	12R <sup>1</sup>	
------------------------------------	-------------------	------	----------------	---	------------------	--

(i-0,2)

NACA	
and man	

	(0)	x-x; = 20j	y <sub>j</sub> + 2 <sup>R</sup> (	I= U, Z)	NACA
$=\frac{x_1-x_0}{x_2-x_1}=\frac{a}{b}$	<sup>1</sup> <sub>2</sub> B <sub>0</sub> b	<sup>1</sup> <sub>2</sub> B <sup>0</sup> <sub>1</sub> b	2B2 b	b <sup>2</sup> f <sup>(3)</sup> (ξ)	
0.70	- 2.01680672	2.42857143	-0.411764706	0.1983	0.70
.71	- 1.99324603	2.40845070	415204678	.2024	.71
.72	- 1.97028424	2.38888889	418604651	.2064	.72
.73	- 1.94789770	2.36986301	421965318	.2105	.73
.74	- 1.92606400	2.35135135	425287356	.2146	.74
.75 .76 .77 .78 .79	- 1.90476190 - 1.88397129 - 1.86367305 - 1.84384903 - 1.82448200	2.33333333 2.31578947 2.29870130 2.28205128 2.26582278	428571429 431818182 435028249 438202247 441340782	.2188 .2229 .2272 .2314 .2357	.75 .76 .77 .78
.80 .81 .82 .83 .84	- 1.80555556 - 1.78705409 - 1.76896274 - 1.75126736 - 1.73395445	2.25000000 2.23456790 2.21951220 2.20481928 2.19047619	4447513812 450549451 453551913 456521739	.2400 .2444 .2487 .2532 .2576	.80 .81 .82 .83 .84
.85 .86 .87 .88 .89	- 1.71701113 - 1.70042511 - 1.68418465 - 1.66827853 - 1.65269603	2.17647059 2.16279070 2.14942529 2.13636364 2.12359551	459459459 462365591 465240642 468085106 470899471	.2621 .2666 .2712 .2757 .2804	.85 .86 .87 .88
.90	- 1.63742690	2.1111111	473684211	.2850	.90
.91	- 1.62246131	2.09890110	476439791	.2896	.91
.92	- 1.60778986	2.08695652	479166667	.2944	.92
.93	- 1.59340353	2.07526882	481865285	.2992	.93
.94	- 1.57929370	2.06382979	484536082	.3039	.94
•95	- 1.56545209	2.05263158	487179487	.3088	.95
•96	- 1.55187075	2.04166667	489795918	.3136	.96
•97	- 1.53854205	2.03092784	492385787	.3185	.97
•98	- 1.52545867	2.02040816	494949495	.3234	.98
•99	- 1.51261357	2.01010101	497487437	.3284	.99
1.00	- 1.50000000	2.00000000	500000000	.3333	1.00
1.01	- 1.48761145	1.99009901	502487562	.3384	1.01
1.02	- 1.47544166	1.98039216	504950495	.3434	1.02
1.03	- 1.46348462	1.97087379	507389163	.3485	1.03
1.04	- 1.45173454	1.96153846	509803922	.3536	1.04
1.05	- 1.44018583	1.95238095	512195122	.3588	1.05
1.06	- 1.42883912	1.94339623	514563107	.3639	1.06
1.07	- 1.41767123	1.93457944	516908213	.3692	1.07
1.08	- 1.40669516	1.92592593	519230769	.3744	1.08
1.09	- 1.39590009	1.91743119	521531100	.3797	1.09
1.10	- 1.38528139	1.90909091	523809524	.3850	1.10
1.11	- 1.37483455	1.90090090	526066351	.3904	1.11
1.12	- 1.36455526	1.89285714	528301887	.3957	1.12
1.13	- 1.35443932	1.88495575	530516432	.4012	1.13
1.14	- 1.34448270	1.87719298	532710280	.4066	1.14
1.15	- 1.33468150	1.86956522	534883721	.4121	1.15
1.16	- 1.32503193	1.86206897	537037037	.4176	1.16
1.17	- 1.31553035	1.85470085	539170507	.4232	1.17
1.18	- 1.30617322	1.84745763	541284404	.4287	1.18
1.19	- 1.29695714	1.84033613	543378995	.4344	1.19
1.20	- 1.28787879	1.83333333	545454545	.4400	1.20
1.21	- 1.27893497	1.82644628	547511312	.4457	1.21
1.22	- 1.27012258	1.81967213	549549549	.4514	1.22
1.23	- 1.26143862	1.81300813	551569507	.4572	1.23
1.24	- 1.25288018	1.80645161	553571429	.4629	1.24
1.25	- 1.2444444	1.80000000	55555556	.4688	1.25
1.26	- 1.23612867	1.79365079	557522124	.4746	1.26
1.27	- 1.22793021	1.78740157	559471366	.4805	1.27
1.28	- 1.21984649	1.78125000	561403509	.4864	1.28
1.29	- 1.21187502	1.77519380	563318777	.4924	1.29
	- <sup>1</sup> <sub>2</sub> B <sub>2</sub> <sup>2</sup> a	- <sup>1</sup> <sub>2</sub> B <sub>1</sub> <sup>2</sup> a	- ½B <sub>0</sub> <sup>2</sup> a	$\frac{{}_{2}^{1}E^{2}}{a^{2}f^{(3)}(\xi)}$	$p = \frac{x_2^{-x_1}}{x_1 - x_0} =$

$$(D^{\dagger}y)_{X=X_{1}} = \sum_{j=0}^{2} {}_{2}^{i}B_{j}^{i} y_{j} + {}_{2}^{i}R^{i}$$



		J	-0		
$r = \frac{x_1 - x_0}{x_2 - x_1} = \frac{a}{b}$	<sup>1</sup> <sub>2</sub> B <sub>0</sub> b	281 b	<sup>1</sup> <sub>2</sub> B <sub>2</sub> <sup>1</sup> b	$\frac{\frac{1}{2^{E}}}{b^{2}f^{(3)}(\xi)}$	
0.10 .11 .12 .13	-9.09090909 -8.19000819 -7.44047619 -6.80735194 -6.26566416	9.00000000 8.09090909 7.3333333 6.69230769 6.14285714	0.090909091 .099099099 .107142857 .115044248 .122807018	-0.0167 0183 0200 0217 0233	0.10 .11 .12 .13
.15 .16 .17 .18	-5.79710145 -5.38793103 -5.02765209 -4.70809793 -4.42282176	5.66666666 5.25000000 4.88235294 4.55555556 4.26315789	.130434783 .137931034 .145299145 .152542373 .159663866	0250 0267 0283 0300 0317	.15 .16 .17 .18
.20 .21 .22 .23 .24	-4.16666667 -3.93545848 -3.72578241 -3.53481796 -3.36021505	4.00000000 3.76190476 3.54545454 3.34782609 3.16666667	.166666667 .173553719 .180327869 .186991870 .193548387	0333 0350 0367 0383 0400	.20 .21 .22 .23 .24
.25 .26 .27 .28	-3.20000000 -3.05250305 -2.91630213 -2.79017857 -2.67308206	3.00000000 2.84615385 2.70370370 2.57142857 2.44827586	.20000000 .206349206 .212598425 .218750000 .224806202	0417 0433 0450 0467 0483	.25 .26 .27 .28 .29
.30 .31 .32 .33	-2.56410256 -2.46244767 -2.36742424 -2.27842333 -2.19490781	2.33333333 2.22580645 2.12500000 2.03030303 1.94117647	.230769231 .236641221 .242424242 .248120301 .253731343	0500 0517 0533 0550 0567	.30 .31 .32 .33
.35 .36 .37 .38 .39	-2.11640212 -2.04248366 -1.97277570 -1.90694127 -1.84467810	1.85714286 1.77777778 1.70270270 1.63157895 1.56410256	.259259259 .264705882 .270072993 .275362319 .280575540	0583 0600 0617 0633 0650	•35 •36 •37 •38 •39
.40 .41 .42 .43 .44	-1.78571429 -1.72980453 -1.67672703 -1.62628070 -1.57828283	1.50000000 1.43902439 1.38095238 1.32558140 1.27272727	.285714286 .290780142 .295774648 .300699301 .305555556	0667 0683 0700 0717 0733	.40 :41 .42 .43
.45 .46 .47 .48 .49	-1.53256705 -1.48898154 -1.44738747 -1.40765766 -1.36967539	1.22222222 1.17391304 1.12765957 1.08333333 1.04081633	.310344828 .315068493 .319727891 .324324324 .328859060	0750 0767 0783 0800 0817	.45 .46 .47 .48 .49
.50 .51 .52 .53 .54	-1.33333333 -1.29853266 -1.26518219 -1.23319768 -1.20250120	1.00000000 .960784314 .923076923 .886792453 .851851852	.33333333 .337748344 .342105263 .346405229 .350649351	0833 0850 0867 0883 0900	.50 .51 .52 .53 .54
•55 •56 •57 •58 •59	-1.17302053 -1.14468864 -1.11744329 -1.09122654 -1.06598444	.818181818 .785714286 .754385965 .724137931 .694915254	.354838710 .358974359 .363057325 .367088608 .371069182	0917 0933 0950 0967 0983	.55 .56 .57 .58 .59
.60 .61 .62 .63 .64	-1.04166667 -1.01822625 -0.995619275 973804655 952743902	.66666667 .639344262 .612903226 .587301587 .562500000	.375000000 .378881988 .382716049 .386503067 .390243902	1000 1017 1033 1050 1067	.60 .61 .62 .63 .64
.65 .66 .67 .68 .69	932400932 912741877 893734918 875350140 857559386	.538461538 .515151515 .492537313 .470588235 .449275362	.393939394 .397590361 .401197605 .404761905 .408284024	1083 1100 1117 1133 1150	.65 .66 .67 .68 .69
	- 2B2 a	- ½B <sub>1</sub> a	- ½80 a	$\frac{{}_{2}^{1}E^{1}}{a^{2}f^{(3)}(\xi)}$	$p = \frac{x_2 - x_1}{x_1 - x_0} = \frac{b}{a}$

	$(D^{\dagger}y)_{x-x_1} = \sum_{j=0}^{2}$	${}_{2}^{1}B_{j}^{1}y_{j} + {}_{2}^{1}R^{1}$		NACA
1.1	1-1	1-1	1 <sub>2</sub> E1	

		· 'j=(	,		and my
$r = \frac{x_1 - x_0}{x_2 - x_1} = \frac{a}{b}$	<sup>1</sup> <sub>2</sub> B <sub>0</sub> b	<sup>1</sup> 8 b	181 b	$\frac{{}_{2}^{1}E^{1}}{b^{2}f^{(3)}(\xi)}$	
0.70	-0.840336134	0.428571429	0.411764706	-0.1167	0.70
.71	823655383	.408450704	.415204678	1183	.71
.72	807493540	.388888889	.418604651	1200	.72
.73	791828332	.369863014	.421965318	1217	.73
.74	776638708	.351351351	.425287356	1233	.74
.75	761904762	.333333333	.428571429	1250	.75
.76	747607656	.315789474	.431818182	1267	.76
.77	733729547	.298701299	.435028249	1283	.77
.78	720253529	.282051282	.438202247	1300	.78
.79	707163567	.265822785	.441340782	1317	.79
.80	694444444	.250000000	.44444444	1333	.80
.81	682081713	.234567901	.447513812	1350	.81
.82	670061646	.219512195	.450549451	1367	.82
.83	658371190	.204819277	.453551913	1383	.83
.84	646997930	.190476190	.456521739	1400	.84
.85	635930048	.176470588	.459459459	1417	.85
.86	625156289	.162790698	.462365591	1433	.86
.87	614665929	.149425287	.465240642	1450	.87
.88	604448743	.136363636	.468085106	1467	.88
.89	594494977	.123595506	.470899471	1483	.89
.90	584795322	.11111111	.473684211	1500	.90
.91	575340889	.0989010989	.476439791	1517	.91
.92	566123188	.0869565217	.479166667	1533	.92
.93	557134102	.0752688172	.481865285	1550	.93
.94	548365876	.0638297872	.484536082	1567	.94
.95	539811066	.0526315789	.487179487	1583	• •95
.96	531462585	.0416666667	.489795918	1600	•96
.97	523313622	.0309278351	.492385787	1617	•97
.98	515357658	.0204081633	.494949495	1633	•98
.99	507588447	.0101010101	.497487437	1650	•99
1.00	500000000	.0000000000	.500000000	1667	1.00
1.01	492586572	0099009901	.502487562	1683	1.01
1.02	485342652	0196078431	.504950495	1700	1.02
1.03	478262949	0291262136	.507389163	1717	1.03
1.04	471342383	0384615385	.509803922	1733	1.04
1.05 <sup>-</sup> 1.06 1.07 1.08 1.09	464576074 457959333 451487652 445156695 438962293	0476190476 0566037736 0654205607 0740740741 0825688073	.512195122 .514563107 .516908213 .519230769 .521531100	1750 1767 1783 1800	1.05 1.06 1.07 1.08 1.09
1.10	432900433	090909090909	.523809524	1833	1.10
1.11	426967252	0990990991	.526066351	1850	1.11
1.12	421159030	107142857	.528301887	1867	1.12
1.13	415472184	115044248	.530516432	1883	1.13
1.14	409903263	122807018	.532710280	1900	1.14
1.15	404448938	130434783	.534883721	1917	1.15
1.16	399106003	137931034	.537037037	1933	1.16
1.17	393871362	145299145	.539170507	1950	1.17
1.18	388742031	152542373	.541284404	1967	1.18
1.19	383715130	159663866	.543378995	1983	1.19
1.20	378787879	166666666	.545454545	2000	1.20
1.21	373957593	173553719	.547511312	2017	1.21
1.22	369221681	180327869	.549549549	2033	1.22
1.23	364577637	186991870	.551569507	2050	1.23
1.24	360023041	193548387	.553571429	2067	1.24
1.25	355555556	200000000	•55555556	2083	1.25
1.26	351172918	206349206	•557522124	2100	1.26
1.27	346872940	212598425	•559471366	2117	1.27
1.28	342653509	218750000	•561403509	2133	1.28
1.29	338512576	224806202	•563318777	2150	1.29
	- ½B <sub>2</sub> a	- ½B1 a	- ½B <sub>0</sub> a	$\frac{{}_{2}^{!}E^{!}}{a^{2}f^{(3)}(\xi)}$	$p = \frac{x_2 - x_1}{x_1 - x_0} = \frac{b}{a}$

$(D^{\dagger}y)_{x-x_{i}} = \sum_{j=0}^{2} {}_{2}^{\dagger}B_{j}^{i}y_{j} + {}_{2}^{\dagger}R^{i}$	(i=2,0)	NACA
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xx.		, j*0			www
$=\frac{x_1-x_0}{x_1-x_0}=\frac{a}{b}$	<sup>1</sup> <sub>2</sub> B <sub>0</sub> <sup>2</sup> b	182 b	182 b	1E2	
$=\frac{x_1 + x_0}{x_2 - x_1} = \frac{a}{b}$	200 0	20, 0	202 0	b <sup>2</sup> f <sup>(3)</sup> (E)	
0.10	9.09090909	-11,00000000	1.90909091	0.1833	0.10
.11	8,19000819	-10.09090909	1.90090090	.1850	.11
.12	7.44047619	- 9.33333333	1.89285714	,1867	.12
		- 8.69230769			
.13	6.80735194		1.88495575	.1883	.13
.14	6.26566416	- 8.14285714	1.87719298	.1900	.14
.15	5.79710145	- 7.66666667	1.86956522	.1917	.15
.16	5,38793103	- 7.25000000	1.86206897	.1933	.16
.17	5.02765209	- 6,88235294	1.85470085	.1950	.17
.18	4:70809793	- 6.5555556	1.84745763	.1967	.18
.19	4.42282176	- 6.26315789	1.84033613	. 1983	.19
.20	4.16666667	- 6.00000000	1.83333333	.2000	.20
.21	3.93545848	- 5.76190476	1.82644628	2017	.21
.22	3.72578241	- 5.54545455	1.81967213	,2033	.22
.23	3.53481796	- 5.34782609	1.81300813	.2050	.23
.24	3.38021505	- 5.16666667	1.80645161	.2067	.24
.25	3.20000000	- 5.00000000	1.80000000	.2083	.25
.26	3.05250305	- 4.84615385	1.79365079	.2100	.26
.27	2.91630213	- 4.70370370	1.78740157	.2117	.27
.28 ·	2.79017857	- 4.57142857	1.78125000	.2133	.28
.29	2.67308206	- 4.44827586	1.77519380	.2150	.29
.30	2.56410256	- 4.33333333	1.76923077	.2167	.30
.31	2.46244767	- 4.22580645	1.76335878	.2183	.31
.32	2.36742424	- 4.12500000	1.75757576	.2200	.32
.33	2,27842333	- 4.03030303	1.75187970	.2217	.33
.34	2.19490781	- 3.94117647	1.74626866	.2233	.34
.35	2.11640212	~ 3,85714286	1.74074074	.2250	.35
	2.04248366	- 3.77777778	1.73529412	,2267	.36
.36				.2283	
.37	1.97277570	- 3.70270270	1.72992701		.37
.38	1.90694127	- 3.63157895	1.72463768	.2300	.38
.39	1.84467810	- 3.56410256	1.71942446	.2317	.39
.40	1.78571429	- 3.50000000	1.71428571	.2333	.40
.41	1.72980453	- 3.43902439	1.70921986	.2350	.41
.42	1.67672703	- 3,38095238	1.70422535	.2367	.42
.43	1.62628070	- 3.32558140	1.69930070	.2383	.43
:44	1.57828283	- 3,27272727	1.69444444	.2400	.44
.45	1.53256705	- 3,2222222	1.68965517	.2417	.45
.46	1.48898154	- 3,17391304	1.68493151	.2433	.46
	1.44738747	- 3.12765957	1.68027211	.2450	.47
.47					.48
.48 .49	1.40765766 1.36967539	- 3.08333333 - 3.04081633	1.67567568	.2467	.49
	2,000				
.50	1.33333333	- 3,00000000	1.66666667	.2500	.50
.51	1.29853266	- 2.96078431	1.66225166	.2517	.51
.52	1.26518219	- 2.92307692	1.65789474	.2533	.52
.53	1.23319768	- 2.88679245	1.65359477	.2550	.53
. 54	1.20250120	- 2.85185185	1.64935065	.2567	.54
.55	1.17302053	- 2.81818182	1.64516129	.2583	.55
.56	1.14468864	- 2.78571429	1.64102564	.2600	.56
.57	1.11744329	- 2.75438596	1.63694268	.2617	.57
.58	1.09122654	- 2.72413793	1.63291139	.2633	.58
.59	1.06598444	- 2.69491525	1,62893082	.2650	.59
	1.04166667	- 2.66666667	1.62500000	.2667	.60
.60	1.01822625	- 2.63934426	1.62111801	.2683	.61
.60 .61			1,61728395	.2700	.62
.60 .61 .62	0.995619275	- 2.61290323			
.61 .62		- 2.61290323 - 2.58730159	1.61349693	.2717	.63
.61	0.995619275				
.61 .62 .63 .64	0.995619275 .973804655 .952743902	- 2.58730159 - 2.56250000	1.61349693 1.60975610	.2717 .2733	.63 .64
.61 .62 .63 .64	0.995619275 .973804655 .952743902 .932400932	- 2.58730159 - 2.56250000 - 2.53846154	1.61349693 1.60975610 1.60606061	.2717 .2733	.63 .64
.61 .62 .63 .64	0.995619275 .973804655 .952743902 .932400932 .912741877	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152	1.61349693 1.60975610 1.60606061 1.60240964	.2717 .2733 .2750 .2767	.63 .64
.61 .62 .63 .64 .65 .66	0.995619275 .973804655 .952745902 .932400932 .912741877 .893734918	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152 - 2.49253731	1.61349693 1.60975610 1.60606061 1.60240964 1.59880240	.2717 .2733 .2750 .2767 .2783	.63 .64 .65 .66
.61 .62 .63 .64 .65 .66 .67	0.995619275 .973804655 .952743902 .932400932 .912741877 .893734918 .875350140	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152 - 2.49253731 - 2.47058824	1.61349693 1.60975610 1.60606061 1.60240964 1.59880240 1.59523810	.2717 .2733 .2750 .2767 .2783 .2800	.63 .64 .65 .66 .67
.61 .62 .63 .64 .65 .66	0.995619275 .973804655 .952745902 .932400932 .912741877 .893734918	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152 - 2.49253731	1.61349693 1.60975610 1.60606061 1.60240964 1.59880240	.2717 .2733 .2750 .2767 .2783	.63 .64 .65 .66
.61 .62 .63 .64 .65 .66 .67	0.995619275 .973804655 .952743902 .932400932 .912741877 .893734918 .875350140 .857559386	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152 - 2.49253731 - 2.47058824 - 2.44927536	1.61349693 1.60975610 1.60606061 1.60240964 1.59880240 1.59523810 1.59171598	.2717 .2733 .2750 .2767 .2783 .2800 .2817	.63 .64 .65 .66 .67 .68 .69
.61 .62 .63 .64 .65 .66 .67	0.995619275 .973804655 .952743902 .932400932 .912741877 .893734918 .875350140	- 2.58730159 - 2.56250000 - 2.53846154 - 2.51515152 - 2.49253731 - 2.47058824	1.61349693 1.60975610 1.60606061 1.60240964 1.59880240 1.59523810	.2717 .2733 .2750 .2767 .2783 .2800	.63 .64 .65 .66 .67

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$(D^{\dagger}y)_{X-X_{1}} = \sum_{i=0}^{2} {}_{2}^{\dagger}B_{j}^{i}y_{j} + {}_{2}^{\dagger}R^{i}$	(i-2,0)	NACA
$(D, \lambda)^{x-x} = \sum_{j=0}^{n} 2^{p_j} \lambda^{j} + 2^{p_j}$	(i-2,0)	NACA

	$\frac{{}_{2}^{1}E^{2}}{b^{2}f^{(3)}(\xi)}$	182 b	1282 b	<sup>1</sup> <sub>2</sub> B <sub>0</sub> <sup>2</sup> b	$= \frac{x_1 - x_0}{x_2 - x_1} = \frac{a}{b}$
			0 400000	0.840336134	0,70
0.70	0.2833	1.58823529	- 2.42857143		.71
.71	.2850	1.58479532	- 2.40845070	.823655383 .807493540	.72
.72	.2867	1.58139535	- 2.38888899	.791828332	.73
.73 .74	.2883	1.57803468	- 2.36986301 - 2.35135135	.776638708	.74
		1.57142857	- 2.33333333	.761904762	.75
.75 .76	,2917 ,2933	1.56818182	- 2.31578947	.747607656	.76
	.2950	1.56497175	- 2.29870130	.733729547	.77
.77	.2967	1.56179775	- 2.28205128	.720253529	.78
.78 .79	.2983	1.55865922	- 2.26582278	.707163567	.79
.80	.3000	1.55555556	- 2.25000000	.69444444	.80
.81	.3017	1.55248619	- 2,23456790	.682081713	.81
.82	.3033	1.54945055	- 2.21951220	.670061646	.82
. 83	.3050	1.54644809	- 2.20481928	.658371190	.83
. 84	.3067	1.54347826	- 2.19047619	.646997930	.84
.85	.3083	1.54054054	- 2.17647059	.635930048	.85
.86	.3100	1,53763441	- 2.16279070	.625156289	.86
.87	.3117	1.53475936	- 2.14942529	.614665929	.87
.88	.3133	1.53191489	- 2.13636364	.604448743	.88
.89	.3150	1.52910053	- 2.12359551	.594494977	.89
.90	,3167	1.52631579	- 2.11111111	.584795322	.90
.91	.3183	1.52356021	- 2.0 <b>98</b> 90110	.575340889	.91
.92	.3200	1.52083333.	- 2.08695652	.566123188	, 92
.93	.3217	1.51813472	- 2.07526882	.557134102	.93
.94	.3233	1.51546392	- 2.06382979	.548365876	.94
.95	.3250	1.51282051	- 2.05263158	.539811066	.95
.96	.3267	1.51020408	- 2.04166667	.531462585	.96
. 97	.3283	1.50761421	- 2.03092784	.523313622	.97
.98	.3300	1.50505051	- 2.02040816	.515357658	.98
.99	.3317	1.50251256	- 2.01010101	.507588447	.99
1.00	.3333	1.50000000	- 2.00000000	.500000000	1.00
1.01	.3350	1.49751244	- 1.99009901	.492586572	1.01
1.02	.3367	1.49504950	- 1.98039216	.485342652	1.02
1.03	.3383	1.49261084	- 1.97087379	.478262949	1.03
1.04	.3400	1.49019608	- 1.96153846	.471342383	1.04
1.05	.3417	1.48780488	- 1.95238095	.464576074	1.05
1.06	.3433	1.48543689	- 1.94339623	.457959333	1.06
1.07	.3450	1.48309179	- 1.93457944	.451487652	1.07
1.08	.3467 .3483	1.48076923 1.47846890	- 1.92592593 - 1.91743119	.445156695 .438962293	1.08
1.09	.0403				
1.10	.3500	1.47619048	- 1.90909091	432900433	1.10
1.11	.3517	1.47393365	- 1.90090090	.426967252	1.12
1.12	.3533	1.47169811	- 1.89285714	.421159030	1.13
1.13	.3550 .3567	1.46948357 1.46728972	- 1.88495575 - 1.87719298	.415472184	1.14
		1.46511628	- 1.86956522	.404448938	.15
1.15	.3583		- 1.86206897	.399106003	.16
1.16	.3600	1.46296296	- 1.85470085	.393871362	.17
1.17	.3633	1.45871560	- 1.84745763	.388742031	.18
1.18 1.19	.3650	1.45662100	- 1.94033613	.383715130	.19
1.20	.3667	1.45454545	- 1.83333333	.378787879	.20
1.21	.3683	1.45248869	- 1.82644628	.373957593	.21
1,22	.3700	1.45045045	- 1.81967213	.369221681	.22
1.23	.3717	1.44843049	- 1.81300813	.364577637	.23
1.24	.3733	1.44642857	- 1.80645161	.360023041	.24
1.25	.3750	1.4444444	- 1.80000000	.35555556	.25
1.26	.3767	1.44247788	- 1.79365079	.351172918	.26
1.27	.3783	1.44052863	- 1.78740157	.346872940	.27
1.28	.3800	1.43859849	- 1.78125000	.342653509	.28
1.29	.3817	1.43668122	- 1.77519380	.338512576	.29
V	12E0			1.0	
	ar (	1.0		1 - 11	1
$p = \frac{x_2 - x_1}{x_1 - x_0} = \frac{b}{a}$	$\frac{2^2}{a^2f^{(3)}(\xi)}$	- 2B <sub>0</sub> a -	$-\frac{1}{2}B_{1}^{0}$ a	$-\frac{1}{2}B_{2}^{0}$ a	

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			ے ر ر <sub>2</sub> ا			***	
-x <sub>1</sub> -x <sub>0</sub> a x <sub>2</sub> -x <sub>1</sub> b	2 B <sub>0</sub> b <sup>2</sup>	<sup>2</sup> Bi b <sup>2</sup>	2Bi b2	$\frac{{}_{2}^{2}E^{0}}{bf^{(3)}(\xi)}$	$\frac{{}^{2}E^{1}}{bf^{(3)}(E)}$	2E <sup>2</sup> bf <sup>(3)</sup> (ξ)	
0.10 .11 .12 .13	18.1818182 16.3800164 14.8809524 13.6147039 12.5313283	-20.0000000 -18.1818182 -16.6666667 -15.3846154 -14.2857143	1.81818182 1.80180180 1.78571429 1.76991150 1.75438596	-0.4000 4067 4133 4200 4267	-0.3000 2967 2933 2900 2867	0.7000 .7033 .7067 .7100 .7133	0.10 .11 .12 .13
.15 .16 .17 .18 .19	11.5942029 10.7758621 10.0553042 9.41619586 8.84564352	-13.3333333 -12.5000000 -11.7647059 -11.1111111 -10.5263158	1.73913043 1.72413793 1.70940171 1.69491525 1.68067227	4333 4400 4467 4533 4600	2833 2800 2667 2733 2700	.7167 .7200 .7233 .7267 .7300	.15 .16 .17 .18 .19
.20 .21 .22 .23 .24	8.33333333 7.87091696 7.45156482 7.06963592 6.72043010	-10.00000000 - 9.52380952 - 9.09090909 - 8.69565217 - 8.33333333	1.66666667 1.65289256 1.63934426 1.62601626 1.61290323	4666 4733 4800 4867 4933	2667 2633 2600 2567 2533	.7333 .7367 .7400 .7433 .7467	.20 .21 .22 .23 .24
.25 .26 .27 .28	6.40000000 6.10500610 5.83260426 5.58035714 5.34616412	- 8.00000000 - 7.69230769 - 7.40740741 - 7.14285714 - 6.89655172	1.60000000 1.58730159 1.57480315 1.56250000 1.55038760	5000 5067 5133 5200 5267	2500 2467 2433 2400 2367	.7500 .7533 .7567 .7600 .7633	.25 .26 .27 .28
.30 .31 .32 .33 .34	5.12820512 4.92489534 4.73484848 4.55684666 4.38981562	- 6.5666667 - 6.45161290 - 6.25000000 - 6.06060606 - 5.88235294	1.53846154 1.52671756 1.51515152 1.50375940 1.49253731	5333 5400 5467 5533 5600	2333 2300 2267 2233 2200	.7667 .7700 .7733 .7766 .7800	.30 .31 .32 .33 .34
.35 .36 .37 .38	4.23280424 4.08496732 3.94555140 3.81388254 3.68935620	- 5.71428571 - 5.55555556 - 5.40540541 - 5.26315789 - 5.12820513	1.48148148 1.47058824 1.45985401 1.44927536 1.43884892	5667 5733 5800 5867 5933	2167 2133 2100 2067 2033	.7833 .7867 .7900 .7933 .7967	.35 .36 .37 .38 .39
.40 .41 .42 .43 .44	3.57142858 3.45960906 3.35345406 3.25256140 3.15656566	- 5.0000000 - 4.87804878 - 4.76190476 - 4.65116279 - 4.54545455	1.42857143 1.41843972 1.40845070 1.39860140 1.38888889	6000 6067 6133 6200 6267	2000 1967 1933 1900 1867	.8000 .8033 .8067 .8100	.40 .41 .42 .43
.45 .46 .47 .48 .49	3.06513410 2.97796307 2.89477493 2.81531532 2.73935077	- 4.4444444 - 4.34782609 - 4.25531915 - 4.16666667 - 4.08163265	1.37931034 1.36986301 1.36054422 1.35135135 1.34228188	6333 6400 6467 6533 6600	1833 1800 1767 1733 1700	.8167 .8200 .8233 .8267 .8300	.45 .46 .47 .48 .49
.50 .51 .52 .53	2.66666667 2.59706532 2.53036437 2.46639536 2.40500241	- 4.00000000 - 3.92156863 - 3.84615385 - 3.77358491 - 3.70370370	1.33333333 1.32450331 1.31578947 1.30718954 1.29870130	6667 6733 6800 6867 6933	1667 1633 1600 1567 1533	.8333 .8367 .8400 .8433 .8467	.50 .51 .52 .53 .54
.55 .56 .57 .58	2.34604106 2.28937729 2.23488658 2.18245308 2.13196887	- 3.63636364 - 3.57142857 - 3.50877193 - 3.44827586 - 3.38983051	1.29032258 1.28205128 1.27388535 1.26582278 1.25786164	7000 7067 7133 7200 7267	1500 1467 1433 1400 1367	.8500 .8533 .8567 .8600 .8633	•55 •56 •57 •58 •59
.60 .61 .62 .63	2.08333333 2.03645250 1.99123855 1.94760931 1.90548780	- 3.3333333 - 3.27868852 - 3.22580645 - 3.17460317 - 3.12500000	1.25000000 1.24223602 1.23456790 1.22699387 1.21951220	7333 7400 7467 7533 7600	1333 1300 1267 1233 1200	.8667 .8700 .8733 .8767 .8800	.60 .61 .62 .63
.65 .66 .67 .68	1.86480186 1.82548375 1.78746984 1.75070028 1.71511877	- 3.07692308 - 3.03030303 - 2.98507463 - 2.94117647 - 2.89855072	1.21212121 1.20481928 1.19760479 1.19047619 1.18343195	7667 7733 7800 7867 7933	1167 1133 1100 1067 1033	.8833 .8867 .8900 .8933 .8967	.65 .66 .67 .68
	28 i a2	2Bi a <sup>2</sup>	2Bi a2	$-\frac{{}^{2}E^{2}}{af^{(3)}(\xi)}$	$-\frac{\frac{2}{2}E^{i}}{af^{(3)}(\xi)}$	$-\frac{\frac{2E^0}{2}}{af^{(3)}(\xi)}$	$p = \frac{x_2 - x_1}{x_1 - x_0} = \frac{b}{a}$

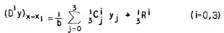
		$(D^2y)_{x=x_i} =$	$\sum_{j=0}^{2} {}_{2}^{2}B_{j}^{i}y_{j} +$	2 R i	(i=0,1,2)	5	NACA
r= x1-x0 a	2Bi b2	2Bi b2	2Bi b2	2E0	2E1	<sup>2</sup> <sub>2</sub> E <sup>2</sup>	7
r= x <sub>2</sub> -x <sub>1</sub> b	2 0	2 1	* 2	bf (3) (ξ)	bf (3)		
0.70 .71	1.68067227	- 2.85714286	1.17647059	-0.8000	-0.1000	0.9000	0.70
.72	1.64731077	- 2.81690141 - 2.77777778	1.16959064	8067	0967	.9033 .9067	.71
•73	1.58365666	- 2.73972603	1.15606936	8200	0900	.9100	.73
.74	1.55327742	- 2.70270270	1.14942529	8267	0867	.9133	.74
•75	1.52380952	- 2.66666667	1.14285714	8333	0833	.9167	<b>.7</b> 5
.76 .77	1.49521531	- 2.63157895 - 2.59740260	1.13636364	8400	0800	.9200 .9233	.76
•78	1.44050706	- 2.56410256	1.12359551	8533	0733	.9267	.78
.79	1.41432713	- 2.53164557	1.11731844	8600	0700	•9300	.79
.80 .81	1.38888889	- 2.50000000	1.11111111	8667	0667	.9333	.80
.82	1.36416343	- 2.46913580 - 2.43902439	1.10497238	8733	0633	.9367	.81 .82
.83	1.31674238	- 2.40963855	1.09289617	8867	0567	.9433	.83
.84	1.29399586	- 2.38095238	1.08695652	8933	0533	.9467	.84
•85	1.27186010	- 2.35294118	1.08108108	9000	0500	•9500	.85
•86 •87	1.25031258 1.22933186	- 2.32558140 - 2.29885058	1.07526882	9067	0467 0433	.9533 .9567	.86 .87
•88	1.20889749	- 2.27272727	1.06382979	9200	0400	9600	.88
•89	1.18898945	- 2.24719101	1.05820106	9267	0367	•9633	.89
•90	1.16959064	- 2.22222222	1.05263158	9333	0333	.9667	•90
.91 .92	1.15068178	- 2.19780220 - 2.17391304	1.04712042	9400	0300	.9700 .9733	.91
.93	1.11426820	- 2.15053763	1.03626943	9533	0233	.9767	.93
•94	1.09673174	- 2.12765957	1.03092784	9600	0200	•9800	.94
•95	1.07962213	- 2.10526316	1.02564103	9667	0167	.9833	.95
.96 .97	1.06292517	- 2.08333333 - 2.06185567	1.02040816	9733	0133	.9867	.96
•98	1.03071532	- 2.04081633	1.01522843	9800 9867	0100	.9900 .9933	.98
•99	1.01517689	- 2.02020202	1.00502513	9933	0033	.9967	.99
1.00	1.00000000	- 2.00000000	1.00000000	-1,0000	ao	1.0000	1.00
1.01	.985173144 .970685304	- 1.98019802 - 1.96078431	.995024876 .990099010	-1.0067	•0033	1.0033	1.01
1.03	.956525898	- 1.94174757	.985221675	-1.0133 -1.0200	.0067	1.0067	1.02
1.04	.942684766	- 1.92307692	.980392157	-1.0267	.0133	1.0133	1.04
1.05	.929152148	- 1.90476190	.975609756	-1.0333	.0167	1.0167	1.05
1.06	.915918666 .902975304	- 1.88679245 - 1.86915888	.970873786	-1.0400	.0200	1.0200	1.06
1.08	.890313390	- 1.85185185	.966183575 .961538462	-1.0467 -1.0533	.0233 .0267	1.0233	1.07
1.09	.877924586	- 1.83486239	.956937799	-1.0600	.0300	1.0300	1.09
1.10	.865800866	- 1.81818182	.952380952	-1.0667	.0333	1.0333	1.10
1.11	.853934504 .942318060	- 1.80180180 - 1.78571429	.947867299	-1.0733	.0367	1.0367	1.11
1.13	.830944368	- 1.76991150	.943396226 .938967136	-1.0800 -1.0867	.0400 .0433	1.0400	1.12
1.14	.819806526	- 1.75438596	.934579439	-1.0933	.0467	1.0467	1.14
1.15	.808897876	- 1.73913043	•930232558	-1.1000	.0500	1.0500	1.15
1.16	.798212006 .787742724	- 1.72413793 - 1.70940171	.925925926 .921658986	-1.1067	.0533	1.0533	1.16
1.18	.777484062	- 1.69491525	.917431193	-1.1133 -1.1200	.0567 .0600	1.0592	1.17
1.19	.767430260	- 1.68067227	.913242009	-1.1267	.0633	1.0633	1.19
1.20	.757575758	- 1.66666667	.909090909	-1.1333	.0667	1.0667	1.20
1.21	.747915186 .738443362	- 1.65289256 - 1.63934426	.904977375	-1.1400	.0700	1.0700	1.21
1.23	.729155274	- 1.62601626	.896860987	-1.1467 -1.1533	.0733 .0767	1.0733	1.22
1.24	.720046082	- 1.61290323	.892857143	-1.1600	.0800	1.0800	1.24
1.25	.711111112	- 1.60000000	.88888888	-1.1667	•08 <b>3</b> 3	1.0833	1.25
1.26	.702345836 .693745880	- 1.58730159 - 1.57480315	.884955752	-1.1733	.0867	1.0867	1.26
1.28	.685307018	- 1.56250000	.881057269 .877192982	-1.1800 -1.1867	.0900 .0933	1.0900 1.0933	1.27
1.29	.677025152	- 1.55038760	.873362445	-1.1933	.0967	1.0967	1.29
	2 1 2	0-1-5		2 <u>-2</u> 2	²€¹	2£0	p=x2-x1
	28i a2	2Bi a2	28 a2	$-\frac{2}{af^{(3)}(\xi)}$	$-\frac{2}{af^{(3)}(\xi)}$	$-\frac{2}{af^{(3)}(\xi)}$	b=x1-x0
	_			((۵) انت	at (8)	ar (2)	

<sup>&</sup>lt;sup>a</sup>The next order remainder term is 0.0833  $\left[f^{(4)}(x)\right]_{x=x_1}$ 

$$(0^{i}y)_{X=X_{j}} = \frac{1}{b} \sum_{j=0}^{3} {}_{3}^{i}C_{j}^{j} y_{j} + {}_{3}^{i}R^{i}$$
 (i=0,3)



			j=0	,	~	and and
r= <u>a_a</u> b_c	1 C 0 3 C 0	1 C0	1C0 3C2	1 C <sup>0</sup> 3	$\frac{\frac{1}{3}E^0}{b^3f^{(4)}(g)}$	
0.10 .11 .12 .13 .14	-11.3852814 -10.4657436 - 9.69788859 - 9.04674701 - 8.48733984	11.5500000 10.6459091 9.8933333 9.25730769 8.71285714	-0.190909091 209099099 227142857 245044248 262807018	0.0261904762 .0289336493 .0316981132 .0344835681 .0372897196	-0.0096 0107 0119 0130 0142	0.10 .11 .12 .13
.15 .16 .17 .18	- 8.00134816 - 7.57503193 - 7.19788329 - 6.86172878 - 6.56011503	8.24166667 7.83000000 7.46735294 7.14555556 6.85815789	280434783 297931034 315299145 332542373 349663866	.0401162791 .0429629630 .0458294931 .0487155963 .0516210046	0155 0167 0180 0193 0206	.15 .16 .17 .18
.20 .21 .22 .23 .24	- 6.28787878 - 6.04083973 - 5.81557713 - 5.60926471 - 5.41954685	6.60000000 6.36690476 6.15545455 5.96282609 5.78666667	366666667 383553719 400327869 416991870 433548387	.0545454545 .0574886878 .0604504505 .0634304933 .0664285714	0220 0234 0248 0263 0278	.20 .21 .22 .23
.25 .26 .27 .28 .29	- 5.24444444 - 5.08228252 - 4.93163391 - 4.79127506 - 4.66015088	5.62500000 5.47615385 5.33870370 5.21142857 5.09327586	450000000 466349206 482598425 498750000 514806202	.0694444444 .0724778761 .0755286344 .0785964912 .0816812227	0293 0308 0324 0340 0357	.25 .26 .27 .28 .29
.30 .31 .32 .33	- 4.53734671 - 4.42206566 - 4.31361024 - 4.21136728 - 4.11479555	4.98333333 4.88080645 4.78500000 4.69530303 4.61117647	530769231 546641221 562424242 578120301 593731343	.0847826087 .0879004329 .0910344828 .0941845494 .0973504274	0374 0391 0408 0426 0444	.30 .31 .32 .33
.35 .36 .37 .38 .39	- 4.02341551 - 3.93680071 - 3.85457064 - 3.77638470 - 3.70193707	4.53214286 4.45777778 4.38770270 4.32157895 4.25910256	609259259 624705882 640072993 655362319 670575540	.100531915 .103728814 .106940928 .110168067 .113410042	0463 0481 0500 0520 0540	.35 .36 .37 .38
.40 .41 .42 .43	- 3.63095238 - 3.56318201 - 3.49840087 - 3.43640473 - 3.37700778	4.20000000 4.14402439 4.09095238 4.04058140 3.99272727	685714286 700780142 715774648 730699301 745555556	.116666667 .119937759 .123223140 .126522634 .129836066	0560 0581 0601 0623 0644	.40 .41 .42 .43
.45 .46 .47 .48	- 3.32004066 - 3.26534862 - 3.21278998 - 3.16223482 - 3.11356369	3.94722222 3.90391304 3.86265957 3.82333333 3.78581633	760344828 775068493 789727891 804324324 818859060	.133163265 .136504065 .139858300 .143225806 .146606426	0666 0688 0711 0734 0757	.45 .46 .47 .48
.50 .51 .52 .53	- 3.06666667 - 3.02144234 - 2.97779706 - 2.93564414 - 2.89490329	3.75000000 3.71578431 3.68307692 3.65179245 3.62185185	833333333 847748344 862105263 876405229 890649351	.150000000 .153406375 .156825397 .160256917 .163700787	0781 0805 0830 0855 0880	.50 .51 .52 .53
.55 .56 .57 .58 .59	- 2.85549997 - 2.81736493 - 2.78043370 - 2.74464622 - 2.70994646	3.59318182 3.56571429 3.53938596 3.51413793 3.48991525	904838710 918974359 933057325 947088608 961069182	.167156863 .170625000 .174105058 .177596899 .181100386	0906 0932 0958 0985 1012	.55 .56 .57 .58
.60 .61 .62 .63	- 2.67628205 - 2.64360404 - 2.61186657 - 2.58102666 - 2.55104398	3.46666667 3.44434426 3.42290323 3.40230159 3.38250000	975000000 98881988 -1.00271605 -1.01650307 -1.03024390	.184615385 .188141762 .191679389 .195228137 .198787879	1040 1068 1097 1125 1155	.60 .61 .62 .63
65 66 67 68 69	- 2.52188064 - 2.49350100 - 2.46587154 - 2.43896066 - 2.41273855	3.36346154 3.34515152 3.32753731 3.31058824 3.29427536	-1.04393939 -1.05759036 -1.07119760 -1.08476190 -1.09828402	.202358491 .205939850 .209531835 .213134328 .216747212	1184 1214 1245 1276 1307	.65 .66 .67 .68
	- 1C3	- <sup>1</sup> C <sup>3</sup> <sub>2</sub>	- 1 C3	- <sup>1</sup> <sub>3</sub> C <sub>0</sub> <sup>3</sup>	$-\frac{{}_{3}^{1}E^{3}}{{}_{5}^{3}f^{(4)}(z)}$	p=CC b a





	- 1C3	- ½C3	- 1C3	- <sup>1</sup> C <sup>3</sup>	$-\frac{{}^{1}E^{3}}{{}^{3}f^{(4)}(\xi)}$	p c c p c c
1.25 1.26 1.27 1.28 1.29	- 1.55213675 - 1.54287714 - 1.53374061 - 1.52472454 - 1.51582639	2.92500000 2.92365079 2.92240157 2.92125000 2.92019380	-1.80555556 -1.81752212 -1.82947137 -1.84140351 -1.85331878	.432692308 .436748466 .440810398 .444878049 .448951368	3809 3868 3928 3989 4050	1.25 1.26 1.27 1.28 1.29
1.20 1.21 1.22 1.23 1.24	- 1.60037879 - 1.59046145 - 1.58068159 - 1.57103615 - 1.56152216	2.93333333 2.93144628 2.92967213 2.92800813 2.92645161	-1.74545455 -1.75751131 -1.76954955 -1.78156951 -1.79357143	.412500000 .416526480 .420559006 .424597523 .428641975	3520 3577 3634 3691 3750	1.20 1.21 1.22 1.23 1.24
1.15 1.16 1.17 1.18 1.19	- 1.65214181 - 1.64148762 - 1.63098776 - 1.62063863 - 1.61043676	2.94456522 2.94206897 2.93970085 2.93745763 2.93533613	-1.68488372 -1.69703704 -1.70917051 -1.72128440 -1.73337900	.392460317 .396455696 .400457413 .404465409 .408479624	3245 3299 3353 3408 3464	1.15 1.16 1.17 1.18 1.19
1.10 1.11 1.12 1.13 1.14	- 1.70786203 - 1.69637796 - 1.68506808 - 1.67392814 - 1.66295404	2.95909091 2.95590090 2.95285714 2.94995575 2.94719298	-1.62380952 -1.63606635 -1.64830189 -1.66051643 -1.67271028	.372580645 .376543408 .380512821 .384488818 .388471338	2984 3035 3087 3139 3192	1.10 1.11 1.12 1.13 1.14
1.05 1.06 1.07 1.08 1.09	- 1.76805468 - 1.75563051 - 1.74340413 - 1.73137048 - 1.71952469	2.97738095 2.97339623 2.96957944 2.96592593 2.96243119	-1.56219512 -1.57456311 -1.58690821 -1.59923077 -1.61153110	.352868852 .356797386 .360732899 .364675325 .368624595	2735 2784 2833 2883 2933	1.05 1.06 1.07 1.08 1.09
1.00 1.01 1.02 1.03 1.04	- 1.83333333 - 1.81983736 - 1.80656749 - 1.79351763 - 1.78068191	3.00000000 2.99509901 2.99039216 2.98587379 2.98153846	-1.50000000 -1.51248756 -1.52495050 -1.53738916 -1.54980392	.33333333 .337225914 .341125828 .345033003 .348947368	2500 2546 2593 2640 2687	1.00 1.01 1.02 1.03 1.04
.95 .96 .97 .98	- 1.90443514 - 1.88970859 - 1.87524238 - 1.86102914 - 1.84706173	3.02763158 3.02166667 3.01592784 3.01040816 3.00510101	-1.43717949 -1.44979592 -1.46238579 -1.47494949 -1.48748744	.313983051 .317837838 .321700337 .325570470 .329448161	2277 2321 2365 2409 2454	.95 .96 .97 .98
.90 .91 .92 .93	- 1.98225449 - 1.96610392 - 1.95025561 - 1.93470046 - 1.91942976	3.06111111 3.05390110 3.04695652 3.04026882 3.03382979	-1.37368421 -1.38643979 -1.39916667 -1.41186528 -1.42453608	.294827586 .298642612 .302465753 .306296928 .310136054	2066 2107 2149 2191 2234	.90 .91 .92 .93
.85 .86 .87 .88	- 2.06788832 - 2.05007546 - 2.03261670 - 2.01550075 - 1.99871680	3.10147059 3.09279070 3.08442529 3.07636364 3.06859551	-1.30945946 -1.32236559 -1.33524064 -1.34808511 -1.36089947	.275877193 .279650350 .283432056 .28722222 .291020761	1867 1906 1946 1985 2026	.85 .86 .87 .88
.80 .81 .82 .83	- 2.16269841 - 2.14292598 - 2.12357267 - 2.10462425 - 2.08606713	3.15000000 3.13956790 3.12951220 3.11981928 3.11047619	-1.2444444 -1.25751381 -1.27054945 -1.28355191 -1.29652174	.257142857 .260871886 .264609929 .268356890 .272112676	1680 1717 1754 1791 1829	.80 .81 .82 .83
.75 .76 .77 .78	- 2.26839827 - 2.24629013 - 2.22468388 - 2.20356127 - 2.18290494	3.20833333 3.19578947 3.18370130 3.17205128 3.16082278	-1.17857143 -1.19181818 -1.20502825 -1.21820225 -1.23134078	.238636364 .242318841 .246010830 .249712230 .253422939	1504 1538 1573 1608 1644	.75 .76 .77 .78
0.70 .71 .72 .73 .74	- 2.38717709 - 2.36224972 - 2.33793130 - 2.31419806 - 2.29102750	3.27857143 3.26345070 3.2488889 3.23486301 3.22135135	-1.11176471 -1.12520468 -1.13860465 -1.15196532 -1.16528736	0,220370370 .224003690 .227647059 .231300366 .234963504	-0.1339 1371 1404 1437 1470	0.70 .71 .72 .73
$r = \frac{a}{b} = \frac{a}{c}$	<sup>1</sup> C <sub>0</sub>	3 C 1	1 C <sub>2</sub>	1C0 3C3	$\frac{\frac{1}{3}E^{0}}{b^{3}f^{(4)}(\xi)}$	



		$(b y)_{x=x_1} = \frac{1}{b} $	_/ 3°j ' 3 "			w w
				lal		
r= <u>a_a</u> b c	3C0	3C 1	3C2	1 C1	b <sup>3</sup> f <sup>(4)</sup> (約	
0.10	-8.65800866	8.50000000	0.181818182	-0.0238095238	0.0083	0.10
0.10 .11	-7.76304094	7.59090909	.198198198	0260663507	.0092	.11
.12	-7.01931716	6.83333333	.214285714	0283018868	.0100	.12
.13	-6.39187976	6.19230769	.230088496	0305164319	•0108	.13 .14
.14	-5.85576090	5.64285714	.245614035	0327102804	•0117	
.15	-5.39265251	5.16666667	.260869565	0348837209 0370370370	.0125 .0133	.15 .16
.16	-4.98882503	4.75000000 4.38235294	.275862069 .290598291	0391705069	.0142	.17
.17	-4.63378072 -4.31935590	4.05555556	.305084746	0412844037	.0150	.18
.18 .19	-4.03910663	3.76315789	.319327731	0433789954	•0158	.19
.20	-3.78787879	3.50000000	.333333333	0454545455	.0167	.20
.21	-3.56150089	3.26190476	.347107438	0475113112	.0175	.21
.22	-3.35656073	3.04545455	.360655738	0495495495	.0183	.22 .23
.23	-3.17024032	2.84782609	.373983740	0515695067 0535714286	.0192 .0200	.24
.24	-3.00019201	2.66666667	.387096774			
.25	-2.8444444	2.50000000	.400000000	055555556	.0208 .0217	.25 .26
.26	-2.70133013	2.34615385	.412698413 .425196850	0575221239 0594713656	.0225	.27
.27	-2.56942919 -2.44752506	2.20370370 2.07142857	.437500000	0614035088	.0233	.28
.28 .29	-2.33456949	1.94827586	.449612403	0633187773	.0242	.29
.30	-2,22965440	1.83333333	.461538462	0652173913	•0250	.30
.31	-2.13198933	1.72580645	.473282443	0670995671	.0258	.31
.32	-2.04088297	1.62500000	•484848485 •486848683	0689655172	.0267 .0275	.32 .33
.33 .34	-1.95572818 -1.87598958	1.53030303 1.44117647	.496240602 .507462687	0708154506 0726495726	0283	.34
	-1.80119329	1.35714286	.518518519	0744680851	.0292	.35
.35 .36	-1.73091836	1.27777778	.529411765	0762711864	.0300	.36
.37	-1.66478962	1.20270270	.540145985	0780590717	.0308	.37 .38
.38 .39	-1.60247165 -1.54366369	1.13157895 1.06410256	.550724638 .561151079	0798319328 0815899582	.0317 .0325	.39
		1.00000000	.571428571	0833333333	.0333	.40
.40 .41	-1.48809524 -1.43552243	.939024390	581560284	0850622407	.0342	.41
42	-1.38572482	.880952381	.591549296	0867768595	.0350	.42
.43	-1.33850263 -1.29367445	.825581395 .772727273	.601398601 .61111111	0884773663	.0358 .0367	.43 .44
.44				0918367347	.0375	•45
•45	-1.25107514	.722222222 .673913043	.620689655 .630136986	0934959350	.0383	.46
.46 .47	-1.21055409 -1.17197366	.627659574	.639455782	0951417004	.0392	.47
.48	-1.13520779	.583333333	.648648649	0967741935	.0400	.48
.49	-1.10014087	.540816327	.657718121	0983935743	.0408	.49
•50	-1.06666667	.500000000	.66666667	100000000 101593626	.0417 .0425	.50 .51
•51	-1.03468738	.460784314 .423076923	.675496689 .684210526	103174603	.0433	.52
.52 .53	-1.00411285 974859827	.386792453	.692810457	104743083	.0442	.53
.54	946851341	.351851852	.701298701	106299213	.0450	•54
.55	920016100	.318181818	.709677419	107843137	.0458	•55
•56	894288004	.285714286	.717948718	109375000	.0467 .0475	.56 .57
•57	869605673	.254385965 224137931	.726114650 .734177215	110894942 112403101	.0483	.58
.58 .59	845912045 823154005	.224137931 .194915254	.742138365	113899614	.0492	.59
.60	801282051	.166666667	.750000000	115384615	•0500	.60
.61	780250000	.139344262	.757763975	116858238	.0508	.61
.62	760014714	.112903226	.7654 <b>3</b> 2099	118320611 119771863	.0517 .0525	.62 .63
.63 .64	740535859 721775684	.087301587 .062500000	.780487805	121212121	.0533	.64
.65	703698817	.038461538	.787878788	122641509	.0542	.65
.66	686272088	.015151515	.795180723	124060150	•0550	•66
.67	669464358	007462687	.802395210	125468165	.0558 .0567	.67 .68
-68	653246373	029411765	.809523810 .816568047	126865672 128252788	.0575	.69
.69	637590622	860#31060	*01000047	.120202,00		
					1 <u>E</u> 2	
	1 1.2	102	102	I C2	3	p <u>cc</u> ba
	- 1C2	- 1C2	- 1C2	- <sup>1</sup> C <sup>2</sup> <sub>0</sub>	b <sup>3</sup> f <sup>(4)</sup> (E)	9-2-2

$(D^{\dagger}y)_{x=x_{i}} * \frac{1}{b} = \sum_{j=0}^{3} {}_{3}C_{j}^{i} y_{j} +$	'R'	(i-1,2)
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		$x=x_i$ $\overline{b}$ $y_{x=x_i}$	ο 3° j 3' j 3"		~	w m
	[				i E i	
$\frac{\mathbf{a}}{\mathbf{b}} = \frac{\mathbf{a}}{\mathbf{c}}$	1C 1	1 C	1 C 1 2	1 C 1	b <sup>3</sup> f <sup>(4)</sup> (ξ)	
	-0.622471211	-0.071428571	0.823529412	-0.129629630	0.0583	0.70
70 71	607863751	091549296	.830409357	130996310	.0592	.71
.72	593745250	1111111111	.837209302	132352941	.0600	.72
.73	580094016	130136986	.843930636	133699634	.0608	.73 .74
.74	566889568	148648649	.850574713	135036496	.0617	• 1 4
•75	554112554	166666667	.857142857	136363636	.0625	•75
.76	541744678	184210526	.86363636 <del>4</del>	137681159	.0633	.76 .77
.77	529768626	201298701	.870056497 .876404494	138989170 140287770	.0642 .0650	.78
.78 .79	518168007 506927288	217948718 234177215	.882681564	141577061	.0658	.79
•				1.400583.47	0668	90
.80	496031746	250000000	.888888889 .895027624	142857143 144128114	.0667 .0675	.80 .81
.81 .82	485467412 475221025	265432099 280487805	.901098901	145390071	.0683	.82
.83	465279993	295180723	.907103825	146643110	.0692	.83
.84	455632345	309523810	.91304347B	147887324	.0700	.84
Q.F.	446266700	323529412	.918918919	149122807	.0708	.85
.85 .86	437172230	337209302	.924731183	150349650	.0717	.86
.87	428338627	350574713	.930481283	151567944	.0725	.87
.88	419756071	363636364	.936170213	152777778	.0733	.88
.89	411415209	376404494	.941798942	153979239	.0742	.89
•90	403307118	38888889	.947368421	155172414	•0750	.90
.91	395423292	401098901	.952879581	156357388	•0758	.91
.92	387755608	413043478	.958333333	157534247	•0767	.92 .93
.93 .94	380296315 373038007	424731183 436170213	.963730570 .969072165	158703072 159863946	.0775 .0783	.94
• 54	- ,07000001	- 1001/0510			-	
.95	365973604	447368421	.974358974	161016949 162162162	.0792 .0800	.95 .96
.96 .97	359096341 352399745	458333333 469072165	.979591837 .984771574	163299663	.0808	.97
.98	345877623	479591837	.989898990	164429530	.0817	98
.99	339524045	489898990	.994974874	165551839	.0825	.99
1 00	333333333	500000000	1.00000000	166666667	.0833	1.00
1.00 1.01	327300048	509900990	1.00497512	167774086	.0842	1.01
1.02	321418975	519607843	1.00990099	168874172	•0850	1.02
1.03	315685115	529126214	1.01477833	169966997	•0858	1.03
1.04	310093673	538461538	1.01960784	171052632	.0867	1.04
1.05	304640049	547619048	1.02439024	172131148	•0875	1.05
1.06	299319826	556603774	1.02912621	173202614	.0883	1.06
1.07	294128763	565420561	1.03381643	174267101 175324675	.0892 .0900	1.07
1.08 1.09	289062789 284117989	574074074 582568807	1.03846154	176375405	.0908	1.09
				3 777 43 07 55	0017	1 10
1.10	279290602	590909091	1.04761905	177419355 178456592	.0917 .0925	1.10
1.11 1.12	274577011 269973737	607142857	1.05660377	179487179	.0933	1.12
1.13	265477434	615044248	1.06103286	180511182	.0942	1.13
1.14	261084881	622807018	1.06542056	181528662	•0950	1.14
1.15	256792977	630434783	1.06976744	182539683	•0958	1.15
1.16	252598736	637931034	1.07407407	183544304	.0967	1.16
1.17	248499282	645299145	1.07834101	184542587	.0975	1.17
1.18	244491843 - 240573749	652542373	1.08256881	185534591 186520376	.0983	1.18
1.19	240573749	659663866	1.08675799	.1000.00.0		
1.20	236742424	666666667	1.09090909	187500000	.1000	1.20
1.21	232995385	673553719 680327869	1.09502262	188473520 189440994	.1008 .1017	1.21
1.22 1.23	229330236 225744667	686991870	1.10313901	190402477	1025	1.23
1.24	222236445	693548387	1.10714286	191358025	.1033	1.24
	_ 910007410	700000000	1.11111111	192307692	.1042	1.25
1.25 1.26	218803419 215443508	700000000	1.11504425	193251534	.1050	1.26
1.27	212154704	712598425	1.11894273	194189602	.1058	1.27
1.28	208935066	718750000	1.12280702	195121951	.1067	1.28
1.29	205782721	724806202	1.12663755	196048632	.1075	1.29
					1.52	
	1 02	102	102	102	1 E <sup>2</sup>	сс
	- 1C2	- 1C2	- 1C2	- 1C2		p= <u>c_c</u> b a
	) )	2 4	3 1	3 0	b <sup>3</sup> f <sup>(4)</sup> (£)	D a

$(D^1y)_{\mathbf{x}=\mathbf{x}} = \frac{1}{D}$	$\sum_{i=0}^{3}$	lci 3°j	Уј	+	¹Ri	(i=2,1)
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		j=0	2 1 , 3			THE PLANT
					13E2	
<u>=a=a</u> b c	1 C2	1 C <sup>2</sup>	1 C2 3 C2	1 C2 3	b <sup>2</sup> f <sup>(4)</sup> (ξ)	
0.10	4.32900433	-5.50000000	0.909090909	0.261904762	-0.0458	0.10
.11	3.88152047	-5.04545455	.900900901	.263033175	0463	.11
.12	3.50965858	-4.66666667	.892857143	.264150943	0467	.12
.13	3.19593988 2.92788045	-4.34615385 -4.07142857	.884955752 .877192982	.265258216 .266355140	0471 0475	.13
.15	2.69632626	-3.83333333	.869565217	.267441860	0479	.15
.16	2.49441252	-3.62500000	.862068966	.268518519	0483 0488	.16 .17
.17	2.31689036	-3.44117647 -3.27777778	.854700855 .847457627	.269585253 .270642202	0492	.18
.18 .19	2.15967795 2.01955332	-3.13157895	.840336134	.271689498	0496	.19
.20	1.89393939	-3.00000000	.833333333	.272727273	0500	.20
.21	1.78075044	-2.88095238	.826446281	.273755656	0504 0508	.21
.22	1.67828036	-2.77272727 -2.67391304	.819672131 .813008130	.274774775	0513	.23
.23 .24	1.58512016	-2.58333333	.806451613	.276785714	0517	.24
.25	1.42222222	-2.50000000	.800000000	.277777778	0521	.25
.26	1.35066506	-2.42307692	.793650794	.278761062 .279735683	0525 0529	.26 .27
.27	1.28471460	-2.35185185 -2.28571429	.787401575 .781250000	.280701754	0533	.28
.28 .29	1.16728475	-2.22413793	.775193798	.281659389	0538	.29
.30	1.11482720	-2.16666667	.769230769	.282608696	0542	.30
.31	1.06599467	-2.11290323	.763358779	.283549784	0546	.31
.32	1.02044149	-2.06250000 -2.01515152	.757575758 .751879699	.284482759 .285407725	0550 0554	.33
.33 .34	.977864090 .937994790	-1.97058824	.746268657	.286324786	0558	.34
.35	.900596645	-1.92857143	.740740741	.287234043	0563	.35
.36	.865459180	-1.88888889	.735294118	.288135593	0567 0571	.36
•37	.832394810	-1.85135135 -1.81578947	.729927007	.289029536 .289915966	0575	.38
.38 .39	.801235825 .771831845	-1.78205128	.719424460	.290794979	0579	.39
.40	.74404762	-1.75000000	.714285714	.291666667	0583	.40
.41	.717761215	-1.71951220	.709219858 .704225352	.292531120 .293388430	0588 0592	.41
.42 .43	.692862410 .669251315	-1.69047619 -1.66279070	699300699	.294238683	0596	. 43
.44	.646837225	-1.63636364	.69444444	.295081967	0600	.44
•45	.625537571	-1.61111111	.689655172	.295918367	0604	.45
.46	.605277047	-1.58695652	.684931507 .680272109	.296747967 .297570350	0608	.46
.47 .48	.585986828 .567603894	-1.56382979 -1.54166667	.675675676	298387097	0617	.48
.49	.550070437	-1.52040816	.671140940	.299196787	0621	•49
•50	.533333333	-1.50000000	.666666667	.300000000	0625 0629	.50 .51
.51 .52	.517343688 .502056423	-1.48039216 -1.46153846	.662251656 .657994737	.300796813 .301587302	0633	.52
.53	.487429914	-1.44339623	.653594771	.302371542	0638	.53
.54	.473425670	-1.42592593	.649350649	.303149606	0642	.54
. 55	.460008050	-1.40909091	.645161290	.303921569	0646 0650	•55 •56
•56	.447144002 .434802836	-1.39285714 -1.37719298	.641025641 .636942675	.304687500 .305447471	0654	.57
•57 •58	.422956023	-1.36206897	.632911392	.306201550	0658	•58
.59	.411577003	-1.34745763	.628930818	.306949807	0663	•59
.60	.400641026	-1.33333333	.625000000	.307692308 .308429119	0667 0671	.60 .61
.62	.390125000 .380007357	-1.31967213 -1.30645161	.621118012 .617283951	.309160305	0675	.62
.63	.370267930	-1.29365079	.613496933	.309885932	0679	.63
.64	.360887842	-1.28125000	•409756098	.310606061	0683	.64
.65	.351849408	-1.26923077	•606060606	.311320755 .312030075	0688 0692	.65 .66
.66 .67	.343136044 .334732179	-1.25757576 -1.24626866	.602409639 .598802395	.312734082	0696	.67
.68	326623187	-1.23529412	.595238095	.313432836	0700	•68
.69	.318795311	-1.22463768	.591715976	.314126394	0704	.69
					i <sub>3</sub> E <sup>1</sup>	
	- iCi	- 1C1	- 1C	- 1C1	3 (4)	$p=\frac{c}{b}=\frac{c}{a}$
	3 3	3 2	ا د	1 30	b f ( E)	U a

	(0	$(y)_{x-x_1} = \frac{1}{b} = \sum_{j=0}^{3} \frac{1}{3}$	C <sub>j</sub> y <sub>j</sub> + 1Ri	(i=2, l)	NA	CA
r=aa bc	1 C <sup>2</sup> 3 0	1 C 2	1C2 3C2	1C2 3C3	$\frac{\frac{1}{3}E^2}{b^3f^{(4)}(\xi)}$	
0.70 .71 .72 .73	0.311235605 .303931875 .296872625 .290047008 .283444784	-1.21428571 -1.20422535 -1.19444444 -1.18493151 -1.17567568	0.588235294 .584795322 .581395349 .578034682 .574712644	0.314814815 .315498155 .316176471 .316849817 .317518248	-0.0708 0713 0717 0721 0725	0.70 .71 .72 .73
.75 .76 .77 .78	.277056277 .270872339 .264884313 .259084003 .253463644	-1.16666667 -1.15789474 -1.14935065 -1.14102564 -1.13291139	.571428571 .568181818 .564971751 .561797753 .558659218	.318181818 .318840580 .319494585 .320143885 .320788530	0729 0733 0738 0742 0746	.75 .76 .77 .78
.80 .81 .82 .83	.248015873 .242733706 .237610513 .232639996 .227816172	-1.12500000 -1.11728395 -1.10975610 -1.10240964 -1.09523810	.55555556 .552486188 .549450549 .546448087 .543478261	.321428571 .322064057 .322695035 .323321555 .323943662	0750 0754 0758 0763 0767	.80 .81 .82 .83
.85 .86 .87 .88	.223133350 .218586115 .214169313 .209878036 .205707604	-1.08823529 -1.08139535 -1.07471264 -1.06818182 -1.06179775	.540540541 .537634409 .534759358 .531914894 .529100529	.324561404 .325174825 .325783972 .326388889 .326989619	0771 0775 0779 0783 0788	.85 .86 .87 .88
.90 .91 .92 .93	.201653559 .197711646 .193877804 .190148158 .186519003	-1.05555556 -1.04945055 -1.04347826 -1.03763441 -1.03191489	.526315789 .523560209 .520833333 .518134715 .515463918	.327586207 .328178694 .328767123 .329351536 .329931973	0792 0796 0800 0804 0808	.90 .91 .92 .93
.95 .96 .97 .98	.182986802 .179548171 .176199873 .172938811 .169762023	-1.02631579 -1.02083333 -1.01546392 -1.01020408 -1.00505051	.512820513 .510204082 .507614213 .505050505 .502512563	.330508475 .331081081 .331649832 .332214765 .332775920	0813 0817 0821 0825 0829	.95 .96 .97
1.00 1.01 1.02 1.03	.166666667 .163650024 .160709487 .157842557 .155046837	-1.00000000 995049505 990196078 985436893 980769231	.500000000 .497512438 .495049505 .492610837 .490196078	.33333333 .333887043 .334437086 .334983498 .335526316	0833 0838 0842 0846 0850	1.00 1.01 1.03 1.03
1.05 1.06 1.07 1.08 1.09	.152320024 .149659913 .147064382 .144531395 .142058995	976190476 971698113 967289720 962962963 958715596	.487804878 .485436893 .483091787 .480769231 .478468900	.336065574 .336601307 .337133550 .337662338 .338187702	0854 0858 0863 0867 0871	1.08 1.08 1.08 1.08
1.10 1.11 1.12 1.13	.139645301 .137288505 .134986868 .132738717 .130542441	954545455 950450450 946428571 942477876 938596491	.476190476 .473933649 .471698113 .469483568 .467289720	.338709677 .339228296 .339743590 .340255591 .340764331	0875 0879 0883 0888 0892	1.10 1.11 1.12 1.13
1.15 1.16 1.17 1.18	.128396489 .126299368 .124249641 .122245922 .120286875	934782609 931034483 927350427 923728814 920168067	.465116279 .462962963 .460829493 .458715596 .456621005	.341269841 .341772152 .342271293 .342767296 .343260188	0896 0900 0904 0908 0913	1.15 1.16 1.17 1.18 1.19
.20 .21 .22 .23	.118371212 .116497693 .114665118 .112872334 .111118223	916666667 913223140 909836066 906504065 903225806	•454545455 •452488688 •450450450 •448430493 •446428571	.343750000 .344236760 .344720497 .345201238 .345679012	0917 0921 0925 0929 0933	1.20 1.21 1.22 1.23 1.24
.25 .26 .27 .28 .29	.109401710 .107721754 .106077352 .104467533 .102891361	900000000 896825397 893700787 890625000 887596899	.44444444 .442477876 .440528634 .438596491 .436681223	.346153846 .346625767 .347094801 .347560976 .348024316	0938 0942 0946 0950 0954	1.28 1.26 1.27 1.28 1.29
	- [0]	- ici	- [C]	- 1C1	$-\frac{\frac{1}{3}E^{1}}{b^{3}f^{(4)}(\xi)}$	P====

$(D^{i}y)_{x \sim x_{i}} = \frac{i}{b}$	$\sum_{i=0}^{3}$	lci yj	+ 1Ri	(i-3,0)
	J=0	- ,		



	٠,	) /x-x; b = 0	3°j ' j ' 3''	(1-0,0)		MACA
$r = \frac{a}{b} = \frac{a}{c}$	1C3	1 C3	1 C3	1C3 3C3	$\frac{{}_{3}^{1}E^{3}}{b^{3}f^{(4)}(\xi)}$	
0.10 .11 .12 .13	-8.65800866 -7.76304094 -7.01931716 -6.39187976 -5.85576090	10.50000000 9.59090909 8.83333333 8.19230769 7.64285714	-3.81818182 -3.80180180 -3.78571429 -3.76991150 -3.75438596	1.97619048 1.97393365 1.97169811 1.96948357 1.96728972	0.1750 .1758 .1767 .1775 .1783	0.10 .11 .12 .13 .14
.15 .16 .17 .18 .19	-5.39265251 -4.98882503 -4.63378072 -4.31935590 -4.03910663	7.16666667 6.75000000 6.38235294 6.0555556 5.76315789	-3.73913043 -3.72413793 -3.70940171 -3.69491525 -3.68067227	1.96511628 1.96296296 1.96082949 1.95871560 1.95662100	.1792 .1800 .1808 .1817 .1825	.15 .16 .17 .18
.20 .21 .22 .23 .24	-3.78787879 -3.56150089 -3.35656073 -3.17024032 -3.00019201	5.50000000 5.26190476 5.04545454 4.84782609 4.66666667	-3.66666667 -3.65289256 -3.63934426 -3.62601626 -3.61290323	1.95454545 1.95248869 1.95045045 1.94843049 1.94642857	.1833 .1842 .1850 .1858 .1867	.20 .21 .22 .23
.25 .26 .27 .28 .29	-2.8444444 -2.70133013 -2.56942919 -2.44752506 -2.33456949	4.50000000 4.34615385 4.20370370 4.07142857 3.94827586	-3.60000000 -3.58730159 -3.57480314 -3.56250000 -3.55038760	1.9444444 1.94247788 1.94052863 1.93859649 1.93668122	.1875 .1883 .1892 .1900 .1908	.25 .26 .27 .28 .29
.30 .31 .32 .33	-2.22965440 -2.13198933 -2.0498297 -1.95572818 -1.87598958	3.83333333 3.72580645 3.62500000 3.53030303 3.44117647	-3.53846154 -3.52671756 -3.51515152 -3.50375940 -3.49253732	1.93478261 1.93290043 1.93103448 1.92918455 1.92735043	.1917 .1925 .1933 .1942 .1950	.30 .31 .32 .33
.35 .36 .37 .38 .39	-1.80119329 -1.73091836 -1.66478962 -1.60247165 -1.54366369	3.35714286 3.27777778 3.20270270 3.13157895 3.06410256	-3.48148148 -3.47058824 -3.45985402 -3.44927536 -3.43884892	1.92553191 1.92372881 1.92194093 1.92016807 1.91841004	.1958 .1967 .1975 .1983 .1992	.35 .36 .37 .38
.40 .41 .42 .43	-1.48809524 -1.43552243 -1.38572482 -1.33850263 -1.29367445	3.00000000 2.93902439 2.88095238 2.82558140 2.77272727	-3.42857142 -3.41843972 -3.40845070 -3.39860140 -3.38888889	1.91666667 1.91493776 1.91322314 1.91152263 1.90983607	.2000 .2008 .2017 .2025 .2033	.40 .41 .42 .43
.45 .46 .47 .48 .49	-1.25107514 -1.21055409 -1.17197366 -1.13520779 -1.10014087	2.7222222 2.67391304 2.62765957 2.58333333 2.54081633	-3.37931034 -3.36986301 -3.36054422 -3.35135135 -3.34228188	1.90816327 1.90650407 1.90485830 1.90322581 1.90160643	.2042 .2050 .2058 .2067 .2075	.45 .46 .47 .48 .49
.50 .51 .52 .53	-1.06666667 -1.03468738 -1.00411285 974859827 946851341	2.50000000 2.46078431 2.42307692 2.38679245 2.35185185	-3.3333333 -3.32450331 -3.31578947 -3.30718954 -3.29870130	1.90000000 1.89840637 1.89682540 1.89525692 1.89370079	.2083 .2092 .2100 .2108 .2117	.50 .51 .52 .53 .54
.55 .56 .57 .58	920016100 894288004 869605673 845912045 823154005	2.31818182 2.28571429 2.25438596 2.22413793 2.19491525	-3.29032258 -3.28205128 -3.27388535 -3.26582278 -3.25786164	1.89215686 1.89062500 1.88910506 1.88759690 1.88610039	.2125 .2133 .2142 .2150 .2158	.55 .56 .57 .58 .59
.60 .61 .62 .63	801282051 780250000 760014714 740535859 721775684	2.16666667 2.13934426 2.11290323 2.08730159 2.06250000	-3.25000000 -3.24223602 -3.23456790 -3.22699387 -3.21951219	1.88461538 1.88314176 1.88167939 1.88022814 1.87878788	.2167 .2175 .2183 .2192 .2200	.60 .61 .62 .63
.65 .66 .67 .68	703698817 686272088 669464358 653246373 637590622	2.03846154 2.01515152 1.99253731 1.97058824 1.94927536	-3.21212121 -3.20481928 -3.19760479 -3.19047619 -3.18343195	1.87735849 1.87593985 1.87453184 1.87313433 1.87174721	.2208 .2217 .2225 .2233 .2242	.65 .66 .67 .68
	- 1C0	- 1 C0	- 1C0	- 1C0	$-\frac{\frac{1}{3}E^{0}}{b^{3}f^{(4)}(z)}$	p= <u>c c</u> b a

			=0			
r= <u>a_a</u> b c	1°C3	1C3	1C3 3C2	1 C3 3 C3	$\frac{\frac{1}{3}E^{3}}{b^{3}f^{(4)}(z)}$	
0.70 .71 .72 .73	-0.622471211 607863751 593745250 580094016 566889568	1.92857143 1.90845070 1.8888889 1.86986301 1.85135135	-3.17647059 -3.16959064 -3.16279070 -3.15606936 -3.14942529	1.87037037 1.86900369 1.86764706 1.86630037 1.86496356	0.2250 .2258 .2267 .2275 .2283	0.70 .71 .72 .73
.75 .76 .77 .78 .79	554112554 541744678 529768626 518168007 506927288	1.83333333 1.81578947 1.79870130 1.78205128 1.76582278	-3.14285714 -3.13636364 -3.12994350 -3.12359550 -3.11731844	1.86363636 1.86231884 1.86101083 1.85971223 1.85842294	.2292 .2300 .2308 .2317 .2325	.75 .76 .77 .78
.80 .81 .82 .83	496031746 485467412 475221025 465279993 455632345	1.75000000 1.73456790 1.71951220 1.70481928 1.69047619	-3.1111111 -3.10497238 -3.09890110 -3.09289617 -3.08695652	1.85714286 1.85587189 1.85460993 1.85335689 1.85211268	.2333 .2342 .2350 .2358 .2367	.80 .81 .82 .83
.85 .86 .87 .88	446266700 437172230 428338627 419756071 411415209	1.67647059 1.66279070 1.64942529 1.63636364 1.62359551	-3.08108108 -3.07526882 -3.06951872 -3.06382979 -3.05820106	1.85087719 1.84965035 1.84843206 1.84722222 1.84602076	.2375 .2383 .2392 .2400 .2408	.85 .86 .87 .88
.90 .91 .92 .93	403307118 395423292 387755608 380296315 373038007	1.6111111 1.59890110 1.58695652 1.57526882 1.56382979	-3.05263158 -3.04712042 -3.04166667 -3.03626943 -3.03092783	1.84482759 1.84364261 1.84246575 1.84129693 1.84013605	.2417 .2425 .2433 .2442 .2450	.90 .91 .92 .93
.95 .96 .97 .98	365973604 359096341 352399745 345877623 339524045	1.55263158 1.54166667 1.53092784 1.52040816 1.51010101	-3.02564103 -3.02040816 -3.01522843 -3.01010101 -3.00502513	1.83898305 1.83783784 1.83670034 1.83557047 1.83444816	.2458 .2467 .2475 .2483 .2492	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	333333333 327300048 321418975 315685115 310093673	1.50000000 1.49009901 1.48039216 1.47087379 1.46153846	-3.00000000 -2.99502488 -2.99009901 -2.98522167 -2.98039216	1.83333333 1.83222591 1.83112583 1.83003300 1.82894737	.2500 .2508 .2517 .2525 .2533	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	304640049 299319826 294128763 289062789 284117989	1.45238095 1.44339623 1.43457944 1.42592593 1.41743119	-2.97560976 -2.97087379 -2.96618357 -2.96153846 -2.95693780	1.82786885 1.82679739 1.82573290 1.82467532 1.82362460	.2542 .2550 .2558 .2567 .2575	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	279290602 274577011 269973737 265477434 261084881	1.40909091 1.40090090 1.39285714 1.38495575 1.37719298	-2.95238095 -2.94786730 -2.94339623 -2.93896714 -2.93457944	1.82258065 1.82154341 1.82051282 1.81948882 1.81847134	.2583 .2592 .2600 .2608 .2617	1.10 1.11 1.12 1.13
1.15 1.16 1.17 1.18 1.19.	256792977 252598736 248499282 244491843 240573749	1.36956522 1.36206897 1.35470085 1.34745763 1.34033613	-2.93023256 -2.92592593 -2.92165899 -2.91743119 -2.91324201	1.81746032 1.81645570 1.81545741 1.81446541 1.81347962	.2625 .2633 .2642 .2650 .2658	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	236742424 232995385 229330236 225744667 222236445	1.33333333 1.32644628 1.31967213 1.31300813 1.30645161	-2.90909091 -2.90497738 -2.90090090 -2.89686099 -2.89285714	1.81250000 1.81152648 1.81055901 1.80959752 1.80864198	.2667 .2675 .2683 .2692 .2700	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	218803419 215443508 212154704 208935066 205782721	1.3000000 1.29365079 1.28740157 1.28125000 1.27519380	-2.88888889 -2.88495575 -2.88105727 -2.87719298 -2.87336245	1.80769231 1.80674847 1.80581040 1.80487805 1.80395137	.2708 .2717 .2725 .2733 .2742	1.25 1.26 1.27 1.28 1.29
	- ½C <sub>3</sub>	- 1C0	- ½C0	- 1C0 3C0	$-\frac{\frac{1}{3}E^0}{b^3f^{(4)}(\varepsilon)}$	p <u>c_c</u> b a

$(D^2y)_{x=x_1} = \frac{1}{b^2}$	$\sum_{i=0}^{3} {}_{3}^{2}C_{i}^{i}$	yj +	2R i	( i	= 0,3)
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		, p. 1=0	•			
aa r= b= c	<sup>2</sup> C <sup>0</sup> <sub>3</sub>	<sup>2</sup> C <sup>0</sup>	<sup>2</sup> <sub>3</sub> C <sub>2</sub> <sup>0</sup>	<sup>2</sup> C <sup>0</sup> 3 3	$\frac{{}_{3}^{2}E^{0}}{b^{2}f^{(4)}(z)}$	
0.10 .11 .12 .13	28.5714286 25.8509263 23.5849057 21.6684724 20.0267023	-32.0000000 -29.2727273 -27.0000000 -25.0769231 -23.4285714	4.00000000 4.00000000 4.00000000 4.00000000	-0.571428571 578199052 584905660 591549296 598130841	0.2192 .2247 .2303 .2359 .2416	0.10 .11 .12 .13 .14
.15 .16 .17 .18	18.6046512 17.3611111 16.2645703 15.2905199 14.4196107	-22.0000000 -20.7500000 -19.6470588 -18.6666667 -17.7894737	4.00000000 4.00000000 4.00000000 4.00000000	604651163 611111111 617511521 623853211 630136986	.2473 .2531 .2589 .2648 .2707	.15 .16 .17 .18
.20 .21 .22 .23	13.6363636 12.9282482 12.2850123 11.6981868 11.1607143	-17.0000000 -16.2857143 -15.6363636 -15.0434783 -14.5000000	4.00000000 4.00000000 4.00000000 4.00000000	636363636 642533957 648648649 654708520 660714286	.2767 .2827 .2888 .2949 .3011	.20 .21 .22 .23 .24
.25 .26 .27 .28 .29	10.6666667 10.2110279 9.78952521 9.39849624 9.03478392	-14.0000000 -13.5384615 -13.1111111 -12.7142857 -12.3448276	4.00000000 4.00000000 4.00000000 4.00000000	66666667 672566372 678414097 684210526 689956332	.3073 .3136 .3199 .3263 .3327	.25 .26 .27 .28 .29
.30 .31 .32 .33	8.69565217 8.37871806 8.08189655 7.80335544 7.54147813	-12.0000000 -11.6774194 -11.3750000 -11.0909091 -10.8235294	4.0000000 4.0000000 4.0000000 4.0000000 4.0000000	695652174 701298701 706896552 712446352 717948718	.3392 .3457 .3523 .3589 .3656	.30 .31 .32 .33 .34
.35 .36 .37 .38	7.29483283 7.06214689 6.84228532 6.63423264 6.43707757	-10.5714286 -10.3333333 -10.1081081 - 9.89473684 - 9.69230769	4.00000000 4.00000000 4.00000000 4.00000000	723404255 728813559 734177215 739495798 744769874	.3723 .3791 .3859 .3928 .3997	.35 .36 .37 .38
.40 .41 .42 .43	6.25000000 6.07225989 5.90318772 5.74217628 5.58867362	- 9.50000000 - 9.31707317 - 9.14285714 - 8.97674419 - 8.81818182	4.00000000 4.0000000 4.0000000 4.0000000 4.0000000	750000000 755186722 760330579 765432099 770491803	.4067 .4137 .4208 .4279 .4351	.40 .41 .42 .43
.45 .46 .47 .48	5.44217687 5.30222694 5.16840382 5.04032258 4.91762970	- 8.66666667 - 8.52173913 - 8.38297872 - 8.25000000 - 8.12244898	4.00000000 4.0000000 4.0000000 4.0000000 4.0000000	775510204 780487805 785425101 790322581 795180723	.4423 .4496 .4569 .4643 .4717	.45 .46 .47 .48 .49
.50 .51 .52 .53	4.80000000 4.68713382 4.57875458 4.47460661 4.37445319	- 8.00000000 - 7.88235294 - 7.76923077 - 7.66037736 - 7.5555556	4.00000000 4.0000000 4.0000000 4.0000000 4.0000000	800000000 804780877 809523809 814229249 818897638	.4792 .4867 .4943 .5019	.50 .51 .52 .53
.55 .56 .57 .58	4.27807487 4.18526786 4.09584272 4.00962310 3.92644460	- 7.45454545 - 7.35714286 - 7.26315789 - 7.17241379 - 7.08474576	4.00000000 4.00000000 4.0000000 4.0000000 4.0000000	823529412 828125000 832684825 837209302 841698842	.5173 .5251 .5329 .5408 .5487	.55 .56 .57 .58
.60 .61 .62 .63	3.84615385 3.76860750 3.69367151 3.62122035 3.55113636	- 7.00000000 - 6.91803279 - 6.83870968 - 6.76190476 - 6.68750000	4.00000000 4.00000000 4.00000000 4.00000000	846153846 850574713 854961832 859315589 863636364	.5567 .5647 .5728 .5809 .5891	.60 .61 .62 .63
.65 .66 .67 .68	3.48330914 3.41763500 3.35401643 3.29236172 3.23258445	- 6.61538462 - 6.54545455 - 6.47761194 - 6.41176471 - 6.34782609	4.00000000 4.00000000 4.00000000 4.00000000	867924528 872180451 876404494 880597015 884758364	.5971 .6056 .6139 .6223 .6307	.65 .66 .67 .68
	<sup>2</sup> <sub>3</sub> C <sub>3</sub> <sup>3</sup>	<sup>2</sup> C <sup>3</sup> 3 <sup>2</sup>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sub>3</sub> <sup>3</sup>	$\frac{{}^{2}_{3}E^{3}}{{b}^{2}f^{(4)}(E)}$	p= <u>c c</u> b a

$$(D^2y)_{x-X_{\dot{1}}} = \frac{1}{b^2} \sum_{j=0}^{3} {}_{3}^{2}C_{\dot{j}}^{\dot{1}} y_{\dot{j}} + {}_{3}^{2}R^{\dot{1}}$$
 (i-0.3)



r= <u>a_a</u>	200	200	200	200	2E0	
b c	<sup>2</sup> <sub>3</sub> C <sub>0</sub> <sup>0</sup>	2 C0	<sup>2</sup> <sub>3</sub> C <sub>2</sub>	<sup>2</sup> <sub>3</sub> C <sup>0</sup> <sub>3</sub>	b <sup>2</sup> f <sup>(4)</sup> (E)	
0.70 .71 .72 .73 .74	3.17460317 3.11834104 3.06372549 3.01068794 2.95916354	- 6.28571429 - 6.22535211 - 6.16666667 - 6.10958904 - 6.05405405	4.00000000 4.00000000 4.00000000 4.00000000	-0.888888889 892988930 897058824 901098901 905109489	0.6392 .6477 .6563 .6649 .6736	0.70 .71 .72 .73
.75 .76 .77 .78 .79	2.90909091 2.86041190 2.81307141 2.76701716 2.72219954	- 6.00000000 - 5.94736842 - 5.89610390 - 5.84615385 - 5.79746835	4.00000000 4.00000000 4.00000000 4.00000000	909090909 913043478 916967509 920863309 924731183	.6823 .6911 .6999 .7088	.75 .76 .77 .78
.80 .81 .82 .83	2.67857143 2.63608804 2.59470680 2.55438716 2.51509054	- 5.75000000 - 5.70370370 - 5.65853659 - 5.61445783 - 5.57142857	4.00000000 4.00000000 4.00000000 4.00000000	928571429 932384342 936170213 939929328 943661972	.7267 .7357 .7448 .7539 .7631	.80 .81 .82 .83
.85 .86 .87 .88	2.47678019 2.43942104 2.40297970 2.36742424 2.33272423	- 5.52941176 - 5.48837209 - 5.44827586 - 5.40909091 - 5.37078652	4.00000000 4.00000000 4.00000000 4.00000000	947368421 951048951 954703833 958333333 961937716	.7723 .7816 .7909 .8003 .8097	.85 .86 .87 .88
.90 .91 .92 .93	2.29885057 2.26577546 2.23347230 2.20191567 2.17108120	- 5.33333333 - 5.29670330 - 5.26086957 - 5.22580645 - 5.19148936	4.00000000 4.00000000 4.00000000 4.00000000	965517241 969072165 972602740 976109215 979591837	.8192 .8287 .8383 .8479 .8576	.90 .91 .92 .93
.95 .96 .97 .98	2.14094558 2.11145649 2.08268250, 2.05451308 2.02695855	- 5.15789474 - 5.12500000 - 5.09278351 - 5.06122449 - 5.03030303	4.00000000 4.00000000 4.00000000 4.00000000	983050847 986486486 989898990 993288591 996655518	.8673 .8771 .8869 .8968	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	2.00000000 1.97361929 1.94779899 1.92252235 1.89777328	- 5.00000000 - 4.97029703 - 4.94117647 - 4.91262136 - 4.88461538	4.00000000 4.00000000 4.00000000 4.00000000	-1.00000000 -1.00332226 -1.00662252 -1.00990099 -1.01315790	.9167 .9267 .9363 .9469	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	1.87353630 1.84979652 1.82653962 1.80375180 1.78141979	- 4.85714286 - 4.83018868 - 4.80373832 - 4.7777778 - 4.75229358	4.00000000 4.00000000 4.00000000 4.00000000	-1.01639344 -1.01960784 -1.02280130 -1.02597403 -1.02912621	.9673 .9776 .9879 .9983 1.0087	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	1.75953079 1.73807248 1.71703297 1.69640080 1.67616493	- 4.72727273 - 4.70270270 - 4.67857143 - 4.65486726 - 4.63157895	4.00000000 4.00000000 4.00000000 4.00000000	-1.03225807 -1.03536978 -1.03846154 -1.04153355 -1.04458599	1.0192 1.0297 1.0403 1.0509 1.0616	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	1.65631470 1.63683981 1.61773032 1.59897665 1.58056953	- 4.60869565 - 4.58620690 - 4.56410256 - 4.54237288 - 4.52100840	4.00000000 4.00000000 4.00000000 4.00000000	-1.04761905 -1.05063291 -1.05362776 -1.05660377 -1.05956113	1.0723 1.0831 1.0939 1.1048 1.1157	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	1.56250000 1.54475940 1.52733937 1.51023182 1.49342891	- 4.50000000 - 4.47933884 - 4.45901639 - 4.43902439 - 4.41935484	4.00000000 4.00000000 4.00000000 4.00000000	-1.06250000 -1.06542056 -1.06832298 -1.07120743 -1.07407407	1.1267 1.1377 1.1488 1.1599 1.1711	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	1.47692308 1.46070698 1.44477353 1.42911585 1.41372729	- 4.40000000 - 4.38095238 - 4.36220472 - 4.34375000 - 4.32558140	4.00000000 4.00000000 4.00000000 4.00000000	-1.07692308 -1.07975460 -1.08256881 -1.08536585 -1.08814590	1.1823 1.1936 1.2049 1.2163 1.2277	1.25 1.26 1.27 1.28 1.29
	<sup>2</sup> C <sup>3</sup> 3 3	2C3 3C2	2C <sup>3</sup> 3 1	<sup>2</sup> C <sup>3</sup> <sub>3</sub>	2E <sup>3</sup> b <sup>2</sup> f <sup>(4)</sup> (ξ)	p= <u>C=C</u> b a

$(D^2y)_{x=x_1} = \frac{1}{b^2} \sum_{j=0}^{3} {}_{3}^{2}C_{j}^{1} y_{j} +$	2 <sub>3</sub> R <sup>1</sup>	(i = 1,2)	)
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		x=x1 b <sup>2</sup> / <sub>j=0</sub> 3 J			June	m
r=aa b=c	<sup>2</sup> C 1 3	<sup>2</sup> C <sup>1</sup>	<sup>2</sup> C <sub>2</sub> <sup>1</sup>	<sup>2</sup> C <sup>1</sup> <sub>3</sub>	$\frac{{}^{2}_{3}E^{1}}{{}^{2}f^{(4)}(z)}$	
0.10 .11 .12 .13	25.9740260 23.2891228 21.0579515 19.1756393 17.5672827	-29.0000000 -26.2727273 -24.0000000 -22.0769231 -20.4285714	3.45454545 3.40540541 3.35714286 3.30973451 3.26315789	-0.428571429 421800948 415094340 408450704 401869159	0.1417 .1392 .1367 .1342 .1317	0.10 .11 .12 .13
.15 .16 .17 .18	16.1779575 14.9664751 13.9013422 12.9580677 12.1173199	-19.0000000 -17.7500000 -16.6470588 -15.6666667 -14.7894737	3.21739130 3.17241379 3.12820513 3.08474576 3.04201681	395348837 388888889 382488479 376146789 369863014	.1292 .1267 .1242 .1217 .1192	.15 .16 .17 .18
.20 .21 .22 .23	11.3636364 10.6845027 10.0696822 9.51072096 9.00057603	-14.0000000 -13.2857143 -12.6363636 -12.0434783 -11.5000000	3.00000000 2.95867769 2.91803279 2.87804878 2.83870968	363636364 357466063 351351351 345291480 339285714	.1167 .1142 .1117 .1092 .1067	.20 .21 .22 .23
.25 .26 .27 .28	8.53333332 8.10399039 7.70828757 7.34257518 7.00370847	-11.0000000 -10.5384615 -10.1111111 - 9.71428571 - 9.34482759	2.80000000 2.76190476 2.72440945 2.68750000 2.65116279	333333333 327433628 321585903 315789474 310043668	.1042 .1017 .0992 .0967 .0942	.25 .26 .27 .28
.30 .31 .32 .33	6.68896320 6.39596799 6.12264891 5.86718454 5.62796874	- 9.00000000 - 8.67741935 - 8.37500000 - 8.09090909 - 7.82352941	2.61538462 2.58015267 2.54545455 2.51127820 2.47761194	304347826 298701299 293103448 287553648 282051282	.0917 .0892 .0867 .0842 .0817	.30 .31 .32 .33
.35 .36 .37 .38 .39	5.40357987 5.19275508 4.99436886 4.80741495 4.63099107	- 7.57142857 - 7.33333333 - 7.10810811 - 6.89473684 - 6.69230769	2.4444444 2.41176470 2.37956204 2.34782609 2.31654676	276595745 271186441 265822785 260504202 255230126	.0792 .0767 .0742 .0717 .0692	.35 .36 .37 .38
.40 .41 .42 .43	4.46428572 4.30656729 4.15717446 4.01550789 3.88102336	- 6.50000000 - 6.31707317 - 6.14285714 - 5.97674419 - 5.81818182	2.28571429 2.25531915 2.22535211 2.19580420 2.16666667	250000000 244813278 239669421 234567901 229508197	.0667 .0642 .0617 .0592 .0567	.40 .41 .42 .43
.45 .46 .47 .48	3.75322543 3.63166228 3.51592097 3.40562337 3.30042262	- 5.66666667 - 5.52173913 - 5.38297872 - 5.25000000 - 5.12244898	2.13793103 2.10958904 2.08163265 2.05405405 2.02684564	224489796 219512195 214574899 209677419 204819277	.0542 .0517 .0492 .0467 .0442	.45 .46 .47 .48
.50 .51 .52 .53	3.20000000 3.10406213 3.01233854 2.92457948 2.84055402	- 5.00000000 - 4.88235294 - 4.76923077 - 4.66037736 - 4.55555556	2.00000000 1.97350993 1.94736842 1.92156863 1.89610390	200000000 195219124 190476190 185770751 181102362	.0417 .0392 .0367 .0342 .0317	.50 .51 .52 .53
.55 .56 .57 .58 .59	2.76004830 2.68286401 2.60881702 2.53773614 2.46946202	- 4.45454545 - 4.35714286 - 4.26315789 - 4.17241379 - 4.08474576	1.87096774 1.84615385 1.82165605 1.79746835 1.77358491	176470588 171875000 167315175 162790698 158301158	.0292 .0267 .0242 .0217 .0192	.55 .56 .57 .58
.60 .61 .62 .63	2.40384615 2.34075000 2.28004414 2.22160758 2.16532704	- 4.0000000 - 3.91803279 - 3.83870968 - 3.76190476 - 3.68750000	1.75000000 1.72670807 1.70370370 1.68098160 1.65853659	153846154 149425287 145038168 140684411 136363636	.0167 .0142 .0117 .0092 .0067	.60 .61 .62 .63
.65 .66 .67 .68	2.11109646 2.05881627 2.00839308 1.95973911 1.91277186	- 3.61538462 - 3.54545455 - 3.47761194 - 3.41176471 - 3.34782609	1.63636364 1.61445783 1.59281437 1.57142857 1.55029586	132075472 127819549 123595506 119402985 115241636	.0042 .0017 0008 0033 0058	.65 .67 .68
	<sup>2</sup> <sub>3</sub> C <sup>2</sup> <sub>3</sub>	<sup>2</sup> C <sup>2</sup> <sub>3</sub> C <sup>2</sup>	<sup>2</sup> C <sup>2</sup> <sub>3</sub>	2C2 3C0	$\frac{\frac{{}_{3}^{2}E^{2}}{{}_{5}^{2}f^{(4)}(\xi)}$	p= C = b = i

1.25 1.26 1.27 1.28 1.29

.656410257 .646330524 .636464112 .626805198

.617348163

2 C2

- 1.40000000 - 1.38095238 - 1.36220472 - 1.34375000 - 1.32558140

2C2

- .1458 - .1483 - .1508 - .1533 - .1558

 $\frac{{}_{3}^{2}E^{2}}{{}_{5}^{2}f^{(4)}(\xi)}$ 

.0769230769 .0797546012 .0825688073

.0853658537 .0881458967

 ${}^{2}_{3}C^{2}_{0}$ 

1.25 1.26 1.27 1.28 1.29

 $p = \frac{c}{h} = \frac{c}{a}$ 

#### FOUR-POINT DIFFERENTIATION COEFFICIENTS

	(D <sup>2</sup> )	$(y)_{x=x_i} = \frac{1}{b^2} \sum_{j=0}^{3} {}_{3}^{2}C_j^i y_j$	$1 + \frac{2}{3}R^{i}$ (i = 1,	,2)	NAC	ممرم
r=aa b=c	<sup>2</sup> C 1 3 C 0	2C1	<sup>2</sup> C <sup>1</sup> <sub>3</sub> C <sup>2</sup>	<sup>2</sup> C <sup>1</sup> <sub>3</sub>	$\frac{{}^{2}E^{1}}{{b}^{2}f^{(4)}(\xi)}$	
0.70 .71 .72 .73	1.86741363 1.82359125 1.78123575 1.74028206 1.70066871	- 3.28571429 - 3.22535211 - 3.16666667 - 3.10958904 - 3.05405405	1.52941176 1.50877193 1.48837209 1.46820809 1.44827586	-0.11111111 107011070 102941176 098901099 094890511	-0.0083 0108 0133 0158 0183	0.7 .7 .7 .7
.75 .76 .77 .78	1.66233765 1.62523404 1.58930589 1.55450403 1.52078187	- 3.00000000 - 2.94736842 - 2.89610390 - 2.84615385 - 2.79746835	1.42857143 1.40909091 1.38983051 1.37078652 1.35195531	090909091 086956522 083032491 079136691 075268817	0208 0233 0258 0283 0308	•7 •7 •7
.80 .81 .82 .83	1.48809524 1.45640223 1.42566308 1.39583998 1.36689703	- 2.75000000 - 2.70370370 - 2.65853659 - 2.61445783 - 2.57142857	1.33333333 1.31491713 1.29670330 1.27868852 1.26086957	0714285714 0676156584 0638297872 0600706714 0563380282	0333 0358 0383 0408 0433	.6 .6 .6
.85 .86 .87 .88	1.33880010 1.31151669 1:28501588 1.25926821 1.23424563	- 2.52941176 - 2.48837209 - 2.44827586 - 2.40909091 - 2.37078652	1.24324324 1.22580645 1.20855615 1.19148936 1.17460317	0526315790 0489510489 0452961673 0416666667 0380622837	0458 0483 0510 0533 0558	. 8 . 8 . 8 . 8
.90 .91 .92 .93	1.20992136 1.18626988 1.16326683 1.14088895 1.11911402	- 2.33333333 - 2.29670330 - 2.26086957 - 2.22580645 - 2.19148936	1.15789474 1.14136126 1.12500000 1.10880829 1.09278351	0344827586 0309278350 0273972603 0238907850 0204081633	0583 0608 0633 0658 0683	.!
.95 .96 .97 .98	1.09792081 1.07728902 1.05719924 1.03763287 1.01857214	- 2.15789474 - 2.12500000 - 2.09278351 - 2.06122449 - 2.03030303	1.07692308 1.06122449 1.04568528 1.03030303 1.01507538	0169491525 0135135135 0101010101 00671140940 00334448161	0708 0733 0758 0783 0808	• •
1.00 1.01 1.02 1.03 1.04	1.00000000 .981900144 .964256925 .947055345 .930281019	- 2.00000000 - 1.97029703 - 1.94117647 - 1.91262136 - 1.88461538	1.00000000 .985074627 .970297030 .955665025 .941176471	0 .00332225914 .00662251656 .0099099010 .0131578947	0833 0858 0883 0908 0933	1.
1.05 1.06 1.07 1.08	.913920147 .897959478 .882386289 .867188367 .852353967	- 1.85714286 - 1.83018868 - 1.80373832 - 1.7777778 - 1.75229358	.926829268 .912621359 .898550725 .884615385 .870813397	.0163934426 .0196078431 .0228013029 .0259740260 .0291262136	0958 0983 1008 1033 1058	1. 1. 1.
1.10 1.11 1.12 1.13 1.14	.837871806 .823731033 .809921211 .796432302 .783254643	- 1.72727273 - 1.70270270 - 1:67857143 - 1.65486726 - 1.63157895	.857142857 .843601896 .830188679 .816901408 .803738318	.0322580645 .0353697749 .038461.5385 .0415335463 .0445859873	1083 1108 1133 1158 1183	1.
1.15 1.16 1.17 1.18 1.19	.770378931 .757796208 .745497846 .733475529 .721721247	- 1.60869565 - 1.58620690 - 1.56410256 - 1.54237288 - 1.52100840	.790697674 .777777778 .764976959 .752293578 .739726027	.0476190476 .0506329114 .0536277603 .0566037736 .0595611285	1208 1233 1258 1283 1308	1.
1.20 1.21 1.22 1.23 1.24	.710227272 .698986155 .687990708 .677234001 .666709335	- 1.50000000 - 1.47933884 - 1.45901639 - 1.43902439 1.41935484	.727272727 .714932127 .702702703 .690582960 .678571429	.0625000000 .0654205607 .0683229814 .0712074303 .0740740741	1333 1358 1383 1408 1433	1. 1. 1.

.666666667 .654867257 .643171806 .631578947 .620087336

 ${}_3^2C_1^2$ 

For any value of  $r = \frac{a}{b} = \frac{a}{c}$ 

$$(D^2y)_{x-x_2} = \frac{y_1-2y_2+y_3}{b^2} + \frac{2}{3}R^2$$

where

$${}_{3}^{2}R^{2}=-\frac{b^{2}}{12}f^{(4)}(\xi)+...$$

For any value of  $p = \frac{c}{b} = \frac{c}{a}$ 

$$(D^2y)_{x=x_1} = \frac{y_0-2y_1+y_2}{b^2} + \frac{2}{3}R^1$$

where

$$\frac{2}{3}R^{1} = -\frac{b^{2}}{12} f^{(4)}(\xi) + ...$$

NACA

$(D^2y)_{x=x} = \frac{1}{b^2}$	$\sum_{j=0}^{3} \ _{3}^{2}C_{j}^{i} \ y_{j} \ + \ _{3}^{2}R^{i}$	(i=3,0)	NACA
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_						
r=a_a b c	<sup>2</sup> C <sup>3</sup> <sub>3</sub>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup> <sub>3</sub>	2C3 3C3	$\frac{{}^{2}E^{3}}{{}^{2}f^{(4)}(E)}$	
0.10 .11 .12 .13 .14	-25.9740260 -23.2891228 -21.0579515 -19.1756393 -17.5672827	31.0000000 28.2727273 26.0000000 24.0769231 22.4285714	-7.45454545 -7.40540541 -7.35714286 -7.30973451 -7.26315789	2.42857143 2.42180095 2.41509434 2.40845070 2.40186916	0.6917 .6942 .6967 .6992 .7017	0.10 .11 .12 .13 .14
.15 .16 .17 .18	-16.1779575 -14.9664751 -13.9013422 -12.9580677 -12.1173199	21.0000000 19.7500000 18.6470588 17.6666667 16.7894737	-7.21739130 -7.17241379 -7.12820513 -7.08474576 -7.04201681	2.39534884 2.38888889 2.38248848 2.37614679 2.36986301	.7042 .7067 .7092 .7117 .7142	.15 .16 .17 .18 .19
.20 .21 .22 .23 .24	-11.3636364 -10.6845027 -10.0696822 - 9.51072096 - 9.00057603	16.0000000 15.2857143 14.6363636 14.0434783 13.5000000	-7.00000000 -6.95867769 -6.91803279 -6.87804878 -6.83870968	2.36363636 2.35746606 2.35135135 2.34529148 2.33928571	.7167 .7192 .7217 .7242 .7267	.20 .21 .22 .23 .24
.25 .26 .27 .28 .29	- 8.53333332 - 8.10399039 - 7.70828757 - 7.34257518 - 7.00370847	13.0000000 12.5384615 12.1111111 11.7142857 11.3448276	-6.80000000 -6.76190476 -6.72440945 -6.68750000 -6.65116279	2.33333333 2.32743363 2.32158590 2.31578947 2.31004367	.7292 .7317 .7342 .7367 .7392	.25 .26 .27 .28 .29
.30 .31 .32 .33	- 6.68896320 - 6.39596799 - 6.12264891 - 5.86718454 - 5.62796874	11.0000000 10.6774194 10.3750000 10.0909091 9.82352941	-6.61538462 -6.58015267 -6.54545455 -6.51127820 -6.47761194	2.30434783 2.29870130 2.29310345 2.28755365 2.28205128	.7417 .7442 .7467 .7492 .7517	.30 .31 .32 .33
.35 .36 .37 .38 .39	- 5.40357987 - 5.19275508 - 4.99436886 - 4.80741495 - 4.63099107	9.57142857 9.33333333 9.10810811 8.89473684 8.69230769	-6.4444444 -6.41176470 -6.37956204 -6.34782609 -6.31654676	2.27659574 2.27118644 2.26582278 2.26050420 2.25523013	.7542 .7567 .7592 .7617 .7642	.35 .36 .37 .38
.40 .41 .42 .43	- 4.46428572 - 4.30656729 - 4.15717446 - 4.01550789 - 3.88102336	8.50000000 8.31707317 8.14285714 7.97674419 7.81818182	-6.28571429 -6.25531915 -6.22535211 -6.19580420 -6.16666667	2.25000000 2.24481328 2.23966942 2.23456790 2.22950820	.7667 .7692 .7717 .7742 .7767	.40 .41 .42 .43
.45 .46 .47 .48 .49	- 3.75322543 - 3.63166228 - 3.51592097 - 3.40562337 - 3.30042262	7.66666667 7.52173913 7.38297872 7.25000000 7.12244898	-6.13793103 -6.10958904 -6.08163265 -6.05405405 -6.02684564	2.22448980 2.21951220 2.21457490 2.20967742 2.20481928	.7792 .7817 .7842 .7867 .7892	.45 .46 .47 .48
.50 6 .51 .52 .53	- 3.20000000 - 3.10406213 - 3.01233854 - 2.92457948 - 2.84055402	7.00000000 6.88235294 6.76923077 6.66037736 6.5555556	-6.00000000 -5.97350993 -5.94736842 -5.92156863 -5.89610390	2.20000000 2.19521912 2.19047619 2.18577075 2.18110236	.7917 .7942 .7967 .7992 .8017	.50 .51 .52 .53
.55 .56 .57 .58	- 2.76004830 - 2.68286401 - 2.60881702 - 2.53773614 - 2.46946202	6.45454545 6.35714286 6.26315789 6.17241379 6.08474576	-5.87096774 -5.84615385 -5.82165605 -5.79746835 -5.77358491	2.17647059 2.17187500 2.16731518 2.16279070 2.15830116	.8042 .8067 .8092 .8117 .8142	.55 .56 .57 .58
.60 .61 .62 .63	- 2.40384615 - 2.34075000 - 2.28004414 - 2.22160758 - 2.16532704	6.00000000 5.91803279 5.83870968 5.76190476 5.68750000	-5.75000000 -5.72670807 -5.70370370 -5.68098160 -5.65853689	2.15384615 2.14942529 2.14503817 2.14068441 2.13636364	.8167 .8192 .8217 .8242 .8267	.60 .61 .62 .63
.65 .66 .67 .68	- 2.11109646 - 2.05881627 - 2.00839308 - 1.95973911 - 1.91277186	5.61538462 5.54545455 5.47761194 5.41176471 5.34782609	-5.63636364 -5.61445783 -5.59281437 -5.57142857 -5.55029586	2.13207547 2.12781955 2.12359551 2.11940299 2.11524164	.8292 .8317 .8342 .8367 .8392	.65 .66 .67 .68
	<sup>2</sup> C <sub>3</sub> <sup>0</sup>	<sup>2</sup> C <sup>0</sup> <sub>3</sub>	2C0 3 i	<sup>2</sup> C <sup>0</sup> <sub>3</sub>	b <sup>2</sup> f <sup>(4)</sup> (E)	p <u>c</u> c ba

 $(D^2y)_{x\rightarrow x} \frac{1}{1} \frac{1}{b^2} \sum_{j=0}^{3} {}_{3}^{2}C_{j}^{j} y_{j} + {}_{3}^{2}R^{j}$  (i-3,0)



		b <sup>2</sup> j=0				
					2E3	
_a_a	203	203	2 C3	2 C3		
r==== b c	<sup>2</sup> <sub>3</sub> C <sub>0</sub> <sup>3</sup>	<sup>2</sup> C <sup>3</sup>	3 2	3 3	b <sup>2</sup> f <sup>(4)</sup> (E)	1
	3 00043505	5 005m1400	E 50043176	9 11111111	0.8417	0.70
.70	- 1.86741363	5.28571429	-5.52941176	2.11111111	.8442	.71
.71	- 1.82359125	5.22535211	-5.50877193	2.10294118	.8467	.72
.72	- 1.78123575	5.16666667	-5.48837209	2.09890110	.8492	.73
.73 .74	- 1.74028206 - 1.70066871	5.10958904 5.05405405	-5.46820809 -5.44827586	2.09489051	.8517	.74
• / 3	- 1,,000,0071	0.00100100				
•75	- 1.66233765	5.00000000 4.94736842	-5.42857143 -5.40909091	2.09090909 2.08695652	.8542 .8567	.75 .76
•76	- 1.62523404 - 1.58930589	4.89610390	-5.38983051	2.08303249	.8592	.77
•77		4.84615385	-5.37078652	2.07913669	.8617	.78
•78 •79	- 1.55450403 - 1.52078187	4.79746835	-5.35195531	2.07526882	.8642	.79
	3 40000504	4.75000000	-5.33333333	2.07142857	.8667	.80
.80 .81	- 1.48809524 - 1.45640223	4.70370370	-5.31491713	2.06761566	.8692	.81
.82	- 1.42566308	4.65853659	-5.29670330	2.06382979	.8717	.82
.83	- 1.39583998	4.61445783	-5.27868852	2.06007067	.8742	.83
.84	- 1.36689703	4.57142857	-5.26086957	2.05633803	.8767	.84
95	- 1.33880010	4.52941176	-5.24324324	2.05263158	.8792	.85
.85 .86	- 1.31151669	4.48837209	-5.22580645	2.04895105	.8817	.86
.87	- 1.28501588	4.44827586	-5.20855615	2.04529617	.8842	.87
88	- 1.25926821	4.40909091	-5.19148936	2.04166667	•8867	.88
.89	- 1.23424563	4.37078652	-5.17460317	2.03806228	.8892	.89
<b>.9</b> 0	- 1.20992136	4.33333333	-5.15789474	2.03448276	.8917	.90
.91	- 1.18626988	4.29670330	-5.14136126	2.03092784	.8942	.91
.92	- 1.16326683	4.26086957	-5.12500000	2.02739726	.8967	.92
.93	- 1.14088895	4,22580645	-5.10880829	2.02389078	.8992	.93
.94	- 1.11911402	4.19148936	-5.09278351	2.02040816	.9017	.94
95	- 1.09792081	4.15789474	-5.07692308	2.01694915	.9042	.95
96	- 1.07728902	4.12500000	-5.06122449	2.01351351	.9067	.96
97	- 1.05719924	4.09278351	-5.04568528	2.01010101	.9092	.97
.98	- 1.03763287	4.06122449	-5.03030303	2.00671141	.9117	.98
.99	- 1.01857214	4.03030303	-5.01507538	2.00334448	.9142	.99
•00	- 1.00000000	4.00000000	-5.00000000	2.00000000	.9167	1.00
.01	981900144	3.97029703	-4.98507463	1.99667774	.9192	1.01
.02	964256925	3.94117647	-4.97029703	1.99337748	.9217	1.02
.03	947055345	3.91262136	-4.95566502	1.99009901	.9242	1.03
.04	930281019	3.88461538	-4.94117647	1.98684211	.9267	1.04
•05	913920147	3.85714286	-4.92682927	1.98360656	.9292	1.05
•06	897959478	3.83018868	-4.91262136	1.98039216	.9317	1.06
.07	882386289	3.80373832	-4.89855072	1.97719870	.9342	1.07
•08	867188367	3.77777778	-4.88461538	1.97402597	.9367	1.08
•09	852353967	3.75229358	-4.87081340	1.97087379	.9392	1.09
.10	837871806	3.72727273	-4.85714286	1.96774194	.9417	1.10
11	823731033	3.70270270	-4.84360190	1.96463023	.9442	1.11
12	809921211	3.67857143	-4.83018868	1.96153846	.9467	1.12
.13	796432302	3.65486726	-4.81690141	1.95846645	.9492 0517	1.13
.14	783254643	3.63157895	-4.80373832	1.95541401	.9517	1.14
.15	770378931	3.60869565	-4.79069767	1.95238095	.9542	1.15
.16	757796208	3.58620690	-4.77777778	1.94936709	.9567	1.16
.17	745497846	3.56410256	-4.76497696	1.94637224	.9592	1.17
.18	733475529 721721247	3.54237288 3.52100840	-4.75229358 -4.73972603	1.94339623	.9617 .9642	1.18
.19						,
.20	710227272	3.50000000	-4.72727273	1.93750000	•9667 •9692	1.20
.21	698986155	3.47933884	-4.71493213	1.93457944	.9717	1.22
.22	687990708	3.45901639	-4.70270270 -4.69058296	1.93167702	.9742	1.23
.23 .24	677234001 666709335	3.43902439 3.41935484	<b>-4.</b> 69058296 <b>-4.</b> 67857143	1.92592593	.9767	1.24
		3.40000000	-4.66666667	1.92307692	.9792	1.25
.25	656410257		-4.65486726	1.92024540	.9817	1.26
.26	646330524	3.38095238 3.36220472	<b>-4.</b> 64317181	1.91743119	.9842	1.27
	636464112	3.34375000	-4.63157895	1.91463415	.9867	1.28
.27						
.27 .28 .29	626805198 617348163	3.32558140	-4.62008734	1.91185410	.9892	1,29
.27 .28		3.32558140	-4.62008734	1.91185410		
.27 .28		3.32558140 2C0 3 C2	-4.62008734	2C0 3C0	$\frac{{}^{2}E^{0}}{b^{2}f^{(4)}(\xi)}$	p= <u>c=c</u> b a

$(D^3y)_{x=x_1}\frac{1}{b^3}$	$\sum_{j=0}^{3}$	3C j y	j + <sup>3</sup> R <sup>i</sup>	(i=0,i	,2,3)	NA	SA
			3 <sub>E</sub> 0	3 <sub>F</sub> 1	3 <sub>F</sub> 2	3 <sub>F</sub> 3	

			j=0				••••	
				3E0	3E1	3E2	3E3	
3 C <sub>0</sub>	3C	3C1 3C2	3Ci 3C3	bf (4)(E)	bf <sup>(4)</sup> (ξ)	bf (4)	bf (4) (E)	
-25.9740260 -23.2891228 -21.0579515 -19.1756393 -17.5672827	30.0000000 27.2727273 25.0000000 23.0769231 21.4285714	-5.40540541 -5.35714286 -5.30973451	1.42180095 1.41509434 1.40845070	-0.8250 8325 8400 8475 8550	-0.7250 7225 7200 7175 7150	0.2750 .2775 .2800 .2825 .2850	1.2750 1.2775 1.2800 1.2825 1.2850	0.10 .11 .12 .13 .14
-16.1779575 -14.9664751 -13.9013422 -12.9580677 -12.1173199	20.0000000 18.7500000 17.6470588 16.6666667 15.7894737	-5.17241379 -5.12820513 -5.08474576	1.38888889 1.38248848 1.37614679	8625 8700 8775 8850 8925	7125 7130 7075 7050 7025	.2875 .2900 .2925 .2950 .2975	1.2875 1.2900 1.2925 1.2950 1.2975	.15 .16 .17 .18 .19
-11.3636364 -10.6845027 -10.0696822 - 9.51072096 - 9.00057603	15.0000000 14.2857143 13.6363636 13.0434783 12.5000000	-4.95867769 -4.91803279 -4.87804878	1.35746606 1.35135135 1.34529148	9000 9075 9150 9225 9300	7000 6975 6950 6925 6900	.3000 .3025 .3050 .3075 .3100	1.3000 1.3025 1.3050 1.3075 1.3100	.20 .21 .22 .23
- 8.53333332 - 8.10399039 - 7.70828757 - 7.34257518 - 7.00370847	12.0000000 11.5384615 11.1111111 10.7142857 10.3448276	-4.76190476 -4.72440945 -4.68750000	1.32743363 1.32158590 1.31578947	9375 9450 9525 9600 9675	6875 6850 6825 6800 6775	.3125 .3150 .3175 .3200 .3225	1.3125 1.3150 1.3175 1.3200 1.3225	.25 .26 .27 .28 .29
- 6.68896320 - 6.39596799 - 6.12264891 - 5.86718454 - 5.62796874	9,09090909	-4.58015267 -4.54545455 -4.51127820	1.29870130 1.29310345 1.28755365	9750 9825 9900 9975 -1.0050	6750 6725 6700 6675 6650	.3250 .3275 .3300 .3325 .3350	1.3250 1.3275 1.3300 1.3325 1.3350	.30 .31 .32 .33
	8.33333333 8.10810811 7.89473684	-4.41176471 -4.37956204 -4.34782609	1.27118644 1.26582278 1.26050420	-1.0125 -1.0200 -1.0275 -1.0350 -1.0425	6625 6600 6575 6550 6525	.3375 .3400 .3425 .3450	1.3375 1.3400 1.3425 1.3450 1.3475	.35 .36 .37 .38 .39
- 4.46428572 - 4.30656729 - 4.15717446 - 4.01550789 - 3.88102336	7.31707317 7.14285714 6.97674419	-4.25531915 -4.22535211 -4.19580420	1.23456790	-1.0500 -1.0575 -1.0650 -1.0725 -1.0800	6500 6475 6450 6425 6400	.3500 .3525 .3550 .3575 .3600	1.3500 1.3525 1.3550 1.3575 1.3600	.40 .41 .42 .43
- 3.75322543 - 3.63166228 - 3.51592097 - 3.40562337 - 3.30042262	6.52173913 6.38297872 6.25000000	-4.10958904 -4.08163265 -4.05405405	1.22448980 1.21951220 1.21457490 1.20967742 1.20481928	-1.0875 -1.0950 -1.1025 -1.1100 -1.1175	6375 6350 6325 6300 6275	.3625 .3650 .3675 .3700 .3725	1.3625 1.3650 1.3675 1.3700 1.3725	.45 .46 .47 .48
- 3.2000000 - 3.10406213 - 3.01233854 - 2.92457948 - 2.84055402	5.88235294 5.76923077 5.66037736	-3.97350993 -3.94736842 -3.92156863	1.20000000 1.19521912 1.19047619 1.18577075 1.18110236	-1.1250 -1.1325 -1.1400 -1.1475 -1.1550	6250 6225 6200 6175 6150	.3750 .3775 .3800 .3825 .3850	1.3750 1.3775 1.3800 1.3825 1.3850	.50 .51 .52 .53
- 2.76004830 - 2.68286401 - 2.60881702 - 2.53773614 - 2.46946202	5.35714286 5.26315789 5.17241379	-3.84615385 -3.82165605 -3.79746835	1.17187500 1.16731518 1.16279070	-1.1625 -1.1700 -1.1775 -1.1850 -1.1925	6125 6100 6075 6050 6025	.3875 .3900 .3925 .3950 .3975	1.3875 1.3900 1.3925 1.3950 1.3975	.55 .56 .57 .58
- 2.40384615 - 2.34075000 - 2.28004414 - 2.22160758 - 2.16532704	4.91803279 4.83870968 4.76190476	-3.72670807 -3.70370370 -3.68098160	1.14942529 1.14503817 1.14068441	-1.2000 -1.2075 -1.2150 -1.2225 -1.2300	6000 5975 5950 5925 5900	.4000 .4025 .4050 .4075 .4100	1.4000 1.4025 1.4050 1.4075 1.4100	.60 .61 .62 .63
- 2.11109646 - 2.05881627 - 2.00839308 - 1.95973911 - 1.91277186	4.54545455 4.47761194 4.41176471	-3.61445783 -3.59281437 -3.57142857	1.12781955 1.12359551 1.11940299	-1.2375 -1.2450 -1.2525 -1.2600 -1.2675	5875 5850 5825 5800 5775	.4125 .4150 .4175 .4200 .4225	1.4125 1.4150 1.4175 1.4200 1.4225	.65 .66 .67 .68
-3Ci	-3Ci 3C2	-3Ci	-3C0	3E3 bf (4)(E)	3E <sup>2</sup> bf <sup>(4)</sup> (ξ)	bf (4) (E)	- 3E0 hf (4) (5)	p= <u>C C</u> b a
	-25.9740260 -23.2891228 -21.0579515 -19.1756393 -17.5672827 -16.1779575 -14.9664751 -13.9013422 -12.9580677 -12.1173199 -11.3636364 -10.6845027 -10.0696822 -9.51072096 -9.00057603 -8.5333332 -8.10399039 -7.70828757 -7.34257518 -7.00370847 -6.68896320 -6.389596799 -6.12264891 -5.86718454 -5.62796874 -5.40357987 -5.19275508 -4.99436886 -4.80741495 -4.63099107 -4.46428572 -4.15717446 -4.01550789 -3.88102336 -3.75322543 -3.63166228 -3.51592097 -3.40562337 -3.30042262 -3.20000000 -3.10406213 -3.01233854 -2.92457948 -2.84055402 -2.76004830 -2.60881702 -2.40384615 -2.34075000 -2.153773614 -2.2160758 -2.11109646 -2.00839508 -1.95973911 -1.91277186	-25.9740260 -23.2891228 -21.0579515 -19.1756393 -17.5672827 -16.1779575 -14.9664751 -13.9013429 -12.9580677 -12.1173199 -11.3636364 -10.66845027 -10.16845027 -10.66845027 -10.0696822 -10.0696822 -10.0696822 -10.0696822 -10.0696822 -10.0696822 -10.06968230 -8.10399039 -11.5384615 -7.70828757 -7.0370847 -7.0370847 -6.68896320 -6.12264891 -5.40357987 -6.12264891 -5.40357987 -6.12264891 -5.40357987 -7.042875 -7.0428757 -7.0428757 -7.0428757 -7.0428757 -7.0428757 -7.042875 -7.0428757 -7.042875 -7.000000000000000000000000000000000000	-25.9740260 -23.2891228 -21.0579515 -21.0579515 -19.1756393 -17.5672827 -16.1779575 -14.9664751 -13.9013422 -16.6666667 -12.1173199 -15.66666667 -12.1173199 -10.66845027 -10.66845027 -10.66845027 -10.66845027 -10.068622 -10.000000 -4.80000000 -4.80000000 -4.80000000 -4.615384615 -7.70828757 -11.111111 -4.72440945 -7.00370847 -10.3448276 -4.65116279 -6.68896320 -6.39596799 -6.12264891 -5.62796874 -8.82552941 -4.4671825 -4.99436886 -12.84891 -5.62796874 -8.82552941 -4.47761194 -5.19275508 -4.63099107 -6.9230769 -4.15717446 -4.01550789 -3.88102336 -3.75322543 -3.63166228 -3.75322543 -3.631666667 -4.1379310 -4.28571429 -4.2553211 -4.964600 -2.6845000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.0000000 -4.000000000 -4.00000000 -4.0000000000	-25,9740260 -25,9740260 -25,9740260 -21,0579515 -21,0579515 -21,0579515 -21,0579515 -21,0579515 -21,0579515 -21,9664751 -14,9664751 -13,9013422 -12,9580677 -14,9664751 -13,9013422 -12,9580677 -12,1177399 -15,76470588 -11,3636364 -10,6845027 -10,16845027 -10,0696821 -13,5636364 -10,6845027 -10,0696821 -11,3635333332 -11,3635333332 -11,3636364 -10,6845027 -10,0696821 -11,36353636 -10,0696821 -11,36353636 -10,0696821 -11,36353636 -10,0696821 -11,36353636 -10,0696821 -11,3635333332 -11,3636364 -10,6845027 -10,0696821 -10,16845027 -10,0696821 -10,16845027 -10,0696821 -10,0696822 -11,3635333332 -11,30434783 -4,87804978 -3,14257518 -7,0028757 -7,0028757 -7,0028757 -7,0328767 -7,0328757 -7,03	3Ci	3ci   3ci   3ci   3ci   3ci   3ci   3ci   5ci   5ci	3c    3c    3c    3c    3c    3c    3c    3c    bf(4)(E)   bf(4)	\$\frac{1}{2}C_0^1

$(D^3y)_{x=x_1} = \frac{1}{b^3}$	$\sum_{i=0}^{3} {}_{3}^{3}C_{j}^{i}$	y <sub>j</sub> + 3R <sup>i</sup>	(i=0,1,2,3)
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			. 62	j=0				and m	,
- <u>a_a</u>	3Ci	3C 1	3C i	3Ci 3Ci	3E <sup>0</sup> bf (4) (ξ)	3Ε <sup>1</sup> bf <sup>(4)</sup> (ξ)	3 <sub>3</sub> E <sup>2</sup> bf <sup>(4)</sup> (ξ)	3E <sup>3</sup>	
0.70 .71 .72 .73	- 1.86741363 - 1.82359125 - 1.78123575 - 1.74028206 - 1.70066871	4.28571429 4.22535211 4.16666667 4.10958904 4.05405405	-3.52941176 -3.50877193 -3.48837209	1.1111111 1.10701107 1.10294118 1.09890110	-1.2750 -1.2825 -1.2900 -1.2975 -1.3050	-0.5750 5725 5700 5675 5650	0.4250 .4275 .4300 .4325 .4350	bf (E) 1.4250 1.4275 1.4300 1.4325 1.4350	0.70 .71 .72 .73
.75 .76 .77 .78	- 1.66233765 - 1.62523404 - 1.58930589 - 1.55450403 - 1.52078187	4.00000000 3.94736842 3.89610390 3.84615385 3.79746835	-3.42857143 -3.40909091 -3.38983051 -3.37078652 -3.35195531	1.08695652 1.08303249 1.07913669	-1.3125 -1.3200 -1.3275 -1.3350 -1.3425	5625 5600 5575 5550 5525	.4375 .4400 .4425 .4450 .4475	1.4375 1.4400 1.4425 1.4450 1.4475	.75 .76 .77 .78
.80 .81 .82 .83	- 1.48809524 - 1.45640223 - 1.42566308 - 1.39583998 - 1.36689703	3.75000000 3.70370370 3.65853659 3.61445783 3.57142857	-3.3333333 -3.31491713 -3.29670330 -3.27868852 -3.26086957	1.06761566 1.06382979 1.06007067	-1.3500 -1.3575 -1.3650 -1.3725 -1.3800	5500 5475 5450 5425 5400	.4500 .4525 .4550 .4575 .4600	1.4500 1.4525 1.4550 1.4575 1.4600	.80 .81 .82 .83
.85 .86 .87 .88	- 1.33880010 - 1.31151669 - 1.28501588 - 1.25926821 - 1.23424563	3.52941176 3.48837209 3.44827586 3.40909091 3.37078652	-3.24324324 -3.22580645 -3.20855615 -3.19148936 -3.17460317	1.04895105 1.04529617 1.04166667	-1.3875 -1.3950 -1.4025 -1.4100 -1.4175	5375 5350 5325 5300 5275	.4625 .4650 .4675 .4700 .4725	1.4625 1.4650 1.4675 1.4700 1.4725	.85 .86 .87 .88
.90 .91 .92 .93	- 1.20992136 - 1.18626988 - 1.16326683 - 1.14088895 - 1.11911402	3.3333333 3.29670330 3.26086957 3.22580645 3.19148936	-3.15789474 -3.14136126 -3.12500000 -3.10880829 -3.09278351	1.03092784 1.02739726 1.02389078	-1.4250 -1.4325 -1.4400 -1.4475 -1.4550	5250 5225 5200 5175 5150	.4750 .4775 .4800 .4825 .4850	1.4750 1.4775 1.4800 1.4825 1.4850	.90 .91 .92 .93
.95 .96 .97 .98	- 1.09792081 - 1.07728902 - 1.05719924 - 1.03763287 - 1.01857214	3.15789474 3.12500000 3.09278351 3.06122449 3.03030303	-3.07692308 -3.06122449 -3.04568528 -3.03030303 -3.01507538	1.01351351 1.01010101 1.00671141	-1.4625 -1.4700 -1.4775 -1.4850 -1.4925	5125 5100 5075 5050 5025	.4875 .4900 .4925 .4950 .4975	1.4875 1.4900 1.4925 1.4950 1.4975	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	- 1.00000000 981900144 964256925 947055345 930281019	3.00000000 2.97029703 2.94117647 2.91262136 2.88461538	-3.00000000 -2.98507463 -2.97029703 -2.95566502 -2.94117647	1.00000000 .996677741 .993377483 .990099010 .986842105	-1.5000 -1.5075 -1.5150 -1.5225 -1.5300	5000 4975 4950 4925 4900	.5000 .5025 .5050 .5075 .5100	1.5000 1.5025 1.5050 1.5075 1.5100	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	913920147 897959478 882386289 867188367 852353967	2.85714286 2.83018868 2.80373832 2.7777778 2.75229358	-2.92682927 -2.91262136 -2.89855072 -2.88461538 -2.87081340	.983606557 .980392157 .977198697 .974025974 .970873786	-1.5375 -1.5450 -1.5525 -1.5600 -1.5675	4875 4850 4825 4800 4775	.5125 .5150 .5175 .5200 .5225	1.5125 1.5150 1.5175 1.5200 1.5225	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	837871806 823731033 809921211 796432302 783254643	2.72727273 2.70270270 2.67857143 2.65486726 2.63157895	-2.85714286 -2.84360190 -2.83018868 -2.81690141 -2.80373832	.967741936 .964630225 .961538462 .958466454 .95541401	-1.5750 -1.5825 -1.5900 -1.5975 -1.6050	4750 4725 4700 4675 4650	.5250 .5275 .5300 .5325 .5350	1.5250 1.5275 1.5300 1.5325 1.5350	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	770378931 757796208 745497846 733475529 721721247	2.60869565 2.58620690 2.56410256 2.54237288 2.52100840	-2.79069767 -2.77777778 -2.76497696 -2.75229358 -2.73972603	.95238095 .94936709 .94637224 .94339623 .94043887	-1.6125 -1.6200 -1.6275 -1.6350 -1.6425	4625 4600 4575 4550 4525	.5375 .5400 .5425 .5450 .5475	1.5375 1.5400 1.5425 1.5450 1.5475	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	710227272 698986155 687990708 677234001 666709335	2.50000000 2.47933884 2.45901639 2.43902439 2.41935484	-2.72727273 -2.71493213 -2.70270270 -2.69058296 -2.67857143	.93750000 .93457944 .83167702 .92879257 .92592593	-1.6500 -1.6575 -1.6650 -1.6725 -1.6800	4500 4475 4450 4425 4400	.5500 .5525 .5550 .5575 .5600	1.5500 1.5525 1.5550 1.5575 1.5600	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	656410257 646330524 636464112 626805198 617348163	2.4000000 2.38095238 2.36220472 2.34375000 2.32558140	-2.66666667 -2.65486726 -2.64317181 -2.63157895 -2.62008734	.92307692 .92024540 .91743119 .91463415 .91185410	-1.6875 -1.6950 -1.7025 -1.7100 -1.7175	4375 4350 4325 4300 4275	.5625 .5650 .5675 .5700 .5725	1.5625 1.5650 1.5675 1.5700 1.5725	1.25 1.26 1.27 1.28 1.29
	- 3C i 3	-3C1	-3Ci	-3Ci	$\frac{{}^{3}E^{3}}{{}^{5}}$	$-\frac{{}^{3}E^{2}}{{}^{5}f^{(4)}(z)}$	$-\frac{\frac{3E^{1}}{3}}{bf^{(4)}(\epsilon)}$	- 3EO bf (4)(E)	p= <u>c=c</u> b=a



			j=0	• 1 • 2		~~	ACA
_a_a_a						LE <sup>0</sup>	
b c d		4 C0	1C0 4C2	1 C <sub>3</sub>	1C0	$\frac{4^{2}}{b^{4}f^{(5)}(E)}$	
0.10	-11.7078620	11.9350000	-0.295909092	0.0811904762	-0.0124193548	0.0060	0.10
.11	-10.7872870	11.0362591	325149099	.0899836493	0138065916	.0067	.11
.12	-10.0184014 - 9.36623583	10.2890667	354342857	.0988981132	0152205128	.0074	.12
.14	- 8.80581118	9.65845769 9.11945714	383494248 412607018	.107933568 .117089720	0166611821 0181286624	.0082	,13
.15	- 8.31880848	8.65375000	441684783	.126366279	0196230159	.0097	.15
.16	- 7.89148762	8.24760000	470731034	.135762963	0211443038	.0106	.16
.17	- 7.51334070	7.89050294	499749145	.145279493	0226925868	.0114	.17
.18 .19	- 7.17619419 - 6.87359466	7.57428889 7.29250789	528742373 557713866	.154915596 .164671005	0242679245 0258703762	.0123	.18
.20	- 6.60037879	7.04000000	586666667	.174545455	0275000000	.0141	.20
.21	- 6.35236621	6.81258810	615603719	.184538688	0291568536	.0150	.21
.22	- 6.12613613	6.60685455	644527869	.194650450	0308409938	.0160	.22
.23	- 5.91886223	6.41997609	673441870	.204880493	0325524768	.0170	.23
.24	- 5,72818882	6.24960000	702348387	.215228571	0342913580	.0180	.24
.25	- 5.55213675	6.09375000	731250000	.225694444	0360576923	.0190	.25
.26	- 5.38903098	5.95075385	760149206	.236277876	0378515337	.0201	.26
.27 .28	- 5.23744431 - 5.09615311	5.81918704 5.69782857	789048425 817950000	•246978634 257706403	0396729358	.0212	.27
.29	- 4.96410225	5.58562586	817950000 846856202	.257796491 .268731223	0415219512 0433986322	.0223	.28
.30	- 4.84037701	5.48166667	875769231	.279782609	0453030303	.0247	.30
.31	- 4.72418046	5.38515645	904691221	.290950433	0472351964	.0259	.31
.32	- 4.61481506	5,29540000	933624242	.302234483	0491951807	.0271	. 32
.33	- 4.51166758	5.21178636	962570301	.313634549	0511830330	.0284	. 33
. 34	- 4.41419675	5.13377647	991531343	.325150427	0531988024	.0297	.34
.35	~ 4.32192297	5.06089286	-1.02050926	.336781915	0552425373	.0310	. 35
.36	- 4.23441975	4.99271111	→1.04950588	.348528814	0573142857	.0324	. 36
.37	- 4.15130654 - 4.07224268	4.92885270 4.86897895	-1.07852299 -1.10756232	.360390928 .372368067	0594140950	.0337	. 37
.39	- 3.99692232	4.81278590	-1.13662554	.384460042	0615420118 0636980826	.0352	.38
.40	- 3.92507003	4.76000000	~1.16571429	.396666667	0658823529	.0381	
.41	- 3.85643714	4.71037439	-1.19483014	.408987759	0680948680	.0396	.40
. 42	- 3.79079853	4.66368572	-1.22397465	.421423140	0703356725	.0411	.42
. 43	- 3.72794992	4.61973140	-1.25314930	.433972634	0726048105	.0427	. 43
.44	- 3.66770546	4.57832727	-1.28235556	.446636066	0749023256	.0442	. 44
.45	- 3.60989573	4.53930556	-1.31159483	.459413265	0772282609	.0460	.45
.46	- 3.55436596	4.50251304	-1.34086849	.472304065	0795826590	.0476	.46
.47	- 3.50097442	4.46780957	-1.37017789	.485308300	0819655620	.0494	.47
.49	- 3.44959114 - 3.40009664	4.43506667 4.40416633	-1.39952432 -1.42890906	.498425806 .511656486	0843770115 0868170487	.0511	.48
.50	- 3.35238095	4.37500000	-1.45833333	.525000000	0892857143	.0547	.50
.51	- 3.30634263	4.34746765	-1.48779834	.538456375	0917830484	.0565	.51
.52	- 3.26188796	4.32147692	-1.51730526	.552025397	0943090909	.0584	.52
.53	- 3.21893026	4.29694245	-1.54685523	.565706917	0968638810	.0604	. 53
.54	- 3.17738916	4.27378519	-1.57644935	.579500787	0994474570	.0623	.54
	~ 3.13719011	4.25193182	-1.60608871	.593406863	102059859	.0643	.55
. 56	- 3.09826380	4.23131429	-1.63577436	.607425000	104701124	.0664	.56
.57	- 3.06054574   - 3.02397583	4.21186930	-1.66550732	621555058	107371289	.0684	.57
	- 3.02397583 - 2.98849799	4.19353793 4.17626525	-1.69528861 -1.72511918	.635796899 .650150386	110070391 112798468	.0705 .0727	.58 .59
.60	- 2.95405983	4.16000000	-1.75500000	.664615385	115555556	.0749	. 60
.61	- 2.92061235	4.14469426	-1.78493199	679191762	118341690	.0771	.61
. 62	- 2.88810966	4.13030323	-1.81491605	.693879389	121156906	.0794	. 62
	- 2.85650875 - 2.82576925	4.11678492 4.10410000	-1.84495307 -1.87504390	.708678137 .723587878	124001240 126874725	.0817 .0841	.63 .64
	- 2.79585324	4.09221154	-1.90518939				
	- 2.76672505	4.08108485	-1.93539036	.738608490 .753739850	129777397 132709290	.0864 .0889	.65 .66
	- 2.73835111	4.07068731	-1.96564760	768981835	135670436	.0914	. 67
. 68	- 2.71069980	4.06098824	-1.99596190	.784334328	138660870	.0939	.68
. 69	- 2.68374126	4.05195870	-2.02633402	.799797212	141680623	.0965	.69
						1-4	
	- 1C4	- 1C4	- 104	_ 1 04	_ 104	4E <sup>4</sup>	d d d
	4 4	4 3	- 1C4	- 1C4	- 1C4	b4f(5)(E)	0= <u>d d d</u> c b a
						5 . (4)	

 $(D^{1}y)_{x=x} = \frac{1}{b} \sum_{j=0}^{4} {}_{4}C^{j}_{j} y_{j} + {}_{4}R^{j}$  (i=0.4)

NACA

						1E0	
aaa bcd	1C0	4C1	1 C <sub>2</sub>	1C0 4C3	1 C <sup>0</sup>	b <sup>4</sup> f <sup>(5)</sup> (£)	
0.70	- 2.65744736	4.04357143	-2.05676471	0.815370370	-0.144729730	0.0991	0.70
	- 2.63179149	4.03580070.	-2.08725468	.831053690	147808221	.1017	.71 .72
	- 2.60674850	4.02862222	-2.11780465	.946847059	150916129	.1072	.73
.73	- 2.58229457	4.02201301	-2.14841532	.862750366 .878763504	154053485 157220321	.1100	.74
.74	- 2.55840717	4.01595135	-2.17908736				.75
	- 2.53506493	4.01041667	-2.20982143	.894886364	160416667 163642553	.1128 .1157	.76
	- 2.51224758	4.00538947	-2.24061818 -2.27147825	.911118841	166898011	.1186	.77
	- 2.48993587	4.00085130 3.99678462	-2.30240225	.943912230	170183069	.1216	.78
	- 2.46811153 - 2.44675718	3.99317278	-2.33339078	.960472939	173497757	.1246	.79
.80	- 2.42585631	3.99000000	-2.3644444	.977142857	176842105	.1277	.80
	- 2.40539316	3.98725123	-2.39556381	.993921886	180216142	.1308	.81
	- 2.38535278	3.98491220	-2.42674945	1.01080993	183619895	.1340	.82 .83
	- 2.36572086	3.98296927	-2.45800191	1.02780689	187053394 190516667	.1405	.84
.84	- 2.34648379	3.98140953	-2.48932174	1.04491268			
.85	- 2.32762858	3.98022058	-2.52070946	1.06212719	194009740	.1438	.85 .86
	- 2.30914281	3.97939071	-2.55216559	1.07945035	197532642 201085401	.1472	.87
.87	- 2.29101463	3.97890862	-2.58369064 -2.61528511	1.09688206	201063401	.1541	.88
	- 2.27323271 - 2.25578620	3.97876364 3.97894550	-2.64694947	1.13207076	208280591	.1576	.89
			-2.67868421	1.14982759	211923077	.1612	.90
	- 2.23866474	3.97944444 3.98025110	-2.71048979	1.16769261	215595524	.1648	.91
	- 2.22185839 - 2.20535765	3.98135653	-2.74236667	1.18566575	219297959	.1685	.92
	- 2.18915339	3.98275215	-2.77431528	1.20374693	223030407	.1722	.93
	- 2.17323686	3.98442979	-2.80633608	1.22193605	226792893	.1760	.94
.95	→ 2.15759970	3.98638157	-2.83842949	1.24023305	230585443	.1799	.95
	→ 2.14223384	3.98860001	-2.87059592	1.25863784	234408081	.1838 .1878	.96
	- 2.12713155	3.99107784	-2.90283579	1.27715034	238260831 242143719	1918	.98
	- 2.11228542	3.99380816	-2.93514949	1.29577047	246056767	.1959	.99
.99	- 2.09768830	3,99678434	-2.96753744			2000	1.00
.00	- 2.08333333	4.00000000	-3.00000000	1.33333333	250000000 253973441	.2000 .2042	1.01
	- 2.06921392	4.00344901	-3.03253756 -3.06515050	1.35227591	257977114	.2085	1.02
	- 2.05532371	4.00712549	-3.09783916	1.39048300	262011042	.2128	1.03
	- 2.04165658 - 2.02820666	4.01513846	-3.13060392	1.40974737	266075248	.2171	1.04
	- 2.01496826	4.01946429	-3.16344512	1.42911885	270169753	.2216	1.05
	- 2.00193592	4.02399623	-3.19636311	1.44859739	274294581	.2261	1.06
.07	- 1.98910437	4.02872944	-3.22935821	1.46818290	278449754	.2306 .2352	1.08
. 06	- 1.97646852	4.03365926 4.03878119	-3.26243077 -3.29558110	1.48787532	282635294 286851222	.2399	1.09
09	- 1.96402346	4.000/0115			001007561	.2447	1.10
.10	- 1.95176447	4.04409091	-3.32880952	1.52758065	291097561 295374331	.2495	1.11
.11	- 1.93968696	4.04958423	-3.36211635 -3.39550189	1.56771282	299681553	.2543	1.12
.12	- 1.92778652 - 1.91605889	4.05525714	-3.42896643	1.58793882	304019249	.2593	1.13
.13	- 1.91603889	4.06712632	-3.46251028	1.60827134	308387440	-2643	1.14
	1 00230567	4.07331521	-3.49613372	1.62871032	312786145	.2694	1.15
.15	- 1.89310567 - 1.88187224	4.07966897	-3.52983704	1.64925570	317215385	.2745	1.16
.16	- 1.87079591	4.08618419	-3.56362051	1.66990741	321675180	.2797	1.17
.18	- 1.85987308	4.09285763	-3.59748440	1.69066541	326165550 330686516	.2903	1.19
.19	- 1.84910025	4.09968613	-3.63142900	1.71152962			
.20	- 1.83847403	4.10666667	-3.66545455	1.73250000	→ .335238095	.2957	1.20
.21	- 1.82799114	4.11379628	-3.69956131	1.75357648	339820309 344433175	.3067	1.22
. 22	- 1.81764841	4.12107214	-3.73374955 -3.76£01951	1.77475901	349076714	.3123	1.23
.23 L.24	- 1.80744277 - 1.79737122	4.12849146	-3.76671951	1.81744198	353750943	.3180	1.24
				1.83894231	358455882	.3237	1.25
.25	- 1.78743087	4.14374999	-3.83680556 -3.87132212	1.86054847	363191549	.3296	1.26
1.26	- 1.77761892	4.15158413	-3.90592137	1.88226040	367957963	.3355	1.27
L.27 L.28	- 1.76793264 - 1.75836940	4.16765001	-3.94060351	1.90407805	372755140	.3414	1.28
	- 1.74892662	4.17587713	-3.97536878	1.92600137	377583100	.3475	1.20
1.29	2.170020						
	2017,002					E <sup>4</sup>	
	- iC4	- <sup>1</sup> C <sup>4</sup> <sub>3</sub>	1C4	- iC4	- <sup>1</sup> C <sup>4</sup> <sub>0</sub>	b <sup>4</sup> f <sup>(5)</sup> (£)	p_d_d p_c_b



						and my
1 C0	4C	1C1	1C1 4C3	iC14	$\frac{{}_{4}^{1}E^{1}}{b^{4}f^{(5)}(\underline{s})}$	
-8.37871806 -7.48846393 -6.74934342 -6.12640232 -5.59467602	8.16666667 7.25757576 6.50000000 5.85897436 5.30952381	.272727273 .297297297 .321428571 .345132743 .368421053	0714285714 0781990521 0849056604 0915492958 0981308411	.0117899250 .0128205128 .0138445154	0055 0060 0065	0.10 .11 .12 .13
-5.13585953 -4.73622630 -4.38528144 -4.07486405 -3.79853288	4.83333333 4.41666667 4.04901961 3.72222222 3.42982456	.391304348 .413793103 .435897436 .457627119 .478991597	104651163 111111111 117511521 123853211 130136986	.0158730159 .0168776371 .0178759201 .0188679245 .0198537095	0075 0080 0085 0090 0095	.15 .16 .17 .18
-3.55113636 -3.32850550 -3.12723050 -2.94449565 -2.77795557	3.16666667 2.92857143 2.71212121 2.51449275 2.333333333	.500000000 .520661157 .540983607 .560975610 .580645161	136363636 142533937 148648649 154708520 160714286	.0208333333 .0218068536 .0227743271 .0237358101 .0246913580	0100 0105 0110 0115 0120	.20 .21 .22 .23
-2.62564103 -2.48588663 -2.35727448 -2.23859000 -2.12878677	2.16666667 2.01282051 1.87037037 1.73809524 1.61494253	.600000000 .619047619 .637795276 .656250000	166666667 172566372 178414097 184210526 189956332	.0256410256 .0265848671 .0275229358 .0284552846	0125 0130 0135 0140	.25 .26 .27 .28
-2.02695855 -1.93231661 -1.84417136 -1.76191728	1.50000000 1.39247312 1.29166667 1.19696970	.692307692 .709923664 .727272727 .744360902	195652174 201298701 206896552 212446352	.0303030303 .0312185297 .0321285141	0150 0155 0160 0165	.29 .30 .31 .32
-1.61300892 -1.54546282 -1.48200856 -1.42231212	1.02380952 .94444445 .869369370 .798245614	.77777778 .794117647 .810218978 .826086957	23404255 228813559 234177215 239495798	.0348258706 .0357142857 .0365974283 .0374753452	0175 0180 0185 0190	.34 .35 .36 .37
-1.31302521 -1.26292296 -1.21554809 -1.17070201	.66666667 .605691057 .547619048 .492248062	.857142857 .872340426 .887323944 .902097902	25000000 255186722 260330579 265432090	.0392156863 .0400782014 .0409356725 .0417881438	0195 0200 0205 0210 0215	.40 .41 .42 .43
-1.08789143 -1.04961338 -1.01323371 978627404	.38888889 .340579710 .294326241 .250000000	.931034483 .945205479 .959183673 .972972973	275510204 280487805 285425101 290322581	.0434782609 .0443159923 .0451488953 .0459770115	0220 0225 0230 0235 0240	.45 .46 .47 .48
• .914285714 • .884348185 • .855777994 • .828492771	.166666667 .127450980 .0897435897 .0534591195	1.00000000 1.01324503 1.02631579 1.03921569	295180923 300000000 304780876 309523810 314229249	.0468003820 .0476190476 .0484330484 .0492424242 .0500472143	0245 0250 0255 0260 0265	.49 .50 .51 .52
.753613486 - .730761070 - .708864842 -	0476190476 0889473684 109195402	1.05194805 1.06451613 1.07692308 1.08917197 1.10126582	318897638 323529412 328125000 332684825 337209302	.0508474576 .0516431925 .0524344569 .0532212885 .0540037244	0270 0275 0280 0285 0290	.54 .55 .56 .57 .58
.667735043 - .648407202 - .629846448 - .612013107 -	166666667 193989071 220430108 246031746	1.11320755 1.12500000 1.13664596 1.14814815 1.15950920	341698842 346153846 350574713 354961832 359315589	.0547818013 .055555556 .0563250231 .0570902394 .0578512396	0295 0300 0305 0310 0315	.59 .60 .61 .62 .63
.578382589 - .562518105 - .547246069 - .532537804 -	294871794 318181818 340796019 362745097	1.18181818 1.19277108 1.20359281 1.21428571	367924528 372180451 376404494 380597015	.0593607305 .0601092896 .0608537693 .0615942028	0325 0330 0335 0340	.64 .65 .66 .67
- 1C3	- <sup>1</sup> C <sup>3</sup> <sub>4</sub>	- <sup>1</sup> C <sup>3</sup> <sub>4</sub> C <sub>2</sub>	- 1C3 4C1	- <sup>1</sup> C <sub>0</sub> <sup>3</sup>	-, 0345 <sup>1</sup> Ε <sup>3</sup> <sup>4</sup> Γ <sup>(5)</sup> (ε)	p=d_d_d c_b_a
	-8.37871806 -7.48846393 -6.74934342 -6.12640232 -6.12640232 -5.59467602 -5.59467602 -5.13585953 -4.73622630 -4.38528144 -4.07486405 -3.79853288 -3.55113636 -3.32850550 -3.12723050 -2.94449565 -2.77795557 -2.62564103 -2.48588663 -2.35727448 -2.23859000 -2.12878677 -2.02695855 -1.93231661 -1.6191728 -1.68502058 -1.61300892 -1.54546282 -1.46200856 -1.42231212 -1.36607406 -1.31302521 -1.26292296 -1.21554809 -1.71070201 -1.12820446 -1.08789143 -1.08789143 -1.09789144	-B. 37871806 -7. 48846393 -6. 74934342 -6. 12640232 -5. 59467602 -5. 59467602 -5. 59467602 -5. 30952381 -5. 13585953 -4. 38528144 -4. 07496405 -3. 32850550 -3. 12723050 -2. 94449565 -2. 77795557 -2. 62564103 -2. 46588663 -2. 48588663 -2. 355713661 -1. 76191728 -1. 61404253 -1. 61404253 -1. 61404253 -1. 61300892 -1. 544444445 -1. 61300892 -1. 5456666667 -1. 2229296 -1. 366666667 -1. 2629296 -1. 2629296 -1. 2629296 -1. 2629296 -1. 2629296 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 12820446 -1. 17070201 -1. 17	-B. 37871806	-E. 37871806   B. 16666667   .272727273  0714285714   .74934342   6.50000000   .345132743  084905661   .0915492958   .368421053	-B. 37871806	4.76  8.1666667  7.28757576  6.79454542  6.50000000  3.21428571  7.0949056604  1.0175828822  7.28757576  6.794934542  6.50000000  3.21428571  7.0949056604  1.0128205128  7.00550  7.00557576  7.28757577  7.2875757  7.287577  7.287577  7.287577  7.28757  7.287577  7.287577  7.287577  7.287577  7.28757  7.28757  7.28757

15(a)

(D	$y)_{x=x} = \frac{1}{b}$	$\sum_{i=0}^{4}$	lcj 4	Уj	+	IRI	(i=1,3)
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						4E	
		1.4	101	Icl	וטו		
a a a	100 400	1 C1	1C1	1C3	1C1	b4f(5)(E)	
b_c_d					********	0750	0.70
0.70	504706387	-0.404761904	1.23529412	38888889	0630630630	0350	.71
.71	491534030	424882629	1.24561404	392988930	.0637915543 .0645161290	0360	.72
.72	478826815	44444444	1.25581395	397058824	.0652368185	0365	.73
.73	466563552	463470319	1.26589595	401098901	.0659536541	0370	.74
.74	454724252	481981982	1.27586207	405109489	. 0000000011		
				409090909	.0666666667	0375	.75
.75	443290043	500000000	1.28571429	413043478	.0673758865	0380	.76
.76	432243094	517543859	1.29545455	416967509	.0680813439	0385	.77
.77	421566546	534632034	1.31460674	420863309	.0687830687	0390	.78
.78	411244450	551282051 567510548	1.32402235	424731183	.0694810905	0395	.79
.79	401261706	007010040	1.00.10				00
	701604010	583333333	1.33333333	428571429	.0701754386		.80
.80	382257805	598765432	1.34254144	432384342	.0708661417	0405	.82
.81	373210228		1.35164835	436170213	,0715532286	0410	.83
.82	364449081	628514056	1.36065574	439929329	.0722367276		.84
.84	- 355962768		1.36956522	443661972	.0729166667	0420	•0.
•04				4.000003	.0735930736	0425	. 85
.85	347740287	656862745	1.37837838	447368421 451049951	.0742659758		.86
.86	339771162	670542636	1.38709677	451048951 454703833	0749354005		.87
.87	→ .332045447	683908046	1.39572192	458333333	.0756013746	0440	.88
.88	324553663	696969697	1.40425532	461937716	0762639246		.89
.89	317286793	709737828	1441509041	3			00
	#3.00##C*#	722222222	1.42105263	465517241	.0769230769		.90
.90	310236245		1.42931937	469072165	.0775788576		.91
.91	303393830 296751741		1.43750000	472602740	.0782312925		.93
.92	290302531		1.44559585	476109215	.0788804071		94
.94	284039091		1.45360825	479591837	.0795262267	0470	•••
*54				407050047	.0801687764	0475	.95
.95	277954637	780701754	1.46153846	483050847	.0808080808		. 96
.96	272042682	791666667	1.46938776	486486486 489898990	.0814441646		.97
.97	266297037		1.47715736	493288591	.0820770519	0490	.98
.98	260711776		1.48484848	496655518	.0827067669	0495	.99
.99	255281237	823232323	1.49240201				3 00
	05000000	833333333	1.50000000	500000000	.0833333333		1.00
1.00	250000000 244862879		1.50746269	503322259	.0839567747		1.02
1.01	→ .239864907		1.51485149	-,506622517	.0845771144		1.03
1.02			1.52216749	509900990	.0851943755		1.04
1.04			1.52941176	513157895	.0858085809		
1.01				516393443	.086419753	0525	1.05
1.05	225659295	880952381	1.53658537	519607843	.0870279146		1.06
1.06	221172285		1.54368932	522801303	.087633087	5 0535	1.07
1.07	216802528		1.55769231	525974026	.088235294	1 0540	1.08
1.08			1.56459330	529126214	.0888345558	0545	1.09
1.09	20839950	915902141	1.0040000			0550	1 10
	004750077	924242424	1.57142857	532258065	.089430894		1.10
1.10			1.57819905	535369775	.090024330		1.12
1.11			1.58490566	538461538	.090614886' .091202582'		1.13
1.13			1.59154930	541533546	.091787439	- 0500	1.14
1.14			1.59813084	544585987	.002701300		_
1			1 60466116	547619048	.092369477	90575	1.15
1.15	18563347	7963768116	1.60465116	550632911	.092948717	90580	1.16
1.16	18216255		1.61751152	553627760	.093525179	90585	1.17
1.17			1.62385321	556603774	.094098883		1.18
1.18		8992997199	1.63013699	559561129	.094669848	80595	1.19
1.19	17224850	502.501150			005050005	- 0600	1,20
1 2 66	16010173	2 -1.00000000	1.63636364	562500000	.095238095		1.21
1.20	16602996	6 -1.00688705	1.64253394	565420561	.095803642		1.22
1.22	16303097	4 -1.01300120	1.64864865	568322981	.096926713		1,23
1.23	- 10010200	1 -1.02032520	1.65470852	571207430 574074074	.097484276		1.24
1.24		8 -1.02688172	1.66071429	, 5/40/40/4	,00.2020.0		
20.00			1.66666667	576923077	.098039215	70625	1.25
1.25	515444947	2 -1.033333333	1.67256637		.098591549	3 0630	1.26
1.20	315172078	0 -1.03968254	1.67841410		.099141295	9 0635	1.27
1.2	714905482	7 -1.04593170	1.68421053		.099688473		1.28
1.20			1.68995633		.100233100	0645	1,28
1.2	914390400	1 -1.00010000				1.3	
						4E3	d d d
		1.03	103	_ 103	- <sup>1</sup> C <sub>0</sub> <sup>3</sup>	4 (5)	p= c b a
	- 1C3	- 1C3	- 1C3	- <sup>1</sup> C <sup>3</sup>	4 0	b <sup>4</sup> f' (ξ)	CDA
1		1 7	1				

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			$(D \mathbf{y})^{\mathbf{x}=\mathbf{x}^{\dagger}} = \frac{\mathbf{p}}{\mathbf{p}}$	_ 4 <sup>C</sup> j yj + 4 <sup>K</sup>	(1 = 2)	and	July
r <u>*a_a_a</u>	102	1C2	. 102	102	1 <sub>C</sub> 2	1E <sup>2</sup>	-
0.10 .11 .12 .13	2.79290602 2.49615464 2.24978114 2.04213411 1.86489201	-3.66666667 -3.36363636 -3.11111111 -2.89743590 -2.71428571	4 2 0.409090909 .40090901 .392857143 .384955752 .377192982	4 3 0.523809524 .526066351 .528301887 .530516432 .532710280	- 0.0591397849 - 0.0594855305 - 0.0598290598 - 0.0601703940 - 0.0605095541	b <sup>4</sup> f <sup>(5)</sup> (g) 0.0183 .0185 .0187 .0188 .0190	0.10 .11 .12 .13
.15 .16 .17 .18	1.71195318 1.57874210 1.46176048 1.35828802 1.26617763	-2.5555556 -2.41666667 -2.29411765 -2.18518519 -2.08771930	.369565217 .362068966 .354700855 .347457627 .340336134	.534883721 .537037037 .539170507 .541284404 .543378995	0608465608 0611814346 0615141956 0618448637 0621734587	.0192 .0193 .0195 .0197	.15 .16 .17 .18
.20 .21 .22 .23	1.18371212 1.10950183 1.04241017 .981492550 .925985190	-2.00000000 -1.92063492 -1.84848485 -1.78260870 -1.7222222	.333333333 .326446281 .319672131 .313008130 .306451613	.545454545 .547511312 .549549550 .551569507 .553571429	0625000000 0628245067 0631469979 0634674923 0637860082	.0200 .0202 .0203 .0205 .0207	.20 .21 .22 .23 .24
.25 .26 .27 .28	.875213677 .828628877 .785758160 .746196667 .709595590	-1.66666667 -1.61538462 -1.56790123 -1.52380952 -1.48275862	.300000000 .293650794 .287401575 .281250000 .275193798	.55555556 .557522124 .559471366 .561403509 .563318777	0641025641 0644171779 0647298675 0650406504 0653495441	.0208 .0210 .0212 .0213 .0215	.25 .26 .27 .28
.30 .31 .32 .33	.675652850 .644105537 .614723787 .587305760 .561673527	-1.4444444 -1.40860215 -1.37500000 -1.34343434 -1.31372549	.269230769 .263358779 .257575757 .251879699 .246268657	.565217391 .567099567 .568965517 .570815451 .572649573	0656565657 0659617321 0662650602 06656C5666 0668662675	.0217 .0218 .0220 .0222 .0223	.30 .31 .32 .33 .34
.35 .36 .37 .38 .39	.537669640 .515154273 .494002853 .474104040 .455358020	-1.28571429 -1.25925926 -1.23423423 -1.21052632 -1.18803419	.240740740 .235294118 .229927007 .224637681 .219422460	.574468085 .576271186 .578059072 .579831933 .581589958	0671641791 0674603175 0677546983 0680473373 0683362498	.0225 .0227 .0228 .0230 .0232	.35 .36 .37 .38 .39
.40 .41 .42 .43	.437675070 .420974320 .405182697 .390234003 .376068153	-1.16666667 -1.14634146 -1.12698413 -1.10852713 -1.09090909	.214285714 .209219858 .204225352 .199300699 .194444444	.583333333 .585062241 .586776860 .588477366 .590163934	0686274510 0689149560 0692007797 0694849368 0697674419	.0233 .0235 .0237 .0238 .0240	.40 .41 .42 .43
.45 .46 .47 .48	.362630476 .349871126 .337744570 .326209135 .315226611	-1.07407407 -1.05797101 -1.04255319 -1.02777778 -1.01360544	.189655172 .184931507 .180272109 .175675676 .171140940	.591836735 .593495935 .595141700 .596774194 .598393574	0700483092 0703275530 0706051873 0708812261 0711556829	.0242 .0243 .0245 .0247 .0248	.45 .46 .47 .48 .49
.50 .51 .52 .53	.304761905 .294782728 .285259331 .276164257 .267472130	-1.00000000 986928106 974358974 962264151 950617284	.166666667 .162251656 .157894737 .153594771 .149350649	.60000000 .601593625 .603174603 .604743083	0714285714 0716999050 0719696970 0722379603 0725047081	.0250 .0252 .0253 .0255 .0257	.50 .51 .52 .53
.55 .56 .57 .58 .59	.259159465 .251204495 .243587023 .236288281 .229290809	939393939 928571429 918128655 908045977 898305085	.145161290 .141025641 .136942675 .132911392 .128930818	.607843137 .609375000 .610894942 .612403101 .613899614	0727699531 0730337079 0732959851 0735567970 0738161560	.0258 .0260 .0262 .0263 .0265	.55 .56 .57 .58
.60 .61 .62 .63	.222578348 .216135734 .209948816 .204004370 .198290023	888888889 879781421 870967742 862433862 854166667	.125000000 .121118012 .117283951 .113496933 .109756098	.615384615 .616858238 .618320611 .619771863 .621212121	0740740741 0743305633 0745856354 0748393021 0750915750	.0267 .0268 .0270 .0272 .0273	.60 .61 .62 .63
.65 .66 .67 .68	.192794196 .187506035 .182415356 .177512601 .172788786	846153846 838383838 83,0845771 823529412 816425121	.106060606 .102409639 .098802395 .095238095 .091715976	.622641509 .624060150 .625468165 .626865672 .628252788	0753424657 0755919854 0758401453 0760869565 0763324299	.0275 .0277 .0278 .0280 .0282	.65 .66 .67 .68
	- <sup>1</sup> <sub>4</sub> C <sub>4</sub> <sup>2</sup>	- <sup>1</sup> C <sup>2</sup> <sub>3</sub>	- <sup>1</sup> C <sup>2</sup> <sub>2</sub>	- <sup>1</sup> C <sup>2</sup> <sub>1</sub>	- <sup>1</sup> C <sup>2</sup> <sub>4</sub> C <sub>0</sub>	b4f <sup>(5)</sup> (E)	p. <u>d</u> . <u>d</u> . <u>d</u>

(D <sup>1</sup> y) <sub>x=xi</sub> =	$\frac{1}{b} \sum_{i=0}^{4} {}^{i}_{4}C_{j}^{i}$	y <sub>j</sub> +	4R <sup>I</sup>	(i = 2)
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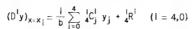
		(0 )/	$x=x_i = \frac{b}{b} \sum_{j=0}^{\infty} 4^{c_j} y$	j · 4 <sup>rt</sup> (' –			-
						LE <sup>2</sup>	
r <u>aaaa</u> bcd	1C2	1 C2	1C2	1 C2	1 C2	b <sup>4</sup> f <sup>(5)</sup> (ξ)	
0.70 .71 .72 .73	0.168235462 .163844677 .159608938 .155521184 .151574751	-0.809523810 802816901 796296296 789954338 783783784	0.0882352941 .0847953216 .0813953488 .0780346820 .0747126436	0.629629630 .630996310 .632352941 .633699634 .635036496	-0.0765765765 0768194070 0770609318 0773011617 0775401069	0.0283 .0285 .0287 .0288 .0290	0.70 .71 .72 .73 .74
.75 .76 .77 .78	.147763348 .144081031 .140522182 .137081483 .133753902	77777778 771929825 766233766 760683761 755274262	.0714285714 .0681818182 .0649717514 .0617977528 .0586592178	.636363636 .637681159 .638989170 .640287770 .641577061	077777778 0780141843 0782493368 0784832451 0787159190	.0292 .0293 .0295 .0297 .0298	.75 .76 .77 .78 .79
.80 .81 .82 .83	.130534670 .127419268 .124403409 .121483027 .118654256	750000000 744855967 739837398 734939759 730158730	.055555556 .0524861878 .0494505494 .0464480874 .0434782609	.642857143 .644128114 .645390071 .646643110 .647887324	0789473684 0791776028 0794066318 0796344648 0798611111	.0300 .0302 .0303 .0305 .0307	.80 .81 .82 .83
.85 .86 .87 .88	.115913429 .113257054 .110681816 .108184554 .105762264	725490196 720930232 716475096 712121212 707865168	.0405405405 .0376344086 .0347593583 .0319148936 .0291005291	.649122807 .650349650 .651567944 .652777778 .653979239	0800865801 0803108808 0805340224 0807560137 0809768638	.0308 .0310 .0312 .0313 .0315	.85 .86 .87 .88 .89
.90 .91 .92 .93	.103412082 .101131277 .0989172470 .0967675103 .0946796970	703703704 699633699 695652174 691756272 687943262	.0263157895 .0235602094 .0208333333 .0181347150 .0154639175	.655172414 .656357388 .657534247 .658703072 .659863946	0811965812 0814151748 0816326531 0818490246 0820642978	.0317 .0318 .0320 .0322 .0323	.90 .91 .92 .93
.95 .96 .97 .98	.0926515457 .0906808940 .088765679 .0869039253 .0850937457	684210526 680555555 676975945 673469388 670033670	.0128205128 .0102040816 .00761421320 .00505050505 .00251256281	.661016949 .662162162 .663299663 .664429530 .665551839	0822784810 0824915825 0827036104 0829145729 0831244779	.0325 .0327 .0328 .0330 .0332	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	.083333333 .0816209597 .0799549690 .0783337753 .0767558597	66666667 663366337 660130719 656957929 653846154	0 00248756219 00495049505 00738916256 00980392157	.66666667 .667774086 .668874172 .669966997 .671052632	0835333333 0835411471 0837479270 0839536807 0841584158	.0333 .0335 .0337 .0338 .0340	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	.0752197650 .0737240950 .0722675093 .0708487227 .0694665010	650793651 647798742 644859813 641975309 639143731	0121951220 0145631068 0169082126 0192307692 0215311005	.672131148 .673202614 .674267101 .675324675 .676375405	0843621399 0845648604 0847665848 0849673203 0851670742	.0342 .0343 .0345 .0347 .0348	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	.0681196590 .0668070587 .0655276060 .0642802503 .0630639807	6363636363 633633634 630952381 628318584 625730994	0238095238 0260663507 0283018868 0305164319 0327102804	.677419355 .678456592 .679487179 .680511182 .681528662	0853658537 0855636659 0857605178 0859564165 0861513688	.0350 .0352 .0353 .0355 .0357	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	.0618778257 .0607208500 .0595921540 .0584908717 .0574161693	623188406 620689655 618233618 615819209 613445378	0412844037	.682539683 .683544304 .684542587 .685534591 .686520376	0863453815 0865384615 0867306155 0869218501 0871121718	.0358 .0360 .0362 .0363 .0365	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	.0563672440 .0553433220 .0543436580 .0533675337 .0524142559	61111111 608815427 606557377 604336043 602150538	0475113122 0495495495 0515695067	.687500000 .688473520 .689440994 .690402477 .691358025	0873015873 0874901029 0876777251 0878644602 0880503145	.0367 .0368 .0370 .0372 .0373	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	.0514831573 .0505735933 .0496849423 .0488166042 .0479680003	600000000 597883598 595800525 593750000 591731266	0575221239 0594713656 0614035088	.692307692 .693251534 .694189603 .695121951 .696048632	0882352941 0884194053 0886026542 0887850467 0889665890	.0375 .0377 .0378 .0380 .0382	1.25 1.26 1.27 1.28 1.29
	- 1C2	- <sup>1</sup> C <sup>2</sup> <sub>4</sub>	- <sup>1</sup> <sub>4</sub> C <sub>2</sub> <sup>2</sup>	- <sup>1</sup> <sub>4</sub> C <sup>2</sup> <sub>1</sub>	- <sup>1</sup> <sub>4</sub> C <sub>0</sub> <sup>2</sup>	$\frac{{}_{4}^{1}E^{2}}{b^{4}f^{(5)}(\xi)}$	p=d=d=

$(D^{1}y)_{x=x_{i}} = \frac{1}{b} \sum_{j=0}^{4} {}_{4}^{1}C_{j}^{1} y_{j} + {}_{4}^{1}R^{1} $ (i = 3,1)									
r= <u>a</u> = <u>a</u> <u>a</u>	1C3	IC 3	IC 3 4 2	1C 3 4 3	1C3	b4f(5)(E)			
0.10 .11 .12 .13	-2.79290602 -2.49615464 -2.24978114 -2.04213411 -1.86489201	3.50000000 3.19696970 2.9444444 2.73076923 2.54761905	-1.90909091 -1.90090090 -1.89285714 -1.88495575 -1.87719298	0.976190476 .973933649 .971698113 .969483568 .967289720	0.225806452 .226152197 .226495726 .226837061 .227176221	-0.0350 0352 0353 0355 0357	0.10 .11 .12 .13 .14		
.15 .16 .17 .18	-1.71195318 -1.57874210 -1.46176048 -1.35828802 -1.26617763	2.38888889 2.25000000 2.12745098 2.01851852 1.92105263	-1.86956522 -1.86206897 -1.85470085 -1.84745763 -1.84033613	.965116279 .962962963 .960829493 .958715596 .956621005	.227513228 .227848101 .228180862 .228511530 .228840125	0358 0360 0362 0363 0365	.15 .16 .17 .18		
.20 .21 .22 .23	-1.18371212 -1.10950183 -1.04241017 981498550 925985190	1.83333333 1.75396825 1.68181818 1.61594203 1.55555556	-1.83333333 -1.82644628 -1.81967213 -1.81300813 -1.80645161	.954545455 .952488688 .950450450 .948430493 .946428571	.229166667 .229491173 .229813665 .230134159 .230452675	0367 0368 0370 0372 0373	.20 .21 .22 .23		
.25 .26 .27 .28	875213677 828628877 785758160 746196667 709595590	1.50000000 1.44871795 1.40123457 1.35714286 1.31609195	-1.80000000 -1.79365079 -1.78740157 -1.78125000 -1.77519380	.94444444 .942477876 .940528634 .938596491 .936681223	.230769231 .231083845 .231396534 .231707317 .232016211	0375 0377 0378 0380 0382	.25 .26 .27 .28 .29		
.30 .31 .32 .33	675652850 644105537 614723787 587305760 561673527	1.27777778 1.24193548 1.20833333 1.17676768 1.14705882	-1.76923077 -1.76335878 -1.75757676 -1.75187970 -1.74626866	.934782609 .932900433 .931034483 .929184549 .927350427	.232323232 .232628399 .232931727 .233233233 .233532934	0383 0385 0387 0388 0390	.30 .31 .32 .33		
.35 .36 .37 .38 .39	537669640 515154273 494002853 474104040 455358020	1.11904762 1.09259259 1.06756757 1.04385965 1.02136752	-1.74074074 -1.73529412 -1.72992701 -1.72463768 -1.71942446	.925531915 .923728814 .921940928 .920168067 .918410042	.233830846 .234126984 .234421365 .234714004 .235004916	0392 0393 0395 0397 0398	.35 .36 .37 .38 .39		
.40 .41 .42 .43	437675070 420974320 405182697 390234003 376068153	1.00000000 .979674797 .960317461 .941860465 .924242424	-1.71428571 -1.70921986 -1.70422535 -1.69930070 -1.69444444	.916666667 .914937759 .913223140 .911522634 .909836066	.235294118 .235581 <b>623</b> .235867446 .236151603 .236434109	0400 0402 0403 0405 0407	.40 .41 .42 .43		
. 45 . 46 . 47 . 48 . 49	362630476 349871126 337744570 326209135 315226611	.907407407 .891304348 .875886525 .86111111 .846938776	-1.68965517 -1.68493151 -1.68027211 -1.67567568 -1.67114094	.908163265 .906504065 .904858300 .903225806 .901606426	.236714976 .236994220 .237271854 .237547893 .237822350	0408 0410 0412 0413 0415	.45 .46 .47 .48		
.50 .51 .52 .53	304761905 294782728 285259331 276164257 267472130	.833333333 .820261438 .807692308 .795597484 .783950617	-1.66666667 -1.66225166 -1.65789474 -1.65359477 -1.64935065	.900000000 .898406375 .896825397 .895256917 .893700787	.238095238 .238366572 .238636364 .238904627 .239171375	0417 0418 0420 0422 0423	.50 .51 .52 .53		
.55 .56 .57 .58	259159465 251204495 243587023 236288281 229290809	.772727273 .761904762 .751461988 .741379310 .731638418	-1.64516129 -1.64102564 -1.63694268 -1.63291139 -1.62893082	.892156863 .890625000 .889105058 .887596899 .886100386	.239436620 .239700375 .239962652 .240223464 .240482823	0425 0427 0428 0430 0432	.55 .56 .57 .58		
.60 .61 .62 .63	222578348 216135734 209948816 204004370 198290023	.72222222 .713114754 .704301075 .695767196 .687500000	-1.62500000 -1.62111801 -1.61728395 -1.61349693 -1.60975610	.884615385 .883141762 .881679389 .880228137 .878787879	.240740741 .240997230 .241252302 .241505969 .241758242	0433 0435 0437 0438 0440	.60 .61 .62 .63		
.65 .66 .67 .68	192794196 187506035 182415356 177512601 172788786	.679487179 .671717172 .664179104 .656862745 .649758454	-1.60606061 -1.60240964 -1.59880240 -1.59523810 -1.59171598	.877358491 .875939850 .874531835 .873134328 .871747212	.242009132 .242258652 .242506812 .242753623 .242999097	0442 0443 0445 0447 0448	.65 .66 .67 .68		
	- <sup>1</sup> <sub>4</sub> C <sup>1</sup> <sub>4</sub>	- <sup>1</sup> C <sup>1</sup> <sub>3</sub>	- <sup>1</sup> C <sub>2</sub>	- ½C¦	- <sup>1</sup> C <sub>0</sub>	b <sup>4</sup> f <sup>(5)</sup> (ε)	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$		

$$(D^{I}y)_{x=x_{\dot{1}}} = \frac{1}{D} \sum_{j=0}^{4} {}_{4}^{I}C_{j}^{i} y_{j} + {}_{4}^{I}R^{i}$$
 (i = 3,1)



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						4E3	
r= <u>a</u> = <u>a</u> = <u>a</u>	1 C 3	1C3	1C3	1 C 3	1C3	$b^4f^{(5)}(\xi)$	
0.70	-0.168235462	0.642857143	-1.58823529	0.870370370	0.243243243	-0.0450	0.70
.71	163844677	.636150235 .629629630	-1.58479532 -1.58139535	.869003690 .867647059	.243486074	0452	.71
.72 .73	159608938 155521184	623287671	-1.57803468	866300366	.243967828	0455	.73
.74	151574751	.617117117	-1.57471264	.864963504	.244206774	0457	.74
.75	147763348	.611111111	-1.57142857	.863636364	.24444444	0458	.75
.76	144081031	.605263158	-1.56818182 -1.56497175	.862318841 .861010830	.244680851	0460	.76
.77 .78	140522182 137081483	.594017094	-1.56179775	.859712230	.245149912	0463	.78
.79	133753902	.588607595	-1.55865922	.858422939	.245382586	0465	.79
.80	130534670	.583333333	-1.55555556	.857142857	.245614035	0467	.80
.81	127419268	.578189300 .573170732	-1.55248619 -1.54945055	.855871886 .854609929	.245844269	0468 0470	.81
.82. .83	124403409 121483027	.568273092	-1.54644809	.853356890	.246301131	0472	.83
.84	118654256	.563492063	-1.54347826	.852112676	.246527778	0473	. 84
.85	115913429	.558823529	-1.54054054	.850877193	.246753247	0475	.85
.86	113257054 110681816	.554263566 .549808429	-1.53763441 -1.53475936	.849650350 .848432056	.246977547 .247200689	0477	.86 .87
.87 .88	108184554	.545454545	-1.53191489	.847222222	.247422680	0480	.88
.89	105762264	.541198502	-1.52910053	.846020761	.247643530	0482	.89
.90	103412082	.537037037	-1.52631579	.844827586	.247863248	0483	.90
.91 .92	101131277 0989172470	.532967033 .528985507	-1.52356021 -1.52083333	.843642612 .842465753	.248081841	0485 0487	.91
.93	0967675103	.525089606	-1.51813472	.841296928	.248515691	0488	.93
.94	0946796970	.521276596	-1.5154639.2	.840136054	.248730964	0490	.94
.95	0926515457	.517543860	-1.51282051	.838983051	.248945148	0492	.95
.96 .97	0906808940 0887656790	.513888889 .510309278	-1.51020408 -1.50761421	.837837838 .836700337	.249158249	0493 0495	.97
.98	0869039253	.506802721	-1.50505051	.835570470	.249581240	0497	.98
•99	0850937457	.503367003	-1,50251256	.834448161	.249791145		_
1.00	0833333333	.500000000 .496699670	-1.50000000 -1.49751244	.833333333 .832225914	.250000000 .250207814	0500	1.00
1.01	0816209597 0799549690		-1.49504950	.831125828	.2504 14 594	0503	1.02
1.03	0783337753 0767558597	.490291262 .487179487	-1.49261084  -1.49019608	.830033003 .828947368	.250620347 .250825083	0505	1.03
1.05 1.06	0752197650 0737240950	.484126984 .481132075	-1.48780488 -1.48543689	.827868852 .826797386	.251028807 .251231527	0508	1.05
1.07	0722675093	.478193146	-1.48309179	.825732899	.251433251	0512	1.07
1.08 1.09	0708487227 0694665010	.475308642 .472477064	-1.48076923 -1.47846890	.824675325 .823624595	.251633987	0513	1.08
		.469696970	-1.47619048	.822580645	.252032520	0517	1.10
1.10	0681196590 0668070587	.466966967	-1.47393365	.821543408	.252230333	0518	1.11
1.12	0655276060	.4642 <b>8</b> 5714 .461651917	-1.47169811 -1.46948357	.820512821 .819488818	.252427184 .252623083	0520	1.12
1.13 1.14	0642802503 0630639807	.459064327	-1.46728972	.818471338	.252818035	0523	1.14
1.15	0618778257	.456521739	-1.46511628	.817460317	.253012048	0525	1.15
1.16	0607208500	.454022989	-1.46296296	.816455696	.253205128	0527	1.16
1.17 1.18	0595921540 0584908717	.451566952 .449152542	-1.46082949 -1.45871560	.815457413 .814465409	.253397282 .253588517	0528	1.17
1.19	0574161693	.446778711	-1.45662100	.813479624	.253778838	0532	1.19
1.20	0563672440	.44444444	-1.45454545	.812500000	.253968254	0533	1.20
1.21	0553433220	.442148760	-1.45248869	.811526480 .810559006	.254156770 .254344392	0535 0537	1.21 1.22
1.22 1.23	0543436580 0533675337	.437669377	-1.45045045 -1.44843049	.809597523	.254531127	0538	1.23
1.24	0524142559	.435483871	-1.44642857	.808641975	.254716981	0540	1.24
1.25	0514831573	.433333333	-1.4444444	.807692308	.254901961	0542	1.25
1.26	0505735933	.431216931 .429133858	-1.44247788 -1.44052863	.806748466 .805810398	.255086072 .255269321	0543 0545	1.26 1.27
1.27	0496849423 0488166042	.427083333	-1,43859649	.804878049	.255451713	0547	1.28
1.29	0479680003	.425064599	-1.43668122	.803951368	.255633256	0548	1.29
						LE1	
	- 101	- 101	- 101	- 1c1	- (C)		$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$
	- 4C4	- 1C3	- 4C2	401	400	b <sup>4</sup> f <sup>(5)</sup> (£)	cba



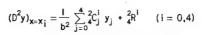


		~~	i b = 0 4-J	, ,		- Color	مر مرکز
r= <u>a</u> = <u>a</u> = <u>a</u>	1C4 4Cc	1 C4	1C4 4C2	1C4 4C3	1C4	$\frac{\int_{4}^{1} E^{4}}{D^{4} f^{(5)}(\varepsilon)}$	
0.10 .11 .12 .13	8.37871806 7.48846393 6.74934342 6.12640232 5.59467602	-10.3333333 - 9.42424242 - 8.66666667 - 8.02564103 - 7.47619048	4.22727273 4.20270270 4.17857143 4.15486726	-4.42857143 -4.42180095 -4.41509434 -4.40845070 -4.40186916	2.15591398 2.15487674 2.15384615 2.15282215 2.15180467	0.1550 .1555 .1560 .1565 .1570	0.10 .11 .12 .13
.15 .16 .17 .18	5.13585953 4.73622630 4.38528144 4.07486405 3.79853288	- 7.00000000 - 6.58333333 - 6.21568627 - 5.88888889 - 5.59649123	4.08620690 4.06410256 4.04237288	-4.39534884 -4.38888889 -4.38248848 -4.37614679 -4.36986301	2.15079365 2.14978903 2.14879075 2.14779874 2.14681296	.1575 .1580 .1585 .1590 .1595	.15 .16 .17 .18
.20 .21 .22 .23	3,55113636 3,32850550 3,12723050 2,94449565 2,77795557	- 5.33333333 - 5.09523810 - 4.87878788 - 4.68115942 - 4.50000000	3.97933884 3.95901639 3.93902439	-4.36363636 -4.35746606 -4.35135135 -4.34529148 -4.33928571	2.14583333 2.14485981 2.14389234 2.14293086 2.14197531	.1600 .1605 .1610 .1615 .1620	.20 .21 .22 .23 .24
.25 .26 .27 .28 .29	2.62564103 2.48588663 2.35727448 2.23859000 2.12878677	- 4.33333333 - 4.17948718 - 4.03703704 - 3.90476190 - 3.78160920	3.88095238 3.8622 <b>0472</b> 3.84375000	-4.3333333 -4.32743363 -4.32158590 -4.31578947 -4.31004367	2.14102564 2.14008180 2.13914373 2.13821138 2.13728470	.1625 .1630 .1635 .1640 .1645	.25 .26 .27 .28 .29
.30 .31 .32 .33	2.02695855 1.93231661 1.84417136 1.76191728 1.68502058	- 3.66666667 - 3.55913978 - 3.45833333 - 3.36363636 - 3.27450980	3.77272727 3.75563910	-4.30434783 -4.29870130 -4.29310345 -4.28755365 -4.28205128	2.13636364 2.13544814 2.13453815 2.13363363 2.13273453	.1650 .1655 .1660 .1665 .1670	.30 .31 .32 .33
.35 .36 .37 .38 .39	1.61300892 1.54546282 1.48200856 1.42231212 1.36607406	- 3.19047619 - 3.11111111 - 2.03603604 - 2.96491228 - 2.89743590	3.67391304	-4.27659574 -4.27118644 -4.26582278 -4.26050420 -4.25523013	2.13184080 2.13095238 2.13006924 2.12919132 2.12831858	.1675 .1680 .1685 .1690 .1695	.35 .36 .37 .38
.40 .41 .42 .43	1.31302521 1.26292296 1.21554809 1.17070201 1.12820446	- 2.83333333 - 2.77235772 - 2.71428571 - 2.65891473 - 2.60606061	3.64285714 3.62765957 3.61267606 3.59790210 3.583333333	-4.2500000 -4.24481328 -4.23966942 -4.23456790 -4.22950820	2.12745098 2.12658847 2.12573099 2.12487852 2.12403101	.1700 .1705 .1710 .1715 .1720	.40 .41 .42 .43
.45 .46 .47 .48	1.08789143 1.04961338 1.01323371 .978627404 .945679834	- 2.5555556 - 2.50724638 - 2.46099291 - 2.41666667 - 2.37414966	3.54081633 3.52702703	-4.22448980 -4.21951220 -4.21457490 -4.20967742 -4.20481928	2.12318841 2.12235067 2.12151777 2.12068966 2:11986628	.1725 .1730 .1735 .1740 .1745	.45 .46 .47 .48
.50 .51 .52 .53	.914285714 .884348185 .855777994 .828492771 .802416390	- 2.33333333 - 2.29411765 - 2.25641026 - 2.22012579 - 2.18518519	3.50000000 3.48675497 3.47368421 3.46078431 3.44805195	-4.20000000 -4.19521912 -4.19047619 -4.18577075 -4.18110236	2.11904762 2.11823362 2.11742424 2.11661945 2.11581921	.1750 .1755 .1760 .1765 .1770	.50 .51 .52 .53
.55 .56 .57 .58	.777478394 .753613486 .730761070 .708864842 .687872428	- 2.15151515 - 2.11904762 - 2.08771930 - 2.05747126 - 2.02824859	3.43548387 3.42307692 3.41082803 3.39873418 3.38679245	-4.17647059 -4.17187500 -4.16731518 -4.16279070 -4.15830116	2.11502347 2.11423221 2.11344538 2.11266294 2.11188487	.1775 .1780 .1785 .1790 .1795	.55 .56 .57 .58
.60 .61 .62 .63	.612013107	- 2.00000000 - 1.97267760 - 1.94623656 - 1.92063492 - 1.89583333	3.36335404 3.35185185 3.34049080	-4.15384615 -4.14942529 -4.14503817 -4.14068441 -4.13636364	2.1111111 2.11034164 2.10957643 2.10881543 2.10805861	.1800 .1805 .1810 .1815	.60 .61 .62 .63
.65 .66 .67 .68	.578382589 .562518105 .547246069 .532537804 .518366359	- 1.87179487 - 1.84848485 - 1.82587065 - 1.80392157 - 1.78260870	3.30722892 3.29640719 3.28571429	-4.13207547 -4.12781955 -4.12359551 -4.11940299 -4.11524164	2.10730594 2.10655738 2.10581290 2.10507246 2.10433604	.1825 .1830 .1835 .1840 .1845	.65 .66 .67 .68
	- <sup>1</sup> C <sup>0</sup> <sub>4</sub>	- <sup>1</sup> C <sup>0</sup> <sub>3</sub>	- <sup>1</sup> <sub>4</sub> C <sub>2</sub> <sup>0</sup>	- <sup>1</sup> C0	- <sup>1</sup> C 0	$\frac{{}_{4}^{1}E^{0}}{b^{4}f^{(5)}(\varepsilon)}$	p= <u>d</u> = <u>d</u> =

(D <sup>1</sup> y) <sub>x=x1</sub> =	$\frac{1}{b}$	$\sum_{j=0}^{4}$	Cj	y <sub>j</sub> +	4R1	(i = 4.0)
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			3				
r= <u>a=a=a</u> b c d	1C4	· 104	1C4 4C2	1C4 4C3	4C4	$\frac{{}^{1}E^{4}}{{}^{4}f^{(5)}(z)}$	
0.70 .71 .72 .73 .74	0.504706387 .491534030 .478826815 .466563552 .454724252	-1.76190476 -1.74178404 -1.72222222 -1.70319635 -1.68468468	3.26470588 3.25438596 3.24418605 3.23410405 3.22413793	-4.1111111 -4.10701107 -4.10294118 -4.09890110 -4.09489051	2.10360360 2.10287511 2.10215054 2.10142985 2.10071301	.1850 .1855 .1860 .1865 .1870	.70 .71 .72 .73
.75 .76 .77 .78	.443290043 .432243094 .421566546 .411244450 .401261706	-1.66666667 -1.64912281 -1.63203463 -1.61538462 -1.59915612	3.21428571 3.20454545 3.19491525 3.18539326 3.17597765	-4.09090909 -4.08695652 -4.08303249 -4.07913669 -4.07526882	2.10000000 2.09929078 2.09858532 2.09788360 2.09718558	.1875 .1880 .1885 .1890	.75 .76 .77 .78 .79
.80 .81 .82 .83	.391604010 .382257805 .373210228 .364449081 .355962768	-1.58333333 -1.56790123 -1.55284553 -1.53815261 -1.52380952	3.16666667 3.15745856 3.14835165 3.13934426 3.13043478	-4.07142857 -4.06761566 -4.06382979 -4.06007067 -4.05633803	2.09649123 2.09580052 2.09511344 2.09442994 2.09375000	.1900 .1905 .1910 .1915 .1920	.80 .81 .82 .83
.85 .86 .87 .88	.347740287 .339771162 .332045447 .324553663 .317286793	-1.50980392 -1.49612403 -1.48275862 -1.46969697 -1.45692884	3.12162162 3.11290322 3.10427807 3.09574468 3.08730159	-4.05263158 -4.04895105 -4.04529617 -4.04166667 -4.03806228	2.09307359 2.09240069 2.09173127 2.09106529 2.09040274	.1925 .1930 .1935 .1940 .1945	.85 .86 .87 .88
.90 .91 .92 .93	.310236245 .303393830 .296751741 .290302531 .284039091	-1.44444444 -1.43223443 -1.42028986 -1.40860215 -1.39716312	3.07894737 3.07068063 3.06250000 3.05440414 3.04639175	-4.03448276 -4.03092784 -4.02739726 -4.02389078 -4.02040816	2.08974359 2.08908781 2.08843537 2.08778626 2.08714044	.1950 .1955 .1960 .1965 .1970	.90 .91 .92 .93
.95 .96 .97 .98	.277954637 .272042682 .266297037 .260711776 .255281237	-1.38596491 -1.3750000 -1.36426117 -1.35374150 -1.34343434	3.03846154 3.03061224 3.02284264 3.01515152 3.00753769	-4.01694915 -4.01351351 -4.01010101 -4.00671141 -4.00334448	2.08649789 2.08585859 2.08522250 2.08458961 2.08395990	.1975 .1980 .1985 .1990 .1995	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	.250000000 .244862879 .239864907 .235001326 .230267579	-1.33333333 -1.32343234 -1.31372549 -1.30420712 -1.29487179	3.00000000 2.99253731 2.98514851 2.97783251 2.97058824	-4.00000000 -3.99667774 -3.99337748 -3.99009901 -3.98684211	2.08333333 2.08270989 2.08208955 2.08147229 2.08085809	.2000 .2005 .2010 .2015 .2020	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	.225659295 .221172285 .216802528 .212546168 .208399503	-1.28571429 -1.27672956 -1.26791277 -1.25925926 -1.25076453	2.96341463 2.95631068 2.94927536 2.94230769 2.93540670	-3.98360656 -3.98039216 -3.97719870 -3.97402597 -3.97087379	2.08024691 2.07963875 2.07903358 2.07843137 2.07783211	.2025 .2030 .2035 .2040 .2045	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	.204358977 .200421176 .196582818 .192840751 .189191942	-1.24242424 -1.23423423 -1.22619048 -1.21828909 -1.21052632	2.92857143 2.92180095 2.91509434 2.90845070 2.90186916	-3.96774194 -3.96463023 -3.96153846 -3.95846645 -3.95541401	2.07723577 2.07664234 2.07605178 2.07546408 2.07487923	.2,050 .2055 .2060 .2065 .2070	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	.185633477 .182162550 .178776462 .175472615 ,172248508	-1.20289855 -1.19540230 -1.18803419 -1.18079096 -1.17366947	2.89534884 2.88888889 2.88248848 2.87614679 2.86986301	-3.95238095 -3.94936709 -3.94637224 -3.94339623 -3.94043887	2.07429719 2.07371795 2.07314149 2.07256778 2.07199682	.2075 .2080 .2085 .2090 .2095	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	.169101732 .166029966 .163030974 .160102601 .157242768	-1.16666667 -1.15977961 -1.15300546 -1.14634146 -1.13978495	2.86363636 2.85746606 2.85135135 2.84529148 2.83928571	-3.93750000 -3.93457944 -3.93167702 -3.92879257 -3.92592593	2.07142857 2.07086302 2.07030016 2.06973995 2.06918239	.2100 .2105 .2110 .2115 .2120	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	.154449472 .151720780 .149054827 .146449813 .143904001	-1.13333333 -1.12698413 -1.12073491 -1.11458333 -1.10852713	2.83333333 2.82743363 2.82158590 2.81578947 2.81004367	-3.92307692 -3.92024540 -3.91743119 -3.91463415 -3.91185410	2.06862745 2.06807512 2.06752537 2.06697819 2.06643357	.2125 .2130 .2135 .2140 .2145	1.25 1.26 1.27 1.28 1.29
	- 1C0	- <sup>1</sup> C <sup>0</sup> <sub>3</sub>	- 1C0	- 1C0	- <sup>1</sup> C <sup>0</sup>	b <sup>4</sup> f <sup>(5)</sup> (£)	p=d=d=c c b a



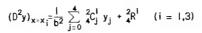


			•			•	
= <u>a</u> =a=a b c d	<sup>2</sup> C <sup>0</sup> <sub>4</sub>	<sup>2</sup> C <sup>0</sup>	<sup>2</sup> C <sup>0</sup> <sub>4</sub> C <sup>2</sup>	<sup>2</sup> C <sup>0</sup> <sub>4</sub>	<sup>2</sup> C <sub>4</sub> <sup>0</sup>	$\frac{{}_{4}^{2}E^{0}}{b^{3}f^{(5)}(z)}$	
0.10 .11 .12 .13 .14	35.9167714 32.5813081 29.8015009 27.4491414 25.4326512	-40.7666667 -37.4433333 -34.6755556 -32.3351282 -30.3304762	6.39090909 6.42909910 6.46714286 6.50504425 6.54280702	-1.82380952 -1.85606635 -1.88830189 -1.92051643 -1.95271028	0.282795699 .288992497 .295213675 .301458999 .307728238	-0.1397 1441 1484 1529 1574	0.10 .11 .12 .13 .14
.15 .16 .17 .18	23.6848722 22.1554351 20.8058216 19.6060726 18.5325355	-28.5944444 -27.0766667 -25.7386275 -24.5503704 -23.4882456	6.58043478 6.61793103 6.65529915 6.69254237 6.72966387	-1.98488372 -2.01703704 -2.04917051 -2.08128440 -2.11337900	.314021164 .320337553 .326677182 .333039832 .339425287	1620 1666 1713 1761 1810	.15 .16 .17 .18
.20 .21 .22 .23	17.5662879 16.6920113 15.8971720 15.1714157 14.5061136	-22.5333333 -21.6703175 -20.8866667 -20.1720290 -19.5177778	6.76666667 6.80355372 6.84032787 6.87699187 6.91354839	-2.14545455 -2.17751131 -2.20954955 -2.24156951 -2.27357143	.345833333 .352263759 .358716356 .365190918 .371687243	1859 1908 1959 2010 2062	.20 .21 .22 .23 .24
.25 .26 .27 .28 .29	13.8940171 13.3289926 12.8058151 12.3200054 11.8677024	-18.9166667 -18.3625641 -17.8502469 -17.3752381 -16.9336782	6.95000000 6.98634921 7.02259843 7.05875000 7.09480620	-2.30555556 -2.33752212 -2.36947137 -2.40140351 -2.43331878	.378205128 .384744376 .391304791 .397886179 .404488349	2115 2168 2222 2277 2332	.25 .26 .27 .28 .29
.30 .31 .32 .33	11.445593 11.0506611 10.6804569 10.3327052 10.0054276	-16.5222222 -16.1379570 -15.7783333 -15.4411111 -15.1243137	7.13076923 7.16664122 7.20242424 7.23812030 7.27373134	-2.46521739 -2.49709957 -2.52896552 -2.56081545 -2.59264951	.41111111 .417754280 .424417671 .431101101 .437804391	2388 2445 2502 2561 2620	.30 .31 .32 .33
.35 .36 .37 .38	9.69687194 9.40548065 9.12986434 8.86877980 8.62111123	-14.2799099	7.30925926 7.34470588 7.38007299 7.41536232 7.45057554	-2.62446809 -2.65627119 -2.68805907 -2.71983193 -2.75158996	.444527363 .451269841 .458031652 .464812623 .471612586	2679 2740 2801 2863 2926	.35 .36 .37 .38
.40 .41 .42 .43	8.38585434 8.16210271 7.94903619 7.74591082 7.55205024	-15.5666667 -13.3530894 -13.1501587 -12.9571318 -12.7733333	7.48571429 7.52078014 7.55577465 7.59069930 7.62555556	-2.78333333 -2.81506224 -2.84677686 -2.87847737 -2.91016393	.478431373 .485268817 .492124756 .498999028 .505891473	2989 3054 3119 3184 3251	.40 .41 .42 .43
.45 .46 .47 .48	7.36683812 7.18971168 7.02015598 6.85769891 6.70190689		7.66034483 7.69506849 7.72972789 7.76432432 7.79885906	-2.94183673 -2.97349593 -3.00514170 -3.03677419 -3.06839357	.512801932 .519730250 .526676273 .533639847 .540620821	3318 3386 3455 3525 3595	.45 .46 .47 .48
.50 .51 .52 .53	6.55238095 6.40875339 6.27068472 6.13786108 6.00999177	-11.8333333 -11.6995425 -11.5712821 -11.4482390 -11.3301235	7.83333333 7.86774834 7.90210526 7.93640523 7.97064935	-3.10000000 -3.13159363 -3.16317460 -3.19474308 -3.22629921	.547619048 .554634378 .561666667 .568715770 .575781544	3667 3739 3812 3885 3960	.50 .51 .52 .53
.55 .56 .57 .58	5.88680724 5.76805714 5.65350866 5.54294501 5.43616408	-11.2166667 -11.1076190 -11.0027485 -10.9018391 -10.8046893	8.00483871 8.03897436 8.07305732 8.10708861 8.14106918	-3.25784314 -3.28937500 -3.32089494 -3.35240310 -3.38389961	.582863850 .589962547 .597077498 .604208566 .611355617	4035 4111 4188 4266 4345	.55 .56 .57 .58
.60 .61 .62 .63	5.33297721 5.23320807 5.13669171 5.04327361 4.95280888		8.17500000 8.20888199 8.24271605 8.27650307 8.31024390	-3.41538462 -3.44685824 -3.47832061 -3.50977186 -3.54121212	.618518519 .625697138 .632891344 .640101010 .647326007	4424 4504 4585 4667 4750	.60 .61 .62 .63
.65 .66 .67 .68 .69	4.86516155 4.78020385 4.69781564 4.61788382 4.54030182	-10.2155556 -10.1426368 -10.0721569	8.34393939 8.37759036 8.41119760 8.44476190 8.47828402	-3.57264151 -3.60406015 -3.63546816 -3.66686567 -3.69825279	.654566210 .661821494 .669091735 .676376812 .683676603	4834 4918 5004 5090 5177	.65 .66 .67 .68
	<sup>2</sup> C <sup>4</sup>	<sup>2</sup> C <sup>4</sup> <sub>4</sub> <sup>5</sup>	<sup>2</sup> C <sup>4</sup> <sub>4</sub>	2C4	<sup>2</sup> C <sup>4</sup>	$-\frac{{}_{4}^{2}E^{4}}{b^{3}f^{(5)}(\xi)}$	p=ddd cba

 $(D^2y)_{x=x_i} = \frac{1}{b^2} \sum_{j=0}^{4} {}_{4}^{2}C_{j}^{i} y_j + {}_{4}^{2}R^{i}$  (i = 0.4)



r=a_a_a	2C0	<sup>2</sup> C <sup>0</sup>	<sup>2</sup> <sub>4</sub> C <sub>2</sub> <sup>0</sup>	<sup>2</sup> C <sup>0</sup> <sub>4</sub>	<sup>2</sup> C <sup>0</sup>	$\frac{{}^{2}_{4}E^{0}}{{}^{3}f^{(5)}(E)}$	
0.70 .71 .72 .73	4.46496917 4.39179102 4.32067780 4.25154481 4.18431194	-9.93809525 -9.87431925 -9.81259260 -9.75283105 -9.69495495	8.51176471 8.54520468 8.57860465 8.61196532 8.64528736	-3.72962963 -3.76099631 -3.79235294 -3.82369963 -3.85503650	0.690990991 .698319856 .705663082 .713020554 .720392157	-0.5265 5354 5444 5535 5626	0.70 .71 .72 .73 .74
.75 .76 .77 .78	4.11890332 4.05524708 3.99327506 3.93292259 3.87412827	-9.63888890 -9.58456140 -9.53190475 -9.48085470 -9.43135020	8.67857143 8.71181818 8.74502825 9.77820225 8.81134078	-3.88636364 -3.91768116 -3.94898917 -3.98028777 -4.01157706	.72777778 .735177305 .742590628 .750017637 .757458223	5719 5812 5906 6002 6098	.75 .76 .77 .78
.80 .81 .82 .83	3.81683375 3.76098357 3.70652494 3.65340766 3.60158383	-9.38333333 -9.33674897 -9.29154471 -9.24767068 -9.20507936	8.8444444 8.87751381 8.91054945 8.94355191 8.97652174	-4.04285714 -4.07412811 -4.10539007 -4.13664311 -4.16788732	.764912281 .772379703 .779860384 .787354221 .794861111	6195 6293 6391 6491 6592	.80 .81 .82 .83 .84
.85 .86 .87 .88	3.55100790 3.50163630 3.45342760 3.40634215 3.36034212	-9.16372549 -9.12356589 -9.08455939 -9.04666667 -9.00985019	9.00945946 9.04236559 9.07524064 9.10808511 9.14089947	-4.19912281 -4.23034965 -4.26156794 -4.29277778 -4.32397924	.802380952 .809913644 .817459087 .825017182 .832587832	6694 6796 6900 7004 7110	.85 .86 .87 .88
.90 .91 .92 .93	3.31539134 3.27145522 3.22850067 3.18649606 3.14541102	-8.97407407 -8.93930403 -8.90550725 -8.87265233 -8.84070922	9.17368421 9.20643979 9.23916667 9.27186528 9.30453608	-4.35517241 -4.38635739 -4.41753425 -4.44870307 -4.47986395	.840170940 .847766411 .855374150 .862994063 .870626058	7216 7323 7432 7541 7651	.90 .91 .92 .93
.95 .96 .97 .98	3.10521655 3.06588476 3.02738899 2.98970360 2.95280403	-8.80964912 -8.77944444 -8.75006873 -8.72149660 -8.69370370	9.33717949 9.36979592 9.40238579 9.43494949 9.46748744	-4.51101695 -4.54216216 -4.57329966 -4.60442953 -4.63555184	.878270042 .885925926 .893593619 .901273032 .908964077	7762 7875 7988 8102 8217	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	2.91666667 2.88126885 2.84658878 2.81260554 2.77929898	-8.66666667 -8.64036304 -8.61477124 -8.58987055 -8.56564103	9.50000000 9.53248756 9.56495050 9.59738916 9.62980392	-4.66666667 -4.69777409 -4.72887417 -4.75996700 -4.79105263	.916666667 .924380715 .932106136 .939842845 .947590759	8333 8450 8569 8688 8808	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	2.74664972 2.71463914 2.68324926 2.65246282 2.62226316	-8.54206349 -8.51911950 -8.49679128 -8.47506173 -8.45391437	9.66219512 9.69456311 9.72690821 9.75923077 9.79153110	-4.82213115 -4.85320261 -4.88426710 -4.91532468 -4.94637540	.955349794 .963119869 .970900901 .978692810 .986495518	8929 9051 9175 9299 9424	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	2.59263422 2.56356054 2.53502718 2.50701976 2.47952437	-8.43333333 -8.41330330 -8.39380952 -8.37483776 -8.35637427	9.82380952 9.85606635 9.88830189 9.92051643 9.95271028	-4.97741935 -5.00845659 -5.03948718 -5.07051118 -5.10152866	.994308943 1.00213301 1.00996764 1.01781275 1.02566828	9551 9678 9807 9936 -1.0067	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	2.45252763 2.42601655 2.39997865 2.37440184 2.34927443	-8.33840580 -8.32091954 -8.30390313 -8.28734463 -8.27123249	9.98488372 10.0170370 10.0491705 10.0812844 10.1133790	-5.13253968 -5.16354430 -5.19454259 -5.22553459 -5.25652038	1.03353414 1.04141026 1.04929656 1.05719298 1.06509944	-1.0199 -1.0331 -1.0465 -1.0599 -1.0735	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	2.32458514 2.30032304 2.27647757 2.25303851 2.22999597	-8.2555556 -8.24030303 -8.22546449 -8.21102981 -8.19698925	10.1775113 10.2095495 10.2415695	-5.28750000 -5.31847352 -5.34944099 -5.38040248 -5.41135802	1.07301587 1.08094220 1.08887836 1.09682427 1.10477987	-1.0872 -1.1010 -1.1149 -1.1289 -1.1431	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	2.20734037 2.18506244 2.16315321 2.14160395 2.12040626	-8.15713911	10.3055556 10.3375221 10.3694714 10.4014035 10.4333188	-5.44230769 -5.47325153 -5.50418960 -5.53512195 -5.56604863	1.11274510 1.12071987 1.12870414 1.13669782 1.14470085	-1.1573 -1.1717 -1.1861 -1.2007 -1.2154	1.25 1.26 1.27 1.28 1.29
	2°C4	<sup>2</sup> C <sup>4</sup> <sub>4</sub>	<sup>2</sup> C <sup>4</sup> <sub>4</sub>	2C 4	<sup>2</sup> <sub>4</sub> C <sub>0</sub> <sup>4</sup>	$-\frac{{}_{4}^{2}E^{4}}{{}_{5}^{3}f^{(5)}(E)}$	p= <u>d_d_d</u> c_b_a





			<u> </u>			<sup>2</sup> E <sup>1</sup>	
_ <u>a_a_a</u> b c d	<sup>2</sup> C <sub>0</sub> 1	2C	<sup>2</sup> C <sub>2</sub>	<sup>2</sup> C <sup>1</sup> <sub>3</sub>	<sup>2</sup> C <sub>4</sub> <sup>1</sup>	b <sup>3</sup> f <sup>(5)</sup> (£)	
	<u> </u>						0.10
0.10	30.7219662	-34,6666667	5.00000000	-1.23809254	0.182795699	-0.0817 0798	0.10
.11	27.4577011	-31.3333333	4.90990991	-1.21327014	.178992497	0780	.12
.12	24.7475926	~28.555556	4.82142857	-1.18867925 -1.16431925	.175213675 .171458999	0762	.13
.13	22.4634752	-26.2051282 -24.1904762	4.73451327 4.64912281	-1.14018692	.167728238	0743	.14
		00 444444	4 56501770	-1.11627907	.164021164	0725	.15
.15	18.8314850	-22.444444 -20.9166667	4.56521739 4.48275862	-1.09259259	.160337553	0707	.16
.16	17.3661631	-19.5686275	4.40170940	-1.06912442	.156677182	0688	.17
.17		-18.3703704	4.32203390	-1.04587156	.153039832	0670	.18
.18 .19	14.9411682 13.9279539	-17.2982456	4.24369748	-1.02283105	.149425287	0652	.19
.20	13.0208333	-16.3333333	4.16666667	-1.00000000	.145833333	0633	.20
.21	12,2045202	-15.4603175	4.09090909	977375565	.142263759	0615	.21
.22	11.4665118	-14.6666667	4.01639344	954954954	.138716356	0597	.22
.23	10.7964841	-13.9420290	3.94308943	932735426	.135190918	0578	.23
.24	10.1858371	-13.2777778	3.87096774	910714285	.131687243	0560	.24
.25	9.62735043	-12.6666667	3.80000000	88888889	.128205128	0542	.25
.26	9.11491763	-12.1025641	3.73015873	867256637	.124744376	0523	.26
.27	8,64333978	-11.5802469	3.66141732	845814978	.121304791	0505	.27
.28	8.20816332	-11.0952381	3.59375000	824561404	.117886179	0487	.28
.29	7.80555148	-10.6436782	3.52713178	803493450	.114488349	0468	.29
.30	7.43218135	-10.2222222	3.46153846	782608696	.111111111	0450	.30
.31	7.08516091	- 9.82795699	3.39694656	761904762	.107754280	0432	.31
.32	6.76196164	- 9.45833333	3.33333333	741379310	.104417671	0413	.32
.33	6.46036336	- 9.11111111	3.27067669	721030043	.101101101	0395	.33
.34	6.17840881	- 8.78431373	3.20895522	700854701	.0978043912	037/	.34
.35	5.91436603	- 8.47619048	3.14814815	680851064	.0945283632	0358	.35
.36	5.66669700	- 8.18518519	3.08823529	661016949	.0912698413	0340	.36
.37	5.43403139	- 7.90990991	3.02919708	641350211	.0880316518	0322	.37
.38	5.21514443	- 7.64912281	2.97101449	621848739	.0848126233	0303	38
.39	5.00893821	- 7.40170940	2.91366906	6025104€∂	.0816125860	0285	.39
.40	4.81442577	- 7.16666667	2.85714286	583333333	.0784313725	0267	.40
.41	4.63071753	- 6.94308943	2.80141844	564315353	.0752688172	0248	.41
. 42	4.45700965	- 6.73015873	2.74647887	545454545	.0721247563	0230	.42
. 43	4.29257403	- 6.52713178	2.69230769	526748971	.0689990282	0212	.43
. 44	4.13674969	- 6.33333333	2.63888889	508196121	.0658914729	0193	.44
. 45	3.98893524	- 6.14814815	2.58620690	489795918	.0628019324	0175	. 45
. 46	3.84858238	- 5.97101449	2.53424658	471544715	.0597302505	0157	.46
. 47	3.71519027	- 5.80141844	2.48299320	453441296	.0566762728	0138	.47
. 48	3.58830048	- 5.63888889	2.43243243	435483872	.0536398467	0120	.48
. 49	3.46749272	- 5,48299320	2.38255034	417670683	.0506208214	0102	. 49
.50	3.35238095	- 5.33333333	2.33333333	400000000	.0476190476	0083	.50
.51	3.24261001	- 5.18954248	2.28476821	382470120	.0446343780	0065	.51
.52	3.13785265	- 5.05128205	2.23684211	365079365	.0416666667	0047	.52
.53	3.03780683	- 4.91823899	2.18954248	347826087	.0387157696	0028	.53
.54	2.94219343	- 4.79012346	2.14285714	330708661	.0357815443	0010	.54
. 55	2.85075411	- 4.66666667	2.09677419	313725490	.0328638498	.0008	.55
.56	2.76324945	- 4.54761905	2.05128205	296875000	.0299625468	.0027	.56
.57	2.67945726	- 4.43274854	2.00636943	280155642	.0270774977	.0045	.57
•58	2.59917109	- 4.32183908	1.96202532	263565891	.0242085661	.0063	.58
.59	2.52219890	- 4.21468927	1,91823899	247104247	.0213556175	.0082	.59
.60	2.44836182	- 4.11111111	1.87500000	230769231	.0185185185	.0100	.60
.61	2.37749307	- 4.01092896	1.83229814	214559388	.0156971376	.0118	.61
.62 .63	2.30943698	- 3.91397849	1.79012346	198473282	.0128913444	.0137	. 62
n 1	2.24404806 2.18119025	- 3.82010582 - 3.72916667	1.74846626 1.70731707	182509506 166666667	.0101010101 .00732600733	.0155 .0173	.63
.64	0.3000000	- 3.64102564	1.66666667	150943396	.00456621005	.0192	• 65
.64 .65	2.12073616			135338346	.00182149362	.0210	.66
.64 .65 .66	2.06256638	- 3.5555556	1.62650602		000000000000000000000000000000000000000		
.64 .65 .66	2.06256638 2.00656892	- 3.5555556 - 3.47263682	1.58682635	119850187	000908265213	.0228	.67
.64 .65 .66 .67	2.06256638	- 3.5555556			<pre>0009082652130036231884100632339657</pre>		
.64 .65 .66	2.06256638 2.00656892 1.95263862	- 3.5555556 - 3.47263682 - 3.39215686	1.58682635 1.54761905	119850187 104477612	00362318841	.0228 .0247 .0265	.67 .68 .69
.64 .65 .66 .67	2.06256638 2.00656892 1.95263862	- 3.5555556 - 3.47263682 - 3.39215686	1.58682635 1.54761905	119850187 104477612	00362318841	.0228 .0247	.67

$(D^2y)_{x=x} = \frac{1}{b^2}$	$\sum_{j=0}^{4}$	2Cj	уį	+ 4Ri	(i =	1,3)
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			$x=x_i$ b <sup>2</sup> $\underset{j=0}{\longleftarrow}$ 4°J	•		and in	~
= a a a	<sup>2</sup> C <sub>0</sub> <sup>1</sup>	<sup>2</sup> C <sup>1</sup>	2C1.	<sup>2</sup> <sub>4</sub> C <sub>3</sub> <sup>1</sup>	<sup>2</sup> C <sup>1</sup>	$\frac{{}^{2}_{4}E^{1}}{b^{3}f^{(5)}(z)}$	
b c d	+ 0						0.70
0.70	1.85059009	- 3.23809524	1.47058824	-0.074074074	-0.00900900901	0.0283	0.70
.71	1.80229144	- 3.16431925	1.43274854	059040590	0116801438	.0302	.71
.72	1.75569832	- 3.09259259	1.39534884	044117647	0143369188	.0320	.72
.73	1.71073302	- 3.02283105	1.35838150	029304029	0169794459	.0338	.73
.74	1.66732226	- 2.95495495	1.32183908	014598540	0196078431	.0357	.74
		0.0000000	1 00571490	0	022222222	.0375	.75
.75	1.62539683	- 2.88888889	1.28571429		0248226950	.0393	.76
.76	1.58489134	- 2.82456140	1.25000000	.014492754		.0412	.77
.77	1.54574400	- 2.76190476	1.21468927	.028880866	0274093722		.78
.78	1.50789632	- 2.70085470	1.17977528	.043165468	0299823633	.0430	
.79	1.47129292	- 2.64135021	1.14525140	.057347670	0325417766	.0448	.79
.80	1.43588137	- 2.58333333	1.11111111	.071428571	0350877193	.0467	.80
.81	1.40161195	- 2.52674897	1.07734807	.085409253	0376202975	.0485	.81
.82	1.36843750	- 2.47154472	1.04395604	.099290780	0401396161	.0503	. 82
	1.33631330	- 2.41767068	1.01092896	.113074205	0426457789	.0522	. 83
. 83 . 84	1.30519682	- 2.36507936	.978260869		0451388889	.0540	. 84
		0 51770540	0.450.450.46	140350077	0476190476	,0558	. 85
. 85	1.27504772	- 2.31372549	.945945946	.140350877	0500863558	.0577	.86
. 86	1.24582760	- 2.26356589	.913978494	.153846154		.0595	.87
.87	1.21749997	- 2.21455939	.882352941	.167247387	0525409130 0549828179	.0613	.88
.88	1.19003010	- 2.16666667	.851063829	102221606	- 0574101690	.0632	.89
. 89	1.16338491	- 2.11985019	.820105820	• 199.1.110%	0574121680	.0002	.00
90	1 13753290	- 2.07407407	.789473684	206896552	0598290598	.0650	.90
.90	1.13753290	- 2.02930403	.759162303		0622335891	.0668	.91
.91	1.11244404	- 1.98550725	.729166667		0646258503	.0687	.92
.92	1.08808972		.699481865	.245733788	0670059372	.0705	.93
.93 .94	1.06444261 1.04147667	- 1.94265233 - 1.90070922	.670103092		0693739425	.0723	.94
• 0 3	1,0111.01.					07.40	06
.95	1.01916700	- 1.85964912	.641025641		0717299578	.0742	.95
.96	.997489835	- 1.81944444	.612244897	.283783784		.0760	.96
.97	.976422468	- 1.78006873	.583756345		0764063812	.0778	.97
.98	.955943179	- 1.74149660	.55555556	308724832	0787269682	.0791	.98
.99	.936031202	- 1.70370370	.527638191	.321070234	0810359231	.0815	.99
	016666667	_ 1 66666667	.500000000	. 333333333	0833333333	.0833	1.00
1.00	.916666667	- 1.66666667	.472636816		0856192851	.0852	1.01
1.01	.897830555	- 1.63036304			0878938640	.0870	1.02
1.02	.879504657	- 1.59477124	.445544554			.0888	1.03
1.03	.861671529	- 1.55987055	.418719212		0901571547		1.04
1.04	.844314456	- 1.52564103	.392156863	. 201210341	0924092409	.0907	1.04
1.05	.827417416	- 1.49206349	.365853659	.393442623	0946502058	.0925	1.05
1.06	810965045	- 1.45911950	.339805825	.405228758	0968801314	.0943	1.06
1.07	.794942604	- 1,42679128	.314009662	.416938111	0990990991	.0962	1.07
1.08	.779335951	- 1.39506173	.288461538		101307190	.0980	1.08
1.09	.764131511	- 1.36391437	.263157895		103504482	.0998	1.09
		1 2222222	020005020	451630007	- 105691057	.1017	1.10
1.10	.749316249	- 1.33333333	.238095238		105691057		1.11
1.11	.734877644	- 1.30330330	.213270142		107866991	.1035	
1.12	.720803667	- 1.27380952	.188679245		110032362	.1053	1.12
1.13	.707082754	- 1.24483776	.164319249		112187248	.1072	1.13
1.14	.693703789	- 1.21637427	.140186916	. 496815287	114331723	.1090	1.14
1.15	.680656084	- 1.18840580	.116279070	.507936508	116465863	.1108	1.15
1.16	.667929349	- 1.16091954	.0925925926		118589744	.1127	1.16
1.17	.655513693	- 1.13390313	.0691244240		120703437	.1145	1.17
1.18	.643399587	- 1.10734463	.0458715596		122807018	.1163	1.18
1.19	.631577862	- 1.08123249	.0228310502		124900557	.1182	1.19
		1 0555556	0.0000000000	562500000	126984127	.1200	1.20
1.20	.620039683	- 1.05555556		.573208723	129057799	.1218	1.21
1.21	.608776541	- 1.03030303	0226244344	.583850932	131121643	.1237	1.22
1.22	.597780237	- 1.00546448	0450450450			.1255	1.23
1.23	.587042869 .576556815	981029810 956989247	0672645740 0892857143	.594427245 .604938272	133175729 135220126	.1273	1.24
1.24	•07000010	112300000					
1.25	.566314732	933333333	1111111111		137254902	.1292	1.25
1.26	.556309526	910052911	132743363	.625766871	139280125	.1310	1.26
1.27	.546534365	887139108	154185022	.636085627	141295863	.1328	1.27
1.28	.536982647	864583333	175438596		143302181	.1347	1.28
1.29	.527648002	842377261	196506550	.656534954	145299145	.1365	1.29
				0.7	2-3	2E3	44.
	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup> <sub>4</sub>	<sup>2</sup> C <sup>3</sup> <sub>4</sub>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup> <sub>4</sub> C0	b3f(5)(E)	p=-=-
	. 4 4	4-3	4 2	4 1	4 0	D T (E)	p=-=- c b a

 $(D^2y)_{x=x_2} = \frac{1}{b^2} \sum_{j=0}^{4} {}_{4}^{2}C_{j}^{2} y_{j} + {}_{4}^{2}R^{2}$ 

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			<b>J</b> -0			- Johnson	مريم
_a_a_a b c d	<sup>2</sup> C <sup>2</sup> <sub>4</sub> C <sub>0</sub>	<sup>2</sup> C <sup>2</sup>	<sup>2</sup> C <sup>2</sup>	<sup>2</sup> C <sup>2</sup> <sub>4</sub>	2C2	$\frac{{}^{2}E^{2}}{b^{3}f^{(5)}(\xi)}$	
0.10 .11 .12	-2.79290602 -2.49615464 -2.24978114	4.33333333 4.03030303 3.77777778	-2.90909091 -2.90090090 -2.89285714	1.47619048 1.47393365 1.47169811	-0.107526882 107181136 106837607	0.0150 .0148 .0147	0.10 .11 .12
.13	-2.04213411 -1.86489201 -1.71195318	3.56410256 3.38095238 3.22222222	-2.88495575 -2.87719298 -2.86956522	1.46948357 1.46728972 1.46511628	106496273 106157113	.0145	.13
.16 .17 .18	-1.57874210 -1.46176048 -1.35828802 -1.26617763	3.08333333 2.96078431 2.85185185 2.75438596	-2.86206897 -2.85470085 -2.84745763 -2.84033613	1.46296296 1.46082949 1.45871560 1.45662100	105820106 105485232 105152471 104821803 104493208	.0142 .0140 .0138 .0137 .0135	.15 .16 .17 .18
.20 .21 .22	-1.18371212 -1.10950183 -1.04241017	2.66666667 2.58730159 2.51515152	-2.83333333 -2.82644628 -2.81967213	1.45454545 1.45248869 1.45045045	104166667 103842160 103519669	.0133 .0132 .0130	.20
.23	981498550 925985190	2.44927536 2.38888889	-2.81300813 -2.80645161	1.44843049 1.44642857	103199174 102880658	.0128	.23
.25 .26 .27 .28	875213677 828628877 785758160 746196667 709595590	2.33333333 2.28205128 2.23456790 2.19047619 2.14942529	-2.80000000 -2.79365079 -2.78740157 -2.78125000 -2.77519380	1.4444444 1.44247788 1.44052863 1.43859649 1.43668122	102564103 102249489 101936799 101626016 101317123	.0125 .0123 .0122 .0120	.25 .26 .27 .28 .29
.30 .31 .32 .33	675652850 644105537 614723787 587305760 561673527	2.1111111 2.07526882 2.04166667 2.01010101 1.98039216	-2.76923077 -2.76335878 -2.75757576 -2.75187970 -2.74626866	1.43478261 1.43290043 1.43103448 1.42918455 1.42735043	101010101 100704935 100401601 100100100 0998003992	.0117 .0115 .0113 .0112	.30 .31 .32 .33
.35 .36 .37 .38	537669640 515154273 494002853 474104040 455358020	1.95238095 1.92592593 1.90090090 1.87719298 1.85470085	-2.74074074 -2.73529412 -2.72992701 -2.72463768 -2.71942446	1.42553192 1.42372881 1.42194093 1.42016807 1.41841004	0995024876 0992063492 0989119683 0986193294 0983284169	.0108 .0107 .0105 .0103 .0102	.35 .36 .37 .38
.40 .41 .42 .43	437675070 420974320 405182697 390236003 376068153	1.83333333 1.81300813 1.79365079 1.77519380 1.75757576	-2.71428571 -2.70921986 -2.70422535 -2.69930070 -2.69444444	1.41666667 1.41493776 1.41322314 1.41152263 1.40983607	0980392157 0977517107 0974658869 0971817298 0968992248	.0100 .0098 .0097 .0095	.40 .41 .42 .43
.45 .46 .47 .48	362630476 349871126 337744570 326209135 315226611	1.74074074 1.72463768 1.70921986 1.6944444 1.68027211	-2.68965517 -2.68493151 -2.68027211 -2.67567568 -2.67114094	1.40816327 1.40650407 1.40485830 1.40322581 1.40160643	0966183575 0963391137 0960614793 0957854406 0955109838	.0092 .0090 .0088 .0087 .0085	. 45 . 46 . 47 . 48 . 49
.50 .51 .52 .53	304761905 294782728 285259331 276164257 267472130	1.6666667 1.65359477 1.64102564 1.62893082 1.61728395	-2.66666667 -2.66225166 -2.65789474 -2.65359477 -2.64935065	1.4000000 1.39840637 1.39682540 1.39525692 1.39370079	0952380952 0949667616 0946969697 0944287063 0941619586	.0083 .0082 .0080 .0078	.50 .51 .52 .53
.55 .56 .57 .58	259159465 251204495 243587023 236286281 229290809	1.60606061 1.59523810 1.58479532 1.57471264 1.56497175	-2.64516129 -2.64102564 -2.63694268 -2.63291139 -2.62893082	1.39215686 1.39062500 1.38910506 1.38759690 1.38610039	0938967136 0936329588 0933706816 0931098696 0928505107	.0075 .0073 .0072 .0070	.55 .56 .57 .58
60	222578348 216135734 209948816 204004370 198290023	1.5555556 1.54644809 1.53763441 1.52910053 1.52083333	-2.62500000 -2.62111801 -2.61728395 -2.61349693 -2.60975610	1.38461538 1.38314176 1.38167939 1.38022814 1.37878788	0925925926 0923361034 0920810313 0918273645 0915750915	.0067 .0065 .0063	.60 .61 .62
65 66 67 68	192794196 187506035 182415356 177512601	1.51282051 1.50505051 1.49751244 1.49019608	-2.60606061 -2.60240964 -2.59880240 -2.59523810	1.37735849 1.37593985 1.37453184 1.37313433	0913242009 0910746812 0908265213 0905797101	.0060 .0058 .0057 .0056 .0053	.64 .65 .66 .67
.69	172788786 <sup>2</sup> C <sup>2</sup> <sup>4</sup> C <sup>4</sup>	2C <sub>4</sub> <sup>2</sup>	-2.59171598 <sup>2</sup> C <sup>2</sup> <sup>4</sup> C <sup>2</sup>	2C <sup>2</sup>	0903342366 <sup>2</sup> C <sup>2</sup> <sup>4</sup> C0	.0052 2 4 b <sup>3</sup> f <sup>(.5)</sup> (£)	$ \begin{array}{c}                                     $

$(D^2y)_{x=x_2}$	$=\frac{1}{b^2}$	$\sum_{j=0}^{4} {}^{2}C_{j}^{2}$	Уj	+	<sup>2</sup> <sub>4</sub> R <sup>2</sup>
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			D J-	•		NAC	A CONTRACT
		T				<sup>2</sup> <sub>4</sub> E <sup>2</sup>	T
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	<sup>2</sup> <sub>4</sub> C <sub>0</sub> <sup>2</sup>	<sup>2</sup> C <sup>2</sup>	<sup>2</sup> C <sup>2</sup> <sub>4</sub>	<sup>2</sup> C <sup>2</sup> <sub>4</sub>	<sup>2</sup> C <sup>2</sup> <sub>4</sub>	$\frac{4^{L}}{b^{3}f^{(5)}(\xi)}$	
0.70 .71 .72 .73	-0.168235462 163844677 159608938 155521184 151574751	1.47619048 1.46948357 1.46296296 1.45662100 1.45045045	-2.58823529 -2.58479532 -2.58139535 -2.57803468 -2.57471264	1.37037037 1.36900369 1.36764706 1.36630037 1.36496350	-0.0900900901 0898472596 0896057347 0893655049 0891265597	0.0050 .0048 .0047 .0045 .0043	0.70 .71 .72 .73
.75 .76 .77 .78	147763348 144081031 140522182 137081483 133753902	1.4444444 1.43859648 1.43290043 1.42735043 1.42194093	-2.57142857 -2.56818182 -2.56497175 -2.56179775 -2.55865922	1.36363636 1.36231884 1.36101083 1.35971223 1.35842294	0888888889 0886524822 0884173297 0881834215 0879507475	.0042 .0040 .0038 .0037 .0035	.75 .76 .77 .78
.80 .81 .82 .83	130534670 127419268 124403409 121483027 118654256	1.4166667 1.41152263 1.40650406 1.40160642 1.39682540	-2.5555556 -2.55248619 -2.54945055 -2.54644809 -2.54347826	1.35714286 1.35587189 1.35460993 1.35335689 1.35211268	0877192982 0874890639 0872600349 0870322019 0868055556	.0033 .0032 .0030 .0028 .0027	.80 .81 .82 .83
.85 .86 .87 .88	115913429 113257054 110681816 108184554 105762264	1.39215686 1.38759690 1.38314176 1.37878788 1.37453184	-2.54054054 -2.53763441 -2.53475936 -2.53191489 -2.52910053	1.35087719 1.34965035 1.34843206 1.3472222 1.34602076	0865800866 0863557858 0861326443 0859106529 0856898029	.0025 .0023 .0022 .0020	. 85 . 86 . 87 . 88 . 89
.90 .91 .92 .93	103412082 101131277 0989172470 0967675103 0946796970	1.37037037 1.36630037 1.36231884 1.35842294 1.35460993	-2.52631579 -2.52356021 -2.52083333 -2.51813472 -2.51546392	1.34482759 1.34364261 1.34246575 1.34129693 1.34013605	0854700855 0852514919 0850340136 0848176421 0846023689	.0017 .0015 .0013 .0012	.90 .91 .92 .93
.95 .96 .97 .98	0926515457 0906808940 0887656790 0869039253 0850937457	1.35087719 1.34722222 1.34364261 1.34013605 1.33670034	-2.51282051 -2.51020408 -2.50761421 -2.50505051 -2.50251256	1.33898305 1.33783784 1.33670034 1.33557047 1.33444816	0843881857 0841750842 0839630563 0837520938 0835421888	.0008 .0007 .0005 .0003 .0002	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	0833333333 0816209597 0799549690 0783337753 0767558597	1.33333333 1.33003300 1.32679739 1.32362460 1.32051282	-2.50000000 -2.49751244 -2.49504950 -2.49261084 -2.49019608	1.33333333 1.33222591 1.33112583 1.33003300 1.32894737	0833333333 0831255195 0829187396 0827129859 0825082508	a <sub>0</sub> -0.0002 0003 0005 0007	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	0752197650 0737240950 0722675093 0708487227 0694665010	1.31746032 1.31446541 1.31152648 1.30864198 1.30581040	-2.48780488 -2.48543689 -2.48309179 -2.48076923 -2.47846890	1.32786885 1.32679739 1.32573290 1.32467532 1.32362460	0823045267 0821018062 0819000819 0816993464 0814995925	0008 0010 0012 0013 0015	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	0681196590 0668070587 0655276060 0642802503 0630639807	1.30303030 1.30030030 1.29761905 1.29498525 1.29239766	-2.47619048 -2.47393365 -2.47169811 -2.46948357 -2.46728972	1.32258065 1.32154341 1.32051282 1.31948882 1.31847134	0813008130 0811030008 0809061489 0807102502 0805152979	0017 0018 0020 0021 0023	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	0618778257 0607208500 0595921540 0584908717 0574161693	1.28985507 1.28735632 1.28490028 1.28248588 1.28011204	-2.46511628 -2.46296296 -2.46082949 -2.45871560 -2.45662100	1.31746032 1.31645570 1.31545741 1.31446541 1.31347962	0803212851 0801282051 0799360512 0797448166 0795549484	0025 0027 0028 0030 0032	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	0563672440 0553433220 0543436580 0533675337 0524142559	1.27777778 1.27548209 1.27322404 1.27100271 1.26881720	-2.45454545 -2.45248869 -2.45045045 -2.44843049 -2.44642857	1.31250000 1.31152648 1.31055901 1.30959752 1.30864198	0793650794 0791765637 0789889415 0788022065 0786163522	0033 0035 0037 0038 0040	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	0514831573 0505735933 0496849423 0488166042 0479680003	1.26666667 1.26455026 1.26246719 1.26041667 1.25839793	-2.4444444 -2.44247788 -2.44052863 -2.43859649 -2.43668122	1.30769231 1.30674847 1.30581040 1.30487805 1.30395137	0784313725 0782472613 0780640125 0778816199 0777000777	0042 0043 0045 0047 0048	1.25 1.26 1.27 1.28 1.29
	<sup>2</sup> <sub>4</sub> C <sub>4</sub> <sup>2</sup>	<sup>2</sup> C <sup>2</sup> <sub>3</sub>	<sup>2</sup> <sub>4</sub> C <sup>2</sup> <sub>2</sub>	<sup>2</sup> C <sup>2</sup>	<sup>2</sup> C <sub>0</sub> <sup>2</sup>	$\frac{{}^{2}_{4}E^{2}}{b^{3}f^{(5)}(z)}$	p= <u>d=d-d</u> c b a

<sup>a</sup>The next order remainder term is 0.0111  $b^4 [f^{(6)}(x)]_{x=x_2}$ 

21(b)

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and and

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raaa b c d	<sup>2</sup> C <sub>0</sub> <sup>3</sup>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup> <sub>4</sub> C <sub>2</sub>	<sup>2</sup> C <sup>3</sup> <sub>4</sub>	<sup>2</sup> C <sup>3</sup> <sub>4</sub>	$\frac{{}^{2}E^{3}}{b^{3}f^{(5)}(E)}$	
0.10 .11 .12 .13 .14	-2.79290602 -2.49615464 -2.24978114 -2.04213411 -1.86489201	3.3333333 3.03030303 2.77777778 2.56410256 2.38095238	0.090909090 .0990990999 .107142857 .115044247 .122807018		0.892473118 .892818864 .893162393 .893503727 .893842887	-0.0683 0685 0687 0688 0690	0.10 .11 .12 .13
.15 .16 .17 .18	-1.71195318 -1.57874210 -1.46176048 -1.35828802 -1.26617763	2.2222222 2.08333333 1.96078431 1.85185185 1.75438596	.130434783 .137931034 .145299145 .152542373 .159663866	-1.53488372 -1.53703703 -1.53917051 -1.54128440 -1.54337900	.894179894 .894514768 .894847529 .895178197 .895506792	0692 0693 0695 0697 0698	.15 .16 .17 .18
.20 .21 .22 .23 .24	-1.18371212 -1.10950183 -1.04241017 981498550 925985190	1.66666667 1.58730159 1.51515152 1.44927536 1.38888889	.16666667 .173553719 .180327869 .186991870 .193548387	-1.54545455 -1.54751131 -1.54954955 -1.55156951 -1.55357143	.895833333 .896157840 .896480331 .896800826 .897119342	0700 0702 0703 0705 0707	.20 .21 .22 .23
.25 .26 .27 .28 .29	875213677 828628877 785758160 746196667 709595590	1.33333333 1.28205128 1.23456790 1.19047619 1.14942529	.200000000 .206349206 .212598425 .218750000 .224806202	-1.5555556 -1.55752212 -1.55947137 -1.56140351 -1.56331878	.897435897 .897750511 .898063201 .898373984 .898682877	0708 0710 0712 0713 0715	.25 .26 .27 .28
.30 .31 .32 .33	675652850 644105537 614723787 587305760 561673527	1.1111111 1.07526882 1.04166667 1.01010101 .980392157	.230769231 .236641221 .242424242 .248120301 .253731343	-1.56521739 -1.56709957 -1.56896552 -1.57081545 -1.57264957	.898989899 .899295065 .899598394 .899899900 .900199601	0717 0718 0720 0722 0723	.30 .31 .32 .33
.35 .36 .37 .38 .39	537669640 515154273 494002853 474104040 455358020	.952380952 .925925926 .900900901 .877192982 .854700855	.259259259 .264705882 .270072993 .275362319 .280575540	-1.57446809 -1.57627199 -1.57805907 -1.57983193 -1.58158996	.900497512 .900793651 .901088032 .901380671 .901671583	0725 0727 0728 0730 0732	.35 .36 .37 .38
.40 .41 .42 .43	437675070 420974320 405182697 390236003 376068153	.833333333 .813008130 .793650794 .775193798 .757575758	.285714286 .290780142 .295774648 .300699301 .305555556	-1.58333333 -1.58506224 -1.58677686 -1.58847737 -1.59016393	.901960784 .902249289 .902534113 .902818270 .903100775	0733 0735 0737 0738 0740	.40 .41 .42 .43
. 45 . 46 . 47 . 48 . 49	362630476 349871126 337744570 326209135 315226611	.740740741 .724637681 .709219858 .694444444 .680272109	.310344828 .315068493 .319727891 .324324324 .328859060	-1.59183673 -1.59349593 -1.59514170 -1.59677419 -1.59839357	.903381643 .903660886 .903938521 .904214559 .904489016	0742 0743 0745 0747 0748	. 45 . 46 . 47 . 48
.50 .51 .52 .53	304761905 294782728 285259331 276164257 267472130	.666666667 .653594771 .641025641 .628930818 .617283951	.33333333 .337748344 .342105263 .346405229 .350649351	-1.60000000 -1.60159363 -1.60317460 -1.60474308 -1.60629921	.904761905 .905033238 .905303030 .905571294 .905838041	0750 0752 0753 0755 0757	.50 .51 .52 .53
.55 .56 .57 .58	259159465 251204495 243587023 236288281 229290809	.606060606 .595238095 .584795322 .574712644 .564971751	.354838710 .358974359 .363057325 .367088608 .371069182	-1.60784314 -1.60937500 -1.61089494 -1.61240310 -1.61389961	.906103286 .906367041 .906629318 .906890130 .907149489	0758 0760 0762 0763 0765	.55 .56 .57 .58
.63	222578348 216135734 209948816 204004370 198290023	.55555556 .546448087 .537634409 .529100529 .5208333333	.378881988 .382716049 .386503067	-1.61538462 -1.61685824 -1.61832061 -1.61977186 -1.62121212	.907407407 .907663897 .907918969 .908172635 .908424908	0767 0768 0770 0772 0773	.60 .61 .62 .63
	192794196 187506035 182415356 177512601 172788786	.512820513 .505050505 .497512438 .490196078 .483091787	.401197603 .404761903	-1.62264151 -1.62406015 -1.62546817 -1.62686567 -1.62825279	.908675799 .908925319 .909173479 .909420290 .909665763	0775 0777 0779 0780 0782	.65 .66 .67 .68
	2C4	<sup>2</sup> C <sup>1</sup> <sub>3</sub>	<sup>2</sup> C <sup>1</sup> <sub>2</sub>	2C 1	<sup>2</sup> C <sub>0</sub> <sup>1</sup>	$\frac{{}^{2}_{4}E^{1}}{b^{3}f^{(5)}(E)}$	p= <u>d_d_d</u> c_b_a

22(a)

		('D*y') <sub>x=x</sub> ;	$=\frac{1}{b^2}\sum_{j=0}^{4} {}_{4}^{2}C_{j}^{i}$	y <sub>j</sub> + 4R <sup>-</sup> .	(i = 3, l)	NA	CA
r= <u>a_a_a</u> b c d	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup>	<sup>2</sup> C <sup>3</sup> <sub>4</sub> C <sub>3</sub>	<sup>2</sup> C <sup>3</sup> <sub>4</sub>	2 <sub>4</sub> E <sup>3</sup> b <sup>3</sup> f <sup>(.5)</sup> (ξ)	
0.70 .71 .72 .73 .74	-0.168235462 163844677 159608938 155521184 151574751	0.476190476 .469483568 .462962963 .456621005 .450450450	0.411764707 .415204680 .418604650 .421965317 .425287357	-1.62962963 -1.63099631 -1.63235294 -1.63369963 -1.63503650	0.909909910 .910152740 .910394265 .910634495 .910873440	-0.0783 0785 0787 0788 0790	0.70 .71 .72 .73
.75 .76 .77 .78	147763348 144081031 140522182 137081483 133753902	.44444444 .438596491 .432900433 .427350427 .421940928	.428571430 .431818183 .435028250 .438202247 .441340783	-1.63636364 -1.63768116 -1.63898917 -1.64028777 -1.64157706	.91111111 .911347518 .911582670 .911816578 .912049252	0792 0793 0795 0797 0798	.75 .76 .77 .78
.80 .81 .82 .83	130534670 127419268 124403409 121483027 118654256	.416666667 .411522633 .406504065 .401606425 .396825396	.44444443 .447513813 .450549450 .453551913 .456521740	-1.64285714 -1.64412811 -1.64539007 -1.64664311 -1.64788732	.912280702 .912510936 .912739965 .912967798 .913194444	0800 0802 0803 0805 0807	.80 .81 .82 .83 .84
.85 .86 .87 .88	115913429 113257054 110681816 108184554 105762264	.392156862 .387596899 .383141762 .378787879 .374531836	. 459459460 . 462365590 . 465240640 . 468085107 . 470899470	-1.64912281 -1.65034965 -1.65156794 -1.65277778 -1.65397924	.913419913 .913644214 .913867356 .914089347 .914310197	0808 0810 0812 0813 0815	.85 .86 .87 .88
.90 .91 .92 .93	103412082 101131277 0989172470 0967675103 0946796970	.370370370 .366300366 .362318840 .358422939 .354609929	.473684210 .476439790 .479166667 .481865283 .484536083	-1.65517241 -1.65635739 -1.65753425 -1.65870307 -1.65986395	.914529914 .914748508 .914965986 .915182358 .915397631	0817 0818 0820 0822 0823	.90 .91 .92 .93
.95 .96 .97 .98	0926515457 0906808940 0887656790 0869039253 0850937457	.350877192 .347222222 .343642612 .340136054 .336700337	.487179487 .489795920 .492385787 .494949495 .497487437	-1.66101695 -1.66216216 -1.66329966 -1.66442953 -1.66555184	.915611814 .915824916 .916036944 .916247906 .916457811	0825 0827 0828 0830 0832	.95 .96 .97 .98
	0833333333 0816209597 0799549690 0783337753 0767558597	.333333333 .330033003 .326797386 .323624595 .320512821	.500000000 .502487562 .504950495 .507389163 .509803922	-1.66666667 -1.66777409 -1.66887417 -1.66996700 -1.67105263	.916666667 .916874480 .917081260 .917287014 .917491749	0833 0835 0837 0838 0840	1.00 1.01 1.02 1.03 1.04
1.06 1.07 1.08	0752197650 0737240950 0722675093 0708487227 0694665010	.317460317 .314465409 .311526480 .308641975 .305810398	.512195122 .514563107 .516908213 .519230769 .521531100	-1.67213115 -1.67320261 -1.67426710 -1.67532468 -1.67637540	.917695473 .917898194 .918099918 .918300654 .918500407	0842 0843 0845 0847 0848	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	0681196590 0668070587 0655276060 0642802503 0630639807	.303030303 .300300300 .297619048 .294985251 .292397661	.523809524 .526066351 .528301887 .530516432 .532710280	-1.67741936 -1.67845659 -1.67948718 -1.68051118 -1.68152866	.918699187 .918896999 .919093851 .919289750 .919484702	0850 0852 0853 0855 0857	1.10 1.11 1.12 1.13 1.14
1.16 1.17 1.18	0618778257 0607208500 0595921540 0584908717 0574161693	.289855072 .287356322 .284900285 .282485876 .280112045	.534883721 .537037037 .539170507 .541284404 .543378995	-1.68253968 -1.68354430 -1.68454259 -1.68553459 -1.68652038	.919678715 .919871795 .920063949 .920255183 .920445505	0858 0860 0862 0864 0865	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	0563672440 0553433220 0543436580 0533675337 0524142559	.277777778 .275482094 .273224044 .271002710 .268817204	.545454545 .547511312 .549549550 .551569507 .553571429	-1.68750000 -1.68847352 -1.68944099 -1.69040248 -1.69135802	.920634921 .920823436 .921011058 .921197794 .921383648	0853 0868 0870 0872 0873	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	0514831573 0505735933 0496849423 0488166042 0479680003	.266666667 .264550265 .262467192 .260416667 .258397933	.55555556 .557522124 .559471366 .561403509 .563318777	-1.69230769 -1.69325153 -1.69418960 -1.69512195 -1.69604863	.921568627 .921752739 .921935988 .922118380 .922299922	0875 0877 0878 0880 0882	1.25 1.26 1.27 1.28 1.29

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2C1

2C 1

b<sup>3</sup>f<sup>(5)</sup>(E)

 $p=\frac{d}{c}\cdot\frac{d}{b}\cdot\frac{d}{a}$ 

2C1

	4			
$(D^2y)_{x-x_2} = \frac{1}{b^2}$	$\sum_{j=0}$	<sup>2</sup> C <sup>2</sup> <sub>j</sub> y <sub>j</sub> +	2R2	(i=4,0)

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			J = 0			~~	~~~
						<sup>2</sup> <sub>4</sub> E <sup>4</sup>	
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	2C 4 4C 0	2C4 4C1	<sup>2</sup> <sub>4</sub> C <sup>4</sup> <sub>2</sub>	<sup>2</sup> C <sup>4</sup> <sub>3</sub>	2C4	b <sup>3</sup> f <sup>(5)</sup> (E)	
0.10 .11 .12 .13	30.7219662 27.4577011 24.7475926 22.4634752 20.5138121	-37.6666667 -34.3333333 -31.555556 -29.2051282 -27.1904762	14.0000000 13.9099099 13.8214286 13.7345133 13.6491228	-10.2380952 -10.2132701 -10.1886792 -10.1643192 -10.1401869	3.18279570 3.17899250 3.17521368 3.17145900 3.16772824	0.6683 .6701 .6720 .6738 .6756	0.10 .11 .12 .13
.15 .16 .17 .18	18.8314850 17.3661631 16.0793653 14.9411682 13.9279539	-25.4444445 -23.9166667 -22.5686275 -21.3703704 -20.2982456	13.5652174 13.4827586 13.4017094 13.3220339 13.2436975	-10.1162791 -10.0925926 -10.0691244 -10.0458716 -10.0228311	3.16402116 3.16033755 3.15667718 3.15303983 3.14942529	.6776 .6793 .6811 .6831	.15 .16 .17 .18
.20 .21 .22 .23	13.0208333 12.2045202 11.4665118 10.7964841 10.1858371	-19.3333333 -18.4603175 -17.6666667 -16.9420290 -16.2777778	13.1666667 13.0909091 13.0163934 12.9430894 12.8709677	-10.0000000 - 9.97737557 - 9.95495495 - 9.93273543 - 9.91071429	3.14583333 3.14226376 3.13871636 3.13519092 3.13168724	.6866 .6885 .6903 .6923	.20 .21 .22 .23
.25 .26 .27 .28	9.62735043 9.11491763 8.64333978 8.20816332 7.80555148	-15.6666667 -15.1025641 -14.5802469 -14.0952381 -13.6436782	12.8000000 12.7301587 12.6614173 12.5937500 12.5271318	- 9.88888889 - 9.86725664 - 9.84581498 - 9.82456140 - 9.80349345	3.12820513 3.12474438 3.12130479 3.11788618 3.11448835	.6958 .6977 .6995 .7014	.25 .26 .27 .28 .29
.30 .31 .32 .33	7.43218135 7.08516091 6.76196164 6.46036336 6.17840881	-13.2222222 -12.8279570 -12.4583333 -12.1111111 -11.7843137	12.4615385 12.3969466 12.3333333 12.2706767 12.2089552	- 9.78260870 - 9.76190476 - 9.74137931 - 9.72103004 - 9.70085470	3.1111111 3.10775428 3.10441767 3.10110110 3.09780439	.7051 .7068 .7088 .7105 .7124	.30 .31 .32 .33
.35 .36 .37 .38 .39	5.91436603 5.66669700 5.43403139 5.21514443 5.00893821	-11.4761905 -11.1851852 -10.9099099 -10.6491228 -10.4017094	12.1481482 12.0882353 12.0291971 11.9710145 11.9136691	- 9.68085106 - 9.66101695 - 9.64135021 - 9.62184874 - 9.60251046	3.09452736 3.09126984 3.08803165 3.08481262 3.08161259	.7142 .7161 .7178 .7197 .7215	.35 .36 .37 .38 .39
.40 .41 .42 .43	4.81442577 4.63071753 4.45700965 4.29257403 4.13674969	-10.1666667 - 9.94308943 - 9.73015873 - 9.52713178 - 9.33333333	11.8571429 11.8014184 11.7464789 11.6923077 11.6388889	- 9.58333333 - 9.56431535 - 9.54545455 - 9.52674897 - 9.50819672	3.07843137 3.07526882 3.07212476 3.06899903 3.06589147	.7234 .7251 .7270 .7289 .7307	.40 .41 .42 .43
. 45 . 46 . 47 . 48 . 49	3.98893524 3.84858238 3.71519027 3.58830048 3.46749272	- 9.14814815 - 8.97101449 - 8.80141844 - 8.63888889 - 8.48299320	11.5862069 11.5342466 11.4829932 11.4324324 11.3825503	- 9.48979592 - 9.47154472 - 9.45344130 - 9.43548387 - 9.41767068	3.06280193 3.05973025 3.05667627 3.05363985 3.05062082	.7326 .7343 .7362 .7379 .7398	. 45 . 46 . 47 . 48 . 49
.50 .51 .52 .53	3.35238095 3.24261001 3.13785265 3.03780683 2.94219343	- 8.33333333 - 8.18954248 - 8.05128205 - 7.91823899 - 7.79012346	11.3333333 11.2847682 11.2368421 11.1895425 11.1428571	- 9.4000000 - 9.38247012 - 9.36507936 - 9.34782609 - 9.33070866	3.04761905 3.04463438 3.04166667 3.03871577 3.03578154	.7417 .7434 .7453 .7472 .7489	.50 .51 .52 .53
.55 .56 .57 .58	2.85075411 2.76324945 2.67945726 2.59917109 2.52219890	- 7.66666667 - 7.54761905 - 7.43274854 - 7.32183908 - 7.21468927	11.0967742 11.0512821 11.0063694 10.9620253 10.9182390	- 9.31372549 - 9.29687500 - 9.28015564 - 9.26356589 - 9.24710425	3.03286385 3.02996255 3.02707750 3.02420857 3.02135562	.7508 .7527 .7544 .7563 .7582	.55 .56 .57 .58
.60 .61 .62 .63	2.44836182 2.37749307 2.30943698 2.24404806 2.18119025	- 7.1111111 - 7.01092896 - 6.91397849 - 6.82010582 - 6.72916667	10.8750000 10.8322981 10.7901235 10.7484663 10.7073171	- 9.23076923 - 9.21455939 - 9.19847328 - 9.18250951 - 9.16666667	3.01851852 3.01569714 3.01289134 3.01010101 3.00732601	.7601 .7618 .7637 .7656 .7672	.60 .61 .62 .63
.65 .66 .67 .68	2.12073616 2.06256638 2.00656892 1.95263862 1.90067665	- 6.64102564 - 6.5555556 - 6.47263682 - 6.39215686 - 6.31400966	10.6666667 10.6265060 10.5868264 10.5476191 10.5088757	- 9.15094340 - 9.13533835 - 9.11985019 - 9.10447761 - 9.08921933	3.00456621 3.00182149 2.99909174 2.99637681 2.99367660	.7691 .7710 .7729 .7746 .7764	.65 .66 .67 .68
	<sup>2</sup> C <sup>0</sup>	2C 0 4 3	<sup>2</sup> C <sup>0</sup> 4 2	<sup>2</sup> C <sup>0</sup>	<sup>2</sup> C 0	2E <sup>0</sup> b <sup>3</sup> f <sup>(5)</sup> (ξ)	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$

23(a)

$(0^2y)_{x=x_2} = \frac{1}{b^2}$	±	<sup>2</sup> C <sup>2</sup>	Уj	+	2R2	( i=4.0	)
-	1=0						

			•			- Color	
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	<sup>2</sup> C <sup>4</sup>	<sup>2</sup> C <sup>4</sup>	<sup>2</sup> C <sup>4</sup> <sub>4</sub>	<sup>2</sup> C <sup>4</sup> <sub>4</sub>	<sup>2</sup> C <sup>4</sup> 4	$\frac{{}^{2}_{4}E^{4}}{b^{3}f^{(5)}(\bar{z})}$	
0.70 .71 .72 .73	1.85059009 1.80229144 1.75569832 1.71073302 1.66732226	- 6.23809524 - 6.16431925 - 6.09259259 - 6.02283105 - 5.95495495	10.4705882 10.4327485 10.3953488 10.3583815 10.3218391	- 9.07407407 - 9.05904059 - 9.04411765 - 9.02930403 - 9.01459854	2.99099099 2.98831986 2.98566308 2.98302055 2.98039216	0.7783 .7800 .7821 .7837 .7856	0.70 .71 .72 .73 .74
.75 .76 .77 .78 .79	1.62539683 1.58489134 1.54574400 1.50789632 1.47129292	- 5.88888889 - 5.82456140 - 5.76190476 - 5.70085470 - 5.64135021	10.2857143 10.2500000 10.2146893 10.1797753 10.1452514	- 9.00000000 - 8.98550725 - 8.97111913 - 8.95683453 - 8.94265233	2.97777778 2.97517731 2.97259063 2.97001764 2.96745822	.7875 .7896 .7912 .7929 .7948	.75 .76 .77 .78 .79
.80 .81 .82 .83	1.43588137 1.40161195 1.36843750 1.33631130 1.30519682	- 5.58333333 - 5.52674897 - 5.47154472 - 5.41767068 - 5.36507936	10.111111 10.0773481 10.0439560 10.0109290 9.97826087	- 8.92857143 - 8.91459075 - 8.90070922 - 8.88692580 - 8.87323944	2.96491228 2.96237970 2.95986038 2.95735422 2.95486111	.7966 .7985 .8004 .8022 .8041	.80 .81 .82 .83
.85 .86 .87 .88	1.27504772 1.24582760 1.21749997 1.19003010 1.16338491	- 5.31372549 - 5.26356589 - 5.21455939 - 5.16666667 - 5.11985019	9.94594594 9.91397849 9.88235294 9.85106383 9.82010582	- 8.85964912 - 8.84615385 - 6.83275261 - 8.81944444 - 8.80622837	2.95238095 2.94991364 2.94745909 2.94501718 2.94258783	.8057 .8076 .8094 .8113 .8132	. 85 . 86 . 87 . 88 . 89
.90 .91 .92 .93	1.13753290 1.11244404 1.08808972 1.06444261 1.04147667	- 5.07407407 - 5.02930403 - 4.98550725 - 4.94265233 - 4.90070922	9.78947368 9.75916230 9.72916667 9.69948186 9.67010309	- 8.79310345 - 8.78006873 - 8.76712329 - 8.75426621 - 8.74149660	2.94017094 2.93776641 2.93537415 2.93299406 2.93062606	.8150 .8169 .8187 .8206 .8224	.90 .91 .92 .93
.95 .96 .97 .98	1.01916700 .997489835 .976422468 .955943179 .936031202	- 4.85964912 - 4.81944444 - 4.78006873 - 4.74149660 - 4.70370370	9.64102564 9.61224490 9.58375635 9.5555556 9.52763819	- 8.72881356 - 8.71621622 - 8.70370370 - 8.69127517 - 8.67892977	2.92827004 2.92592593 2.92359362 2.92127303 2.91896408	.8240 .8259 .8277 .8296 .8314	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	.916666667 .897830555 .879504657 .961671529 .844314456	- 4.6666667 - 4.63036304 - 4.59477124 - 4.55987055 - 4.52564103	9.50000000 9.47263682 9.44554455 9.41871921 9.39215686	- 8.66666667 - 8.65448505 - 8.64238411 - 8.63036304 - 8.61842105	2.91666667 2.91438071 2.91210614 2.90984285 2.90759076	.8333 .8351 .8370 .8388 .8406	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	.827417416 .810965045 .794942604 .779335951 .764131511	- 4.49206349 - 4.45911950 - 4.42679128 - 4.39506173 - 4.36391437	9.36585366 9.33980583 9.31400966 9.28846154 9.26315789	- 8.60655738 - 8.59477124 - 8.58306189 - 8.57142857 - 8.55987055	2.90534979 2.90311987 2.90090090 2.89869281 2.89649552	.8425 .8443 .8462 .8480 .8498	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	.749316249 .734877644 .720803667 .707082754 .693703789	- 4.33333333 - 4.30330330 - 4.27380952 - 4.24483776 - 4.21637427	9.23809524 9.21327014 9.18867925 9.16431925 9.14018692	- 8.54838710 - 8.53697749 - 8.52564103 - 8.51437700 - 8.50318471	2.89430894 2.89213301 2.88996764 2.88781275 2.88566828	.8517 .8535 .8553 .8571 .8590	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	.680656084 .667929349 .655513693 .643399587 .631577862	- 4.18840580 - 4.16091954 - 4.13390313 - 4.10734463 - 4.08123249	9.11627907 9.09259259 9.06912442 9.04587156 9.02283105	- 8.49206349 - 8.48101266 - 8.47003155 - 8.45911950 - 8.44827586	2.88353414 2.88141026 2.87929656 2.87719298 2.87509944	.8608 .8627 .8645 .8663 .8682	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	.620039683 .608776541 .597780237 .587042869 .576556815	- 4.0555556 - 4.03030303 - 4.00546448 - 3.98102981 - 3.95698925	9.0000000 8.97737557 8.95495495 8.93273543 8.91071429	- 8.43750000 - 8.42679128 - 8.41614907 - 8.40557276 - 8.39506173	2.87301587 2.87094220 2.86887836 2.86682427 2.86477987	.8700 .8718 .8737 .8755 .8773	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	.566314732 .556309526 .546534365 .536982647 .527648002	- 3.93333333 - 3.91005291 - 3.88713911 - 3.86458333 - 3.84237726	8.88888889 8.86725664 8.84581498 8.82456140 8.80349345	- 8.38461538 - 8.37423313 - 8.36391437 - 8.35365854 - 8.34346505	2.86274500 2.86071987 2.85870414 2.85669782 2.85470085	.8792 .8810 .8828 .8847 .8865	1.25 1.26 1.27 1.28 1.29
	<sup>2</sup> C <sup>0</sup>	<sup>2</sup> <sub>4</sub> C <sub>3</sub> <sup>0</sup>	<sup>2</sup> C <sup>0</sup> <sub>4</sub>	2C0	<sup>2</sup> C <sub>0</sub>	$\frac{{}^{2}_{4}E^{0}}{{}^{5}_{1}^{(5)}(E)}$	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$

 $(D^3y)_{x=x_1} = \frac{1}{b^3} \sum_{j=0}^{4} {}_{4}^{3}C_{j}^{i} y_{j} + {}_{4}^{3}R^{i}$  (i=0,4)

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	1					3 <sub>4</sub> E <sup>0</sup>	
aaa	30.0	300	3 C0	300	3 c 0		}
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	3C 0	3C0	4 2	3C <sup>0</sup> <sub>3</sub>	3C <sub>4</sub> <sup>0</sup>	b <sup>2</sup> f <sup>(5)</sup> (£)	
0.10	-53.6237956	63.0000000	-14.4545455	6.14285714	-1.06451613	0.6430 .6526	0.10
.11	-48.2257077 -43.7357454	57.5454545 53.0000000	-14.4054054 -14.3571429	6.15639810 6.16981132	-1.07073955 -1.07692308	.6623	.12
.13	-39.9441431	49.1538462	-14.3097345	6.18309859	-1.08306709	.6721	.13
.14	-36.7010747	45.8571429	-14.2631579	6.19626168	-1.08917197	.6819	.14
.15	-33.8966729	43.0000000	-14.2173913	6.20930233	-1,09523810	.6918	.15
.16	-31.4485426	40.5000000	-14.1724138	6.22222222	-1.10126582	.7017	.16
.17	-29.2936800	38.2941176 36.3333333	-14.1282051 -14.0847457	6.23502304	-1.10725552 -1.11320755	.7117	.17
.18	-27.3830864 -25.6780823	34.5789474	-14.0420168	6.26027397	-1.11912226	.7318	.19
00	0.4 1.477077	33,0000000	-14.0000000	6.27272727	-1.12500000	.7420	.20
.20	-24.1477273 -22.7669776	31.5714286	-13.9586777	6.28506787	-1.13084112	.7522	.21
.22	-21.5153458	30.2727273	-13.9180328	6.29729730	-1.13664596	.7625	.22
.23	-20.3759099	29.0869565	-13.8780488 -13.8387097	6.30941704 6.32142857	-1.14241486 -1.14814815	.7729 .7833	.23
.24	-19.3345707	28.0000000	-19.0901991	0.0214207	-1,14014010		
.25	-18.3794872	27.0000000	-13.8000000	6.33333333	-1.15384615	.7938	.25
.26	-17.5006419 -16.6895034	26.0769231 25.2222222	-13.7619048 -13.7244094	6.34513274	-1.15950920 -1.16513761	.8043 .8149	.26 .27
.27	-15.9387608	24.4285714	-13.6875000	6.36842105	-1.17073171	. 8255	.28
.29	-15.2421133	23.6896552	-13.6511628	6.37991266	-1.17629179	. 8362	.29
.30	-14.5941016	23.0000000	-13.6153846	6.39130435	-1.18181918	.8470	.30
.31	-13.9899723	22.3548387	-13.5801527	6.40259740	-1.18731118	.8578	.31
.32	-13.4255675	21.7500000	-13.5454545 -13.5112782	6.41379310 6.42489270	-1.19277108 -1.19819820	.8687 .8797	.32 .33
.33	-12.8972345 -12.4017515	21.1818182 20.6470588	-13.4776119	6.43589744	-1.20359281	.8907	.34
	13 0760660	00 1400571	13 4444444	6.44680851	-1.20895522	.9018	.35
.35	-11.9362660 -11.4982434	20.1428571 19.6666667	-13.4444444 -13.4117647	6.45762712	-1.21428571	.9129	.36
.37	-11.0854240	19.2162162	-13.3795620	6.46835443	-1.21958457	,9241	.37
.38	-10.6957871	18.7894737	-13.3478261	6.47899160	-1.22485207 -1.23008850	.9353	.38
.39	-10.3275199	18.3846154	-13.3165468	0.46933973	-1,2,0008500		•05
. 40	- 9.97899160	18.0000000	-13.2857143	6.50000000	-1.23529412	.9580	. 40
. 41	- 9.64873143	17.6341463	-13.2553192 -13.2253521	6.51037344	-1.24046921 -1.24561404	.9694	.41
. 42	- 9.33540929 - 9.03781951	17.2857143 16.9534884	-13.1958042	6.53086420	-1.25072886	.9925	. 43
.44	- 8.75486662	16.6363636	-13.1666667	6.54098361	-1.25581395	1.004	. 44
. 45	- 8.48555314	16.3333333	-13.1379310	6.55102041	-1.26086957	1.016	. 45
.46	- 8.22896888	16.0434783	-13.1095890	6.56097561	-1.26589595	1.027	. 46
. 47	- 7.98428162	15.7659574	-13.0816327	6.57085020	-1.27089337	1.039	.47 .48
.48	- 7.75072904 - 7.52761148	15.5000000 15.2448980	-13.0540541 -13.0268456	6.58064516 6.59036145	-1.27586207 -1.28080229	1.051	. 49
İ				6.60000000	-1.28571429	1.075	•50
.50	- 7.31428571 - 7.11015941	15.0000000 14.7647058	-13.0000000 -12.9735099	6.60956175	-1.29059829	1.087	.51
.52	- 6.91468619	14.5384615	-12.9473684	6.61904762	-1.29545455	1.099	.52
.53	- 6.72736130	14.3207547	-12.9215686	6.62845850 6.63779528	-1.30028329 -1.30508475	1.111	.53 .54
.54	- 6.54771774	14.1111111	-12.8961039				
•55	- 6.37532284	13.9090909	-12.8709677	6.64705882	-1.30985915	1.136	.55
.56	- 6.20977513 - 6.05070166	13.7142857 13.5263158	-12.8461538 -12.8216561	6.65625000	-1.31460674 -1.31932773	1.148	.56 .57
.57	- 5.89775549	13.3448276	-12.7974684	6.67441860	-1.32402235	1.173	.58
.59	- 5.75061350	13.1694915	-12.7735849	6.68339768	-1.32869081	1.185	.59
.60	- 5.60897436	13.0000000	-12.7500000	6.69230769	-1.33333333	1.198	.60
.61	- 5.47255679	12.8360656	-12.7267081	6.70114943	-1.33795014	1.211	.61
.62	- 5.34109788 - 5.21435167	12.6774194	-12.7037037 -12.6809816	6.70992366 6.71863118	-1.34254144 -1.34710744	1.223	.62 .63
.63 .64	- 5.09208779	12.3750000	-12.6585366	6.72727273	-1.35164835	1.249	.64
65	- 4.97409027	12.2307692	-12.6363636	6.73584906	-1.35616438	1.258	.65
.65	- 4.86015642	12.0909091	-12.6144578	6.74436090	-1.36065574	1.275	.66
.67	- 4.75009588	11.9552239	-12.5928144	6.75280899	-1.36512262	1.288	.67
.68	- 4.64372965 - 4.54088930	11.8235294	-12.5714286 -12.5502959	6.76119403	-1.36956522 -1.37398374	1.301	.68
.09	- 4.04000300	11.0000022	-12.0002909	3.10001070	1,0,000/14	3E4	
	- 3C4	- <sup>3</sup> C <sub>3</sub> <sup>4</sup>	- 3C4	- <sup>3</sup> C <sup>4</sup>	- 3C4	4 <sup>E</sup>	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$
	404	4 3	4~2	4 1	40	b <sup>2</sup> f <sup>(5)</sup> (E)	сва
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$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	3C <sup>0</sup>	3C0	3 C <sup>0</sup>	3C <sup>0</sup>	3 <sub>C</sub> 0 4 4	$\frac{{}_{4}^{3}E^{0}}{b^{2}f^{(5)}(\xi)}$	
0.70 .71 .72 .73	- 4.44141621 - 4.34516083 - 4.25198211 - 4.16174688 - 4.07432930	11.5714286 11.4507042 11.3333333 11.2191781 11.1081081	-12.5294118 -12.5087719 -12.4883721 -12.4682081 -12.4482759	6.77777778 6.78597786 6.79411765 6.80219780 6.81021898	-1.37837838 -1.38274933 -1.38709677 -1.39142091 -1.39572192	1.327 1.340 1.354 1.367 1.380	0.70 .71 .72 .73
.75 .76 .77 .78	- 3.98961039 - 3.90747757 - 3.82782424 - 3.75054938 - 3.67555722	11.0000000 10.8947368 10.7922078 10.6923077 10.5949367	-12.4285714 -12.4090909 -12.3898305 -12.3707865 -12.3519553	6.81818182 6.82608696 6.83393502 6.84172662 6.84946237	-1.40000000 -1.40425532 -1.40848806 -1.41269841 -1.41688654	1.394 1.407 1.421 1.435 1.448	.75 .76 .77 .78 .79
.80 .81 .82 .83	- 3.60275689 - 3.53206212 - 3.46339092 - 3.39666543 - 3.33181151	10.5000000 10.4074074 10.3170732 10.2289157 10.1428571	-12.3333333 -12.3149171 -12.2967033 -12.2786885 -12.2608696	6.85714286 6.86476868 6.87234043 6.87985866 6.88732394	-1.42105263 -1.42519685 -1.42931937 -1.43342037 -1.43750000	1.462 1.476 1.490 1.504 1.518	.80 .81 .82 .83
.85 .86 .87 .88	- 3.26875870 - 3.20743977 - 3.14779084 - 3.08975087 - 3.03326174	10.0588235 9.97674419 9.89655172 9.81818182 9.74157303	-12.2432432 -12.2258065 -12.2085562 -12.1914894 -12.1746032	6.89473684 6.90209790 6.90940767 6.91666667 6.92387543	-1.44155844 -1.44559586 -1.44961240 -1.45360825 -1.45758355	1.532 1.546 1.560 1.574 1.589	.85 .86 .87 .88
.90 .91 .92 .93	- 2.97826795 - 2.92471652 - 2.87255685 - 2.82174060 - 2.77222153	9.66666667 9.59340659 9.52173913 9.45161290 9.38297872	-12.1578947 -12.1413613 -12.1250000 -12.1088083 -12.0927835	6.93103448 6.93814433 6.94520548 6.95221843 6.95918367	-1.46153846 -1.46547315 -1.46938776 -1.47328244 -1.47715736	1.603 1.617 1.632 1.646 1.661	.90 .91 .92 .93
.95 .96 .97 .98	- 2.72395544 - 2.67689999 - 2.63101472 - 2.58626082 - 2.54260112	9.31578947 9.25000000 9.18556701 9.12244898 9.06060606	-12.0769231 -12.0612245 -12.0456853 -12.0303030 -12.0150754	6.96610169 6.97297297 6.97979798 6.98657718 6.99331104	-1.48101266 -1.48484849 -1.48866499 -1.49246231 -1.49624060	1.676 1.690 1.705 1.720 1.735	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	- 2.50000000 - 2.45842330 - 2.41783826 - 2.37821342 - 2.33951860	9.00000000 8.94059406 8.88235294 8.82524272 8.76923077	-12.0000000 -11.9850746 -11.9702970 -11.9556650 -11.9411765	7.00000000 7.00664452 7.01324503 7.01980198 7.02631579	-1.50000000 -1.50374065 -1.50746269 -1.51116625 -1.51485149	1.750 1.765 1.780 1.795 1.810	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	- 2.30172481 - 2.26480420 - 2.22872999 - 2.19347646 - 2.15901885	8.71428571 8.66037736 8.60747664 8.5555556 8.50458716	-11.9268293 -11.9126214 -11.8985507 -11.8846154 -11.8708134	7.03278689 7.03921569 7.04560261 7.05194805 7.05825243	-1.51851852 -1.52216749 -1.52579853 -1.52941176 -1.53300733	1.826 1.841 1.856 1.872 1.887	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	- 2.12533336 - 2.09239707 - 2.06018793 - 2.02868470 - 1.99786691	8.45454545 8.40540541 8.35714286 8.30973451 8.26315789	-11.8571429 -11.8436019 -11.8301887 -11.8169014 -11.8037383	7.06451613 7.07073955 7.07692308 7.08306709 7.08917197	-1.53658537 -1.54014599 -1.54368932 -1.54721550 -1.55072464	1.903 1.919 1.934 1.950 1.966	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	- 1.96771486 - 1.93820953 - 1.90933261 - 1.88106643 - 1.85339394	8.21739130 8.17241379 8.12820513 8.08474576 8.04201681	-11.7906977 -11.7777778 -11.7649770 -11.7522936 -11.7397260	7.09523810 7.10126582 7.10725552 7.11320755 7.11912226	-1.55421687 -1.55769231 -1.56115108 -1.56459330 -1.56801909	1.982 1.998 2.014 2.030 2.046	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	- 1.82629870 - 1.79976483 - 1.77377699 - 1.74832040 - 1.72338073	8.00000000 7.95867769 7.91803279 7.87804878 7.83870968	-11.7272727 -11.7149321 -11.7027027 -11.6905830 -11.6785714	7.12500000 7.13084112 7.13664596 7.14241486 7.14814815	-1.57142857 -1.57482185 -1.57819905 -1.58156028 -1.58490566	2.062 2.078 2.095 2.111 2.127	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	- 1.69894420 - 1.67499741 - 1.65152748 - 1.62852192 - 1.60596865	7.80000000 7.76190476 7.72440945 7.68750000 7.65116279	-11.6666667 -11.6548673 -11.6431718 -11.6315789 -11.6200873	7.15384615 7.15950920 7.16513762 7.17073171 7.17629179	-1.58823529 -1.59154930 -1.59484778 -1.59813084 -1.60139860	2.144 2.160 2.177 2.194 2.210	1.25 1.26 1.27 1.28 1.29
	- <sup>3</sup> C <sup>4</sup>	- <sup>3</sup> C <sup>4</sup> <sub>3</sub>	- <sup>3</sup> C <sub>2</sub> <sup>4</sup>	- <sup>3</sup> C <sup>4</sup>	- <sup>3</sup> C <sub>4</sub>	b <sup>2</sup> f <sup>(5</sup> (E)	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$

 $(D^3y)_{x=x_1} = \frac{1}{b^3} \sum_{j=0}^{4} {}_{3}^{3}C_{j}^{i} y_j + {}_{4}^{3}R^{i}$  (i=1,3)

			b) =0			The same of the sa	ACA
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	3C1	3C 1	3C1 4C2	3C1	3C 1	$\frac{{}_{4}^{3}E^{1}}{{}_{5}^{2}f^{(5)}(E)}$	
0.10 .11 .12 .13	-50.2723084 -44.9307836 -40.4960605 -36.7584139 -33.5680561	59.0000000 53.5454545 49.000000 45.1538462 41.8571429	-13.3636364 -13.2162162 -13.0714286 -12.9292035 -12.7894737	.5.57142857 5.53080569 5.49056604 5.45070423 5.41121495	-0.935483871 929260450 923076923 916932907 910828025	0.5200 .5170 .5140 .5110 .5080	0.10 .11 .12 .13 .14
.15 .16 .17 .18	-30.8151572 -28.4173578 -26.3116886 -24.4491843 -22.7911973	39.0000000 36.5000000 34.2941176 32.333333 30.5789474	-12.6521739 -12.5172414 -12.3846154 -12.2542373 -12.1260504	5.37209302 5.33333333 5.29493088 5.25688073 5.21917808	904761905 898734177 892744479 886792453 880877743	.5050 .5020 .4990 .4960 .4930	.15 .16 .17 .18
.20 .21 .22 .23 .24	-21.3068182 -19.9710330 -18.7633830 -17.6669739 -16.6677334	29.0000000 27.5714286 26.2727273 25.0869565 24.0000000	-12.0000000 -11.8760331 -11.7540984 -11.6341463 -11.5161290	5.18181818 5.14479638 5.10810811 5.07174888 5.03571429	875000000 869158879 863354037 857585139 851851852	.4900 .4870 .4840 .4810	.20 .21 .22 .23
.25 .26 .27 .28 .29	-15.7538462 -14.9153198 -14.1436469 -13.4315400 -12.7727206	23.0000000 22.0769231 21.2222222 20.4285714 19.6896552	-11.4000000 +11.2857143 -11.1732284 -11.0625000 -10.9534884	5.00000000 4.96460177 4.92951542 4.89473684 4.86026201	846153846 840490798 834862385 829268293 823708207	.4750 .4720 .4690 .4660 .4630	.25 .26 .27 .28
.30 .31 .32 .33	-12.1617513 -11.5938997 -11.0650282 -10.5715037 -10.1101235	19.0000000 18.3548387 17.7500000 17.1818182 16.6470588	-10.8461539 -10.7404580 -10.6363636 -10.5338346 -10.4328358	4.82608696 4.79220779 4.75862069 4.72532189 4.69230769	818181818 812688822 807228916 801801802 796407186	.4600 .4570 .4540 .4510 .4480	.30 .31 .32 .33
.35 · .36 .37 .38 .39	- 9.67805352 - 9.27277692 - 8.89205136 - 8.53387272 - 8.19644436	16.1428571 15.6666667 15.2162162 14.7894737 14.3846154	-10.3333333 -10.2352941 -10.1386861 -10.0434783 - 9.94964028	4.65957447 4.62711864 4.59493671 4.56302521 4.53138075	791044776 785714286 780415430 775147929 769911504	.4450 .4420 .4390 .4360 .4330	.35 .36 .37 .38
.40 .41 .42 .43	- 7.87815126 - 7.57753776 - 7.29328854 - 7.02421206 - 6.76922676	14.0000000 13.6341463 13.2857143 12.9534884 12.6363636	- 9.85714284 - 9.76595745 - 9.67605633 - 9.58741260 - 9.50000000	4.50000000 4.46887967 4.43801653 4.40740741 4.37704918	764705882 759530792 754385965 749271137 744186047	.4300 .4270 .4240 .4210 .4180	.40 .41 .42 .43
.45 .46 .47 .48 .49	- 6.52734857 - 6.29768026 - 6.07940225 - 5.87176442 - 5.67407900	12.3333333 12.0434783 11.7659574 11.5000000 11.2448980	- 9.41379310 - 9.32876712 - 9.24489796 - 9.16216216 - 9.08053691	4.34693878 4.31707317 4.28744939 4.25806452 4.22891566	739130435 734104046 729106628 724137931 719197708	.4150 .4120 .4090 .4060 .4030	. 45 . 46 . 47 . 48
.50 .51 .52 .53	- 5.48571429 - 5.30608911 - 5.13466797 - 4.97095663 - 4.81449834	11.0000000 10.7647058 10.5384615 10.3207547 10.1111111	- 9.00000000 - 8.92052960 - 8.84210526 - 8.76470588 - 8.68831169	4.20000000 4.17131474 4.14285714 4.11462451 4.08661417	714285714 709401709 704545455 699716714 694915254	.4000 .3970 .3940 .3910 .3880	.50 .51 .52 .53
.55 .56 .57 .58	- 4.66487037 - 4.52168092 - 4.38458642 - 4.25318905 - 4.12723457	9.90909091 9.71428571 9.52631579 9.34482759 9.16949153	- 8.61290323 - 8.53846154 - 8.46496815 - 8.39240506 - 8.32075472	4.05882353 4.03125000 4.00389105 3.97674419 3.94980695	690140845 685393258 680672269 675977654 671309192	.3850 .3820 .3790 .3760 .3730	.55 .56 .57 .58
.60 .61 .62 .63	- 4.00641026 - 3.89044321 - 3.77907869 - 3.67207864 - 3.56922041	9.0000000 8.83606557 8.67741935 8.52380952 8.37500000	- 8.25000000 - 8.18012422 - 8.11111111 - 8.04294480 - 7.97560977	3.92307692 3.89655172 3.87022901 3.84410646	666666667 662049861 657458564 652892562 648351648	.3700 .3670 .3640 .3610	.60 .61 .62 .63
.65 .66 .67 .68	- 3.47029554 - 3.37510863 - 3.28347642 - 3.19522683 - 3.11019815	8.23076923 8.09090909 7.95522388 7.82352941 7.69565217	- 7.90909092 - 7.84337349 - 7.77844311 - 7.71428571 - 7.65088758	3.79245283 3.76691729 3.74157303 3.71641791	643835616 639633262 634877384 630434783 626016260	.3550 .3520 .3490 .3460 .3430	.65 .66 .67 .68
	- <sup>3</sup> <sub>4</sub> C <sub>4</sub> <sup>3</sup>	- <sup>3</sup> <sub>4</sub> C <sub>3</sub>	- <sup>3</sup> C <sup>3</sup> <sub>2</sub>	- <sup>3</sup> <sub>4</sub> C <sub>1</sub> <sup>3</sup>	- <sup>3</sup> <sub>4</sub> c <sup>3</sup> <sub>0</sub>	b <sup>2</sup> f <sup>(5)</sup> (ξ)	$p = \frac{d}{c} = \frac{d}{b} = \frac{d}{a}$

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			b j=0			N.	ACA.
r <u>aaa</u> a bcd	3C1	3C	3C1	3C1 4 3	3C1	$\frac{{}_{4}^{3}E^{1}}{{}_{5}^{2}f^{(5)}(\xi)}$	
0.70 .71 .72 .73	- 3.02823832 - 2.94920418 - 2.87296089 - 2.79938131 - 2.72834551	7.57142857 7.45070423 7.33333333 7.21917808 7.10810811	7.58823528 7.52631579 7.46511627 7.40462427 7.34482758	3.66666667 3.64206642 3.61764706 3.59340659 3.56934307	-0.621621622 617250674 612903226 608579088 604278075	0.3400 .3370 .3340 .3310 .3280	0.70 .71 .72 .73 .74
.75 .76 .77 .78	- 2.65974026 - 2.59345856 - 2.52939928 - 2.46746670 - 2.40757023	7.00000000 6.89473684 6.79220779 6.69230769 6.59493671	- 7.28571429 - 7.22727273 - 7.16949153 - 7.11235956 - 7.05586593	3.54545455 3.52173913 3.49819495 3.47482014 3.45161290	600000000 595744681 591511936 587301587 583113456	.3250 .3220 .3190 .3160 .3130	.75 .76 .77 .78 .79
.80 .81 .82 .83	- 2.34962406 - 2.29354683 - 2.23926137 - 2.18669449 - 2.13577661	6.50000000 6.40740741 6.31707317 6.22891566 6.14285714	- 7.00000000 - 6.94475138 - 6.89010989 - 6.83606557 - 6.78260870	3.42857143 3.40569395 3.38297872 3.36042403 3.33802817	578947368 574803150 570680628 566579634 562500000	.3100 .3070 .3040 .3010 .2980	.80 .81 .82 .83 .84
.85 .86 .87 .88	- 2.08644172 - 2.03862697 - 1.99227268 - 1.94732198 - 1.90372076	6.05882353 5.97674419 5.89655172 5.81818182 5.74157303	- 6.72972973 - 6.67741935 - 6.62566845 - 6.57446809 - 6.52380952	3.31578947 3.29370629 3.27177700 3.25000000 3.22837370	558441558 554404145 550387597 546391753 542416452	.2950 .2920 .2890 .2860 .2830	.85 .86 .87 .88
.90 .91 .92 .93	- 1.86141747 - 1.82036298 - 1.78051045 - 1.74181519 - 1.70423455	5.66666667 5.59340659 5.52173913 5.45161290 5.38297872	- 6.47368421 - 6.42408377 - 6.37500000 - 6.32642487 - 6.27835052	3.20689655 3.18556701 3.16438356 3.14334471 3.12244898	538461538 534526854 530612245 526717557 522842640	.2800 .2770 .2740 .2710 .2680	.90 .91 .92 .93
.95 .96 .97 .98	- 1.66772782 - 1.63225609 - 1.59778222 - 1.56427066 - 1.53168742	5.31578947 5.25000000 5.18556701 5.12244898 5.06060606	- 6.23076923 - 6.18367347 - 6.13705584 - 6.09090909 - 6.04522613	3.10169492 3.08108108 3.06060606 3.04026846 3.02006689	518987342 515151515 511335013 507537688 503759398	.2650 .2620 .2590 .2560 .2530	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	- 1.50000000 - 1.46917727 - 1.43918944 - 1.41000796 - 1.38160547	5.00000000 4.94059406 4.88235294 4.82524272 4.76923077	- 6.00000000 - 5.95522388 - 5.91089109 - 5.86699507 - 5.82352941	3.00000000 2.98006645 2.96026490 2.94059406 2.92105263	50000000 496259352 492537313 488833747 485148515	.2500 .2470 .2440 .2410 .2380	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	- 1.35395577 - 1.32703371 - 1.30081517 - 1.27527701 - 1.25039702	4.71428571 4.66037736 4.60747664 4.5555556 4.50458716	- 5.78048780 - 5.73786408 - 5.69565217 - 5.65384615 - 5.61244019	2.90163934 2.88235294 2.86319218 2.84415584 2.82524272	481481481 477832512 474201474 470588235 466992665	.2350 .2320 .2290 .2260 .2230	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	- 1.22615386 - 1.20252706 - 1.17949691 - 1.15704451 - 1.13515164	4.45454545 4.40540541 4.35714286 4.30973451 4.26315789	- 5.57142857 - 5.53080569 - 5.49056604 - 5.45070423 - 5.41121495	2.80645161 2.78778135 2.76923077 2.75079872 2.73248408	463414634 459854015 456310680 452784504 449275362	.2200 .2170 .2140 .2110 .2080	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	- 1.11380086 - 1.09297530 - 1.07265877 - 1.05283569 - 1.03349105	4.21739130 4.17241379 4.12820513 4.08474576 4.04201681	- 5.37209302 - 5.33333333 - 5.29493088 - 5.25688073 - 5.21917808	2.71428571 2.69620253 2.67823344 2.66037736 2.64263323	445783132 442307692 438848921 435406699 431980907	.2050 .2020 .1990 .1960	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	- 1.01461039 996179794 978185841 960615603 943456607	4.0000000 3.95867769 3.91803279 3.87804878 3.83870968	- 5.18181818 - 5.14479638 - 5.10910811 - 5.07174888 - 5.03571429	2.62500000 2.60747664 2.59006211 2.57275542 2.55555555	428571429 425178147 421800948 418439716 415094340	.1900 .1870 .1840 .1810 .1780	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	926696834 910324679 894328962 878698876 863424004	3.80000000 3.76190476 3.72440945 3.68750000 3.65116279	- 5.00000000 - 4.96460177 - 4.92951542 - 4.89473684 - 4.86026201	2.53846154 2.52147239 2.50458716 2.48780488 2.47112462	411764706 408450704 405152225 401869159 398601399	.1750 .1720 .1690 .1660	1.25 1.26 1.27 1.28 1.29
	- <sup>3</sup> <sub>4</sub> C <sup>3</sup> <sub>4</sub>	- <sup>3</sup> C <sup>3</sup>	- <sup>3</sup> C <sup>3</sup> <sub>4</sub>	- <sup>3</sup> C <sup>3</sup>	- 3C3	$\frac{{}^{3}E^{3}}{{}^{2}f^{(5)}(\xi)}$	p_ <u>d_d_d</u> -

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<u>a a a</u> b c d	3C 2 4° 0	3C2	<sup>3</sup> C <sup>2</sup> <sub>4</sub>	3C 2 4 3	3C2	$\frac{{}_{4}^{3}E^{2}}{b^{2}f^{(5)}(\xi)}$	
0.10	-16,7574361	19.0000000	-2.45454545	-0.142857143	0.354838710	-0.1600	0.10
.11	-14.9769279	17.1818182	-2.40540541	156398104	,356913183	1610	.11
	-13.4986868	15.6666667	-2.35714286	169811321	.358974359	1620	.12
. 12							.13
.13	-12.2528046	14.3846154	-2.30973451	183098592	.361022364	1630	
.14	-11.1893520	13.2857143	-2.26315789	196261682	.363057325	1640	.14
.15	-10.2717191	12.3333333	-2.21739130	209302326	.365079365	1650	.15
.16	- 9.47245266	11.5000000	-2.17241379	222222222	.367088608	1660	.16
.17	- 8,77056288	10.7647059	-2.12820513	235023042	.369085174	1670	.17
.18	- 8.14972810	10.1111111	-2.08474576	247706422	.371069182	1680	.18
.19	- 7.59706576	9.52631579	-2.04201681	260273972	.373040752	1690	.19
.20	- 7.10227272	9.00000000	-2.00000000	272727272	.375000000	1700	.20
.21	- 6.65701100	8.52380952	-1.95867769	285067874	.376947040	1710	.21
.22		8.09090909		297297298	.378881988	1720	.22
	- 6.25446100						
.23	- 5.88899130	7.69565217	-1.87804878	309417040	.380804954	1730	.23
.24	- 5.55591114	7.33333333	-1.83870968	321428572	.382716049	1740	.24
.25	- 5.25128206	7.00000000	-1.80000000	333333334	.384615385	1750	.25
.26	- 4.97177326	6.69230769		345132744	.386503067	1760	.26
						1770	.27
.27	- 4.71454897	6.40740741			.388379205		
.28	- 4.47718000	6.14285714		368421052	.390243902	1780	.28
.29	- 4.25757354	5.89655172	-1.65116279	379912664	.392097264	1790	.29
.30	- 4.05391710	5,66666667	-1.61538462	391304348	.393939394	1800	.30
.31	- 3.86463322	5.45161290		402597402	.395770393	1810	.31
				413793104	.397590361	1820	.32
.32	- 3.68834272	5.25000000					
.33	- 3.52383456	5.06060606		424892704	.399399399	1830	.33
.34	- 3.37004116	4.88235294	-1.47761194	435897436	.401197605	1840	•34
.35	- 3.22601784	4.71428571	-1.4444444	446808510	.402985075	1850	.35
		4.55555556		457627118	.404761905	1860	.36
.36	- 3.09092564						
.37	- 2.96401712	4.40540541	-1.37956204	468354430	.406528190	1870	.37
.38	- 2.84462424	4.26315789		478991597	.408284024	1880	•38
.39	- 2.73214812	4.12820513	-1.31654676	489539748	.410029499	1890	.39
.40	- 2.62605042	4.00000000	-1.28571429	500000000	.411764706	1900	.40
.41	- 2.52584592	3.87804878		510373444	.413489736	1910	.41
					.415204678	1920	.42
. 42	- 2.43109618	3.76190476		520661158			
. 43	- 2.34140402	3.65116279	-1.19580420	530864198	.416909621	1930	. 43
. 44	- 2.25640892	3.54545455	-1,16666667	540983606	.418604651	1940	. 44
.45	- 2.17578286	3.4444444	-1.13793103	551020408	.420289855	1950	.45
	- 2.09922675	3.34782609		560975610	.421965318	1960	.46
. 46							
. 47	- 2.02646742	3.25531915		570850202	.423631124		.47
.48	- 1.95725481	3.16666667	-1.05405405	580645161	.425287356	1980	.48
. 49	- 1.89135967	3.08163265	-1.02684564	590361446	.426934097	1990	.49
.50	- 1.82857143	3.00000000	-1.00000000	600000000	.428571429	2000	.50
.51	- 1.76869637	2.92156863		609561753	.430199430	2010	.51
			947368421	619047619	.431818182	2020	.52
.52	- 1.71155599	2.84615385				2030	
.53	- 1.65698554 - 1.60483278	2.77358491	921568627 896103896	628458498 637795276	.433427762 .435028249	2030	.53
	1.00.002.0		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				
•55	- 1.55495679	2.63636364	870967742	647058823	.436619718	2050	.55
.56	- 1.50722697	2.57142857		656250000	.438202247	2060	.56
.57	- 1.46152214	2.50877193		665369650	.439775910	2070	.57
	- 1.41772968	2.44827586		674418605	.441340782	2080	.58
.58 .59	- 1.37574486	2.38983051			.442896936	2090	.59
. 60	- 1.33547009	2.33333333		692307692	.44444444	2100	.60
.61	- 1.29681440	2.27868852		701149425	.445983380	2110	.61
.62	- 1.25969290			709923664	.447513812	2120	. 62
. 63	- 1.22402621	2.17460317	680981595	718631179	.449035813	2130	.63
.64	- 1.18974014			727272727	.450549450	2140	.64
65	_ 1 15676510	2.07692308	636363636	735849057	.452054793	2150	.65
. 65	- 1.15676518					2160	.66
.66	- 1.12503621	2.03030303		744360902	.453551913		
. 67	- 1.09449214	1.98507463			.455040873	2170	.67
.68	- 1.06507561	1.94117647	571428571	761194030	.456521740	2180	.68
.69	- 1.03673272	1.89855072		769516729	.457994580	2190	.69
			2 - 2	7.0	7.0	3 <sub>4</sub> E <sup>2</sup>	
	- 3C2	- 3C2	- 3C2	- 3C2	- 3C2		p=d=d=
	4 4	4 3	4 2	4 1	4 0	b <sup>2</sup> f <sup>(5)</sup> (£)	C b
		1		1		. (4)	

26(a)

$(D^3y)_{x=x_1} = \frac{1}{b^3}$	$\sum_{j=0}^{4}$	3C }	Уј	+	3R i	(i=2)
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NACA	NACA	
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			•			-4145	مر مرکزی
						3 <sub>4</sub> E <sup>2</sup>	
- <u>a_a</u> _a b c d	3C2	3C2	3C2	3C2	3C2	b <sup>2</sup> f <sup>(5)</sup> (£)	
	- 1.00941277	1.85714286	-0.529411765	-0.77777778	0.459459460	-0.2200	0.70
0.70	983068060	1.81690141		785977860	.460916443	2210	.71
.71 .72	957653630	1.77777778	488372093	794117647	.462365590	2220	.72
.73	933127104		468208092	802197802	.463806970	2230	.73
.74	909448504	1.70270270	448275862	810218978	.465240640	2240	.74
.75	886580086	1.66666667	428571429	818181818	.466666667	2250 2260	.75 .76
.76		1.63157895	409090909	826086957	.468085107 .469496020	2270	.77
.77	843133092	1.59740260	- 389830508	833935018 841726619	470899470	2280	.78
.78 . <b>79</b>	822488900 802523410	1.56410256	370786517 351955307	849462366	472295513	2290	.79
			333333333	857142857	.473684211	2300	.80
.80	783208020 764515610	1.50000000	314917127	864768683	.475065617	2310	.81
.81 .82	746420456	1.43902439	296703297	872340426	.476439791	2320	. 82
. 83		1.40963855	278688525	879858657	. 477806789	2330	. 83
. 84	711925536	1.38095238	260869565	887323944	.479166667	2340	.84
. 85	695480574	1.35294118	243243243	894736842	.480519481	2350	.85 .86
. 86	→ .679542324	1.32558140	225806452	902097902	.481865285	2360 2370	.87
. 87	664090894	1.29885057	208556150	909407666	.483204134 .484536082	2380	.88
. 88 . 89	649107326 634573587	1.27272727	191489362 174603175	916666667 923875433	.485861183	2390	.89
			157894737	931034483	.487179487	2400	.90
.90	620472490	1.22222222		938144330	488491049	2410	.91
.91	606787660	1.17391304		945205479	.489795918	2420	. 92
.92	593503482 580605063	1.15053763	108808290	952218430	.491094148	2430	.93
.93 .94	568078182	1.12765957	0927835051	959183673	.492385787	2440	.94
.95	555909274	1.10526316	0769230769	966101695 972972973	.493670886	2450	. 95
.96	544085364	1.08333333	0612244897	972972973	. 494949495	2460	.96
.97	532594074	1.06185567	0456852792	979797980	.496221662	2470 2480	.97 .98
.98 .99	521423552	1.04081633	030303030303 0150753769	986577181 993311037	.497487437 .498746867	2490	.99
			0	-1.00000000	.500000000	2500	1.00
1.00	500000000 489725758	1.00000000		-1.00664452	.501246883	2510	1.01
1.01	479729814	.960784314	.0297029703	-1.01324503	.502487562	2520	1.02
1.03	470002652	.941747573	.0443349754	-1.01980198	.503722084	2530	1.03
1.04	460535158	.923076923	.0588235294	-1.02631579	.504950495	2540	1.04
1.05	451318590	.904761905		-1.03278689	.506172839	2550	1.05
1.06	442344570	.886792453		-1.03921569	.507389163 .508599509	2560 2570	1.06 1.07
1.07	433605056	.869158879	.101449275	-1.04560261 -1.05194805	.509803922	2580	1.08
1.08 1.09	425092336 416799006	.851851852 .834862385	.115384615	-1.05825243	.511002445	2590	1.09
	408717954	.818181818	.142857143	-1.06451613	.512195122	2600	1.10
1.10 1.11	- 400842352	.801801802		-1.07073955	.513381995	2610	1.11
1.12	393165 336	.785714286		-1.07692308	.514563107	2620	1.12
1.13	385631502	.769911504	.183098592	-1.08306709	.515738499	2630	1.13
1.14	378383885	.754385965	.196261682	-1.08917197	.516968213	2640	1.14
1.15	371266955	.739130435		-1.09523810	.518072289	2650 2660	1.15 1.16
1.16	364325099	.724137931		-1.10126582	.519230769 .520383693	2670	1.17
1.17	357552924	.709401709		-1.10725552 -1.11320755	.521531100	2680	1.18
1.18 1.19	350945229 344497016	.694915254		-1.11912226	.522673031	2690	1.19
		.66666667		-1.12500000	.523809524	2700	1.20
1.20	338203463 332059932	.652892562		-1.13084112	.524940618	2710	1.21
1.21	326061947	.639344262		-1.13664596	.526066351	2720	1.22
1.23	- 320205201	.626016260		-1.14241486	.527186761	2730	1.23
1.24	314485536	.612903226		-1.14814815	.528301887	2740	1.24
1.25	308898945	.600000000		-1.15384615	.529411765	2750	1.25 1.26
1.26	303441560	.587301587		-1.15950920	.530516432	2760 2770	1.27
1.27	298109654	.574803150		-1.16513761	.531615925 .532710280	2780	1.28
1.28 1.29	292899625 287808001	.562500000		-1.17073171 -1.17629179	.533799534	2790	1.29
						3 <sub>E</sub> <sup>2</sup>	
		3-2	302	302	_ 3∩2		p <u>d_d_d</u> c b a
	- 3C2	- 3C2	- 3C2	- 3C2	- 3C2	$b^2 f^{(5)}(\varepsilon)$	c_p_a
	4 4	4 9					

_	4		
$(D^3y)_{y=y} = \frac{1}{1}$	5 3C! v: +	3 <sub>R</sub> i	(i=3,1)
$(D^3y)_{x=x} = \frac{1}{b^3}$	j=0	4	

			$-x_1 = \frac{1}{b^3} \stackrel{\angle}{\underset{j=0}{\angle}} 4$			NAC	مسر 🛕
						3 <sub>4</sub> E <sup>3</sup>	
<u>a_a_a</u> b c d	<sup>3</sup> C <sub>0</sub> <sup>3</sup>	3C3	3C2	<sup>3</sup> C <sup>3</sup> <sub>4</sub>	3C 3	b <sup>2</sup> f <sup>151</sup> (ξ)	
0.10	16.7574361	-21.0000000	8.45454545	-5.85714286	1.64516129	0.1600	0.10
.11	14.9769279	-19.1818182	8,40540541	-5.84360189	1.64308682	.1610	.11
.12	13.4986868	-17.6666667	8.35714286	-5.83018868 -5.81690141	1.64102564 1.63897764	.1630	.13
.13	12.2528046 11.1893520	-16.3846154 -15.2857143	8.30973451	-5.80373832	1.63694268	.1640	.14
.15	10.2717191	-14.3333333	8.21739130	-5.79069767	1.63492063	.1650	.15
.16	9.47245266	-13.5000000	8.17241379	-5.77777778	1.63291139	.1660	.16
.17	8.77056288	-12.7647059	8.12820513	-5.76497696	1.63091483	.1670	.17
.18	8.14972810 7.59706576	-12.1111111 -11.5263158	8.08474576 8.04201681	-5.75229358 -5.73972603	1.62893082 1.62695925	.1680 .1690	.18 .19
.20	7.10227272	-11.0000000	8.00000000	-5.72727273	1.62500000	.1700	.20
.21	6.65701100	-10.5238095	7.95867769	-5.71493213	1.62305296	.1710	.21
.22	6.25446100	-10.0909091	7.91803279	-5.70270270	1.62111801	.1720	. 22
.23	5.88899130	- 9.69565217	7.87804878	-5.69058296	1.61919505	.1730	.23
.24	5.55591114	- 9.33333333	7.83870968	-5.67857143	1.61728395	.1740	.24
.25	5.25128206	- 9.00000000	7.80000000	-5.66666667	1.61538462	.1750	.25
.26	4.97177326	- 8,69230770	7.76190476	-5.65486726	1.61349693	.1760	.26
.27	4.71454897 4.47718000	- 8.40740741 - 8.14285714	7.72440945	-5.64317180 -5.63157895	1.61162080	.1770	.28
.29	4.25757354	- 7.89655172	7.65116279	-5.62008734	1.60790274	.1790	.29
.30	4.05391710	- 7.66666667	7.61538462	-5.60869565	1.60606061	.1800	.30
.31	3.86463322	- 7.45161290	7.58015267	-5.59740260	1.60422961	.1810	.31
. 32	3.68834272	- 7.25000000	7.54545455	-5.58620690	1.60240964	.1820	. 32
.33	3.52383456 3.37004116	- 7.06060606 - 6.88235294	7.51127820	-5.57510729 -5.56410256	1.60060060 1.59880240	.1830	.33
. 35	3.22601784	- 6.71428571	7.4444444	-5.55319149	1.59701492	.1850	. 35
.36	3.09092564	- 6.5555556	7.41176471	-5.54237288	1.59523810	.1860	.36
.37	2.96401712	- 6.40540541	7.37956204	-5.53164557	1.59347181	.1870	.37
.38	2.84462424	- 6.26315789	7.34782609	-5.52100840	1.59171598	.1880	.38
. 39	2.73214812	- 6.12820513	7.31654676	-5.51046025	1.58997050	.1890	.39
.40	2.62605042	- 6.00000000	7.28571429	-5.50000000	1.58823529	.1900	. 40
.41	2.52584592	- 5.87804878	7.25531915	-5.48962655	1.58651026	.1910	. 41
. 42	2.43109618	- 5.76190476	7.22535211	-5.47933884 -5.46913580	1.58479532	.1920	. 42
. 43	2.34140402 2.25640892	- 5.65116279 - 5.54545455	7.16666667	-5.45901640	1.58309038 1.58139535	.1940	. 44
. 45	2.17578286	- 5.4444444	7.13793103	-5.44897959	1.57971014	.1950	. 45
. 46	2.09922675	- 5.34782609	7.10958904	-5.43902439	1.57803468	.1960	.46
. 47	2.02646742	- 5.25531915	7.08163265	-5.42914980	1.57636888	.1970	. 47
.48	1.95725481	- 5.16666667	7.05405405	-5.41935484	1.57471264	.1980 .1990	.48
.49	1.89135967	- 5.08163265	7.02684564	-5.40963855	1.57306590	1	
.50	1.82857143	- 5.00000000	7.00000000	~5.40000000	1.57142857	.2000	.50
.51	1.76869637	- 4.92156863	6.97350993	-5.39043285	1.56980057	.2010	.51
.52	1.71155599	- 4.84615385 - 4.77358491	6.94736842	-5.38095238 -5.37154150	1.56818182	.2020	.52
.53	1.65698554 1.60483278	- 4.77358491 - 4.70370370	6.89610390	-5.36220472	1.56497175	.2040	.54
.55	1.55495679	- 4.63636364	6.87096774	-5.35294118	1.56338028	.2050	.55
.56	1.50722697	- 4.57142857	6.84615385	-5.34375000	1.56179775	.2060	.56
.57	1.46152214	- 4.50877193	6.82165605	-5.33463035	1.56022409	.2070	.57
.58 .59	1.41772968 1.37574486	- 4.44827586 - 4.38983051	6.79746835	-5.32558140 -5.31660232	1.55865922	.2090	.58
.60	1.33547009	- 4.33333333	6.75000000	-5.30769231	1.55555556	.2100	.60
.61	1.29681440	- 4.27868852	6.72670807	-5.29885058	1.55401662	.2110	.61
. 62	1.25969290	- 4.22580645	6.70370370	-5.29007634	1.55248619	.2120	. 62
.63	1.22402621 1.18974014	- 4.17460317 - 4.12500000	6.68098160	-5.28136882 -5.27272727	1.55096419	.2130	.63
						.2150	
•65 66	1.15676518 1.12503621	- 4.07692308 - 4.03030303	6.63636364	-5.26415095 -5.25563910	1.54794521	.2150	.65
.66	1.09449214	- 3.98507463	6.59281437	-5.24719101	1.54495913	.2170	.67
.68	1.06507561	- 3.94117647	6.57142857	-5.23880597	1.54347826	.2180	.68
.69	1.03673272	- 3.89855072	6.55029586	-5.23048327	1.54200542	.2190	.69
	$-\frac{3}{4}C_{4}^{1}$	- <sup>3</sup> C <sub>3</sub> <sup>1</sup>	- 3C 1	- 3C1	- <sup>3</sup> C <sub>0</sub>	3 <sub>4</sub> E¹	p_ <u>d_d</u>
	4 4	4 3	1 4 2	4 1	1 4 0	b <sup>2</sup> f <sup>(5)</sup> (£)	c b

$(D^3y)_{x=x_i} = \frac{1}{b^3} \sum_{j=0}^{4} {}_{4}^{3}C_{j}^{j}$	Уj	+	³Ri	(i=3,i)
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•			1			NA.	CA A
r <u>aaa</u> bcd	3C3	3C3	<sup>3</sup> C <sup>3</sup> <sub>4</sub> C <sub>2</sub>	3C3 4C3	3C3	$\frac{{}_{4}^{3}E^{3}}{b^{2}f^{(5)}(\xi)}$	
0.70 .71 .72 .73 .74	1.00941277 .983068060 .957653630 .933127104 .909448504	- 3.85714286 - 3.81690141 - 3.7777778 - 3.73970603 - 3.70270270	6.46820809	-5.22222222 -5.21402214 -5.20588235 -5.19780220 -5.18978102	1.54054054 1.53908356 1.53763441 1.53619303 1.53475936	0.2200 .2210 .2220 .2230 .2240	0.70 .71 .72 .73
.75 .76 .77 .78	.886580086 .864486188 .843133092 .822488900 .802523410	- 3.66666667 - 3.63157895 - 3.59740260 - 3.56410256 - 3.53164557	6.42857143 6.40909091 6.38983051 6.37078652 6.35195531	-5.18181818 -5.17391304 -5.16606498 -5.15827338 -5.15053763	1.53333333 1.53191489 1.53050398 1.52910053 1.52770449	.2250 .2260 .2270 .2280 .2290	.75 .76 .77 .78
.80 .81 .82 .83	.783208020 .764515610 .746420456 .728898162 .711925536	- 3.5000000 - 3.46913580 - 3.43902439 - 3.40963855 - 3.38095238	6.33333333 6.31491713 6.29670330 6.27868853 6.26086957	-5.14285714 -5.13523132 -5.12765957 -5.12014134 -5.11267606	1.52631579 1.52493438 1.52356021 1.55219321 1.52083333	.2300 .2310 .2320 .2330 .2340	.80 .81 .82 .83 .84
. 85 . 86 . 87 . 88 . 89	.695480574 .679542324 .664090894 .649107326 .634573587	- 3.35294118 - 3.32558140 - 3.29885057 - 3.27272727 - 3.24719101		-5.10526316 -5.09790210 -5.09059234 -5.08333333 -5.07612457	1.51948052 1.51813472 1.51679589 1.51546392 1.51413882	.2350 .2360 .2370 .2380 .2390	.85 .86 .87 .88
.90 .91 .92 .93	.620472490 .606787660 .593503482 .580605063 .568078182	- 3.22222222 - 3.19780220 - 3.17391304 - 3.15053763 - 3.12765957		-5.06896552 -5.06185567 -5.05479452 -5.04778157 -5.04081632	1.51282051 1.51150895 1.51020408 1.50890585 1.50761421	.2400 .2410 .2420 .2430 .2440	.90 .91 .92 .93
.95 .96 .97 .98	.555909274 .544085364 .532594074 .521423552 .510562474	- 3.10526316 - 3.08333333 - 3.06185567 - 3.04081633 - 3.02020202	6.07692308 6.06122449 6.04568528 6.03030303 6.01507538	-5.03389831 -5.02702703 -5.02020202 -5.01342282 -5.00668896	1.50632911 1.50505051 1.50377834 1.50251256 1.50125313	.2450 .2460 .2470 .2480 .2490	.95 .96 .97 .98
1.00 1.01 1.02 1.03 1.04	.500000000 .489725758 .479729814 .470002652 .460535158	- 3.00000000 - 2.98019802 - 2.96078431 - 2.94174757 - 2.92307692	6.00000000 5.98507463 5.97029703 5.95566502 5.94117647	-5.00000000 -4.99335548 -4.98675497 -4.98019802 -4.97368421	1.50000000 1.49875312 1.49751244 1.49627792 1.49504951	.2500 .2510 .2520 .2530 .2540	1.00 1.01 1.02 1.03 1.04
1.05 1.06 1.07 1.08 1.09	.451318590 .442344570 .433605056 .425092336 .416799006	- 2.90476190 - 2.88679245 - 2.86915888 - 2.85185185 - 2.83486239	5.92682927 5.91262136 5.89855072 5.88461538 5.87081340	-4.96721311 -4.96078431 -4.95439739 -4.94805195 -4.94174757	1.49382716 1.49261084 1.49140049 1.49019608 1.48899755	.2550 .2560 .2570 .2580 .2590	1.05 1.06 1.07 1.08 1.09
1.10 1.11 1.12 1.13 1.14	.408717954 .400842352 .393165636 .385681502 .378383885	- 2.81818182 - 2.80180180 - 2.78571429 - 2.76991150 - 2.75438596	5.81690141	-4.93548387 -4.92926045 -4.92307692 -4.91693291 -4.91082803	1.48780488 1.48661801 1.48543689 1.48426150 1.48309179	.2600 .2610 .2620 .2630 .2640	1.10 1.11 1.12 1.13 1.14
1.15 1.16 1.17 1.18 1.19	.371266955 .364325099 .357552924 .350945229 .344497016	- 2.73913043 - 2.72413793 - 2.70940171 - 2.69491525 - 2.68067227	5.79069767 5.77777778 5.76497696 5.75229358 5.73972603	-4.90476190 -4.89873418 -4.89274448 -4.88679245 -4.88087774	1.48192771 1.48076923 1.47961631 1.47846890 1.47732697	.2650 .2660 .2670 .2680 .2690	1.15 1.16 1.17 1.18 1.19
1.20 1.21 1.22 1.23 1.24	.338203463 .332059932 .326061947 .320205201 .314485536	- 2.66666667 - 2.65289256 - 2.63934426 - 2.62601626 - 2.61290323		-4.87500000 -4.86915888 -4.86335404 -4.85758514 -4.85185185	1.47619048 1.47505938 1.47393365 1.47281324 1.47169811	.2700 .2710 .2720 .2730 .2740	1.20 1.21 1.22 1.23 1.24
1.25 1.26 1.27 1.28 1.29	.308898945 .303441560 .298109654 .292899625 .287808001	- 2.6000000 - 2.58730159 - 2.57480315 - 2.56250000 - 2.55038760	5.66666667 5.65486726 5.64317181 5.63157895 5.62008734	-4.84615385 -4.84049080 -4.83486239 -4.82926829 -4.82370821	1.47058824 1.46948357 1.46838408 1.46728972 1.46620047	.2750 .2760 .2770 .2780 .2790	1.25 1.26 1.27 1.28 1.29

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- 3C1

- 3C1

- 3C1

$(D^3y)_{x=x_i} = \frac{1}{b^3}$	$\sum_{j=0}^{4} {}_{4}^{3}C_{j}^{i} y_{j} +$	3R i	(i=4,0)
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		(U-y),	$c=x_1=\frac{1}{b^3}$	4Cj yj + 4K'	(1=4,0)		
			j=0			- N.	ACA,
		•				3 <sub>4</sub> E <sup>4</sup>	
= <u>a</u> - <u>a</u> - <u>a</u> b c d	. <sup>3</sup> C <sub>0</sub> <sup>4</sup>	3C4	3C4 4C2	<sup>3</sup> C <sup>4</sup> <sub>4</sub>	3C4 4 4	b <sup>2</sup> f <sup>(5)</sup> (£)	
0.10	50.2723084	-61.0000000	19.3636364	-11.5714286	2.93548387	1.480	0.10
.11	44.9307836	-55.5454545	19.2162162	-11.5308057	2.92926045	1.483	.11
.12	40.4960605	-51.0000000	19.0714286	-11.4905660	2.92307692	1.486	.12
.13	36.7584139 33.5680561	-47.1538462 -43.8571429	18.9292035 18.7894737	-11.4507042 -11.4112150	2.91693291	1.489	.13
• 14	00.000001	-40.0071429	10.1094101	-11, 4112100	2.91082803	1.492	.14
.15	30.8151572	-41.0000000	18.6521739	-11.3720930	2.90476190	1.495	.15
.16	28.4173578	-38.5000000	18.5172414	-11.3333333	2.89873418	1.498	.16
.17	26.3116886	-36.2941176	18.3846154	-11.2949309	2.89274448	1.501	.17
.18	24.4491843 22.7911973	-34.3333333	18.2542373	-11.2568807	2.88679245	1.504	.18
•19	22.1911913	-32.5789474	18.1260504	-11.2191781	2.88087774	1.507	.19
.20	21.3068182	-31.0000000	18.0000000	-11.1818182	2.87500000	1.510	.20
.21	19.9710330	-29.5714286	17.8760331	-11.1447964	2.86915888	1.513	.21
.22	-18.7633830	-28.2727273	17.7540984	-11.1081081	2.86335404	1.516	.22
.23	17.6669739 16.6677334	-27.0869565 -26.0000000	17.6341463 17.5161290	-11.0717489 -11.0357143	2.85758574	1.519	.23
•••	10.0011001	20.000000	17.0101000	11,000/140	2.00100100	1.022	.24
.25	15.7538462	-25.0000000	17.4000000	-11.0000000	2.84615385	1.525	.25
.26	14.9153198	-24.0769231	17.2857143	-10,9646018	2.84049080	1.528	.26
.27	14.1436469 13.4315400	-23.2222222 -22.4285714	17.1732284	-10.9295154 -10.8947368	2.83486239	1.531	.27
.29	12.7727206	-21.6896552	16.9534884	-10.8602620	2.82370821	1.534	.29
	/					1.00.	•
.30	12.1617513	-21.0000000	16.8461539	-10.8260870	2.81818182	1.540	.30
.32	11.5938997 11.0650282	-20.3548387 -19.7500000	16.7404580	-10.7922078	2.81268882	1.543	.31
.33	10.5715037	-19.1818182	16.6363636 16.5338346	-10.7586207 -10.7253219	2.80722892	1.546	.32
.34	10.1101235	-18.6470588	16.4328358	-10.6923077	2.79640719	1.552	.34
	0.00000000	10.1.000					
.35 .36	9.67805352 9.27277692	-18.1428571 -17.6666667	16.3333333 16.2352941	-10.6595145 -10.6271186	2.79104478	1.555 1.558	•35
.37	8.89205136	-17.2162162	16.1386861	-10.5949367	2.78571429	1.561	.36
.38	8.53387272	-16.7894737	16.0434783	-10.5630252	2.77514793	1.564	.38
. 39	8.19644436	-16.3846154	15.9496403	-10.5313808	2.76991150	1.567	.39
. 40	7.87815126	-16.0000000	15.8571428	-10.5000000	2.76470588	1.570	. 40
.41	7.57753776	-15.6341463	15.7659574	-10.4688797	2.75953079	1.573	.41
. 42	7.29328854	-15.2857143	15.6760563	-10.4380165	2.75438597	1.576	. 42
. 43	7.02421206	-14.9534894	15.5874126	-10.4074074	2.74927114	1.579	. 43
. 44	6.76922676	-14.6363636	15,5000000	-10.3770492	2.74418605	1.582	.44
. 45	6.52734857	-14.3333333	15.4137931	-10.3469388	2.73913043	1.585	. 45
. 46	6.29768026	-14.0434783	15.3287671	-10.3170732	2.73410405	1.588	.46
.47	6.07940225	-13.7659574	15.2448980	-10.2874494	2.72910663	1.591	. 47
.49	5.97176442 5.67407900	-13.5000000 -13.2448980	15.1621622 15.0805369	-10.2580645 -10.2289157	2.72413793	1.594 1.597	.48
		2002110000	20.000000	10.2203107	2.71515771	1.057	. 49
.50	5.48571429	-13.0000000	15.0000000	-10.2000000	2.71428571	1.600	.50
.51 .52	5.30608911 5.13466797	-12.7647058	14.9205298	-10.1713147	2.70940171	1.603	.51
.53	4.97095663	-12.5384615 -12.3207547	14.8421053	-10.1428571 -10.1146245	2.70454545	1.606	.52
.54	4.81449834	-12.1111111	14.6883117	-10.0866142	2.69491525	1.609 1.612	.53 .54
		11 0000000					
.55 .56	4.66487037 4.52168092	-11.9090909 -11.7142857	14.6129032	-10.0588235	2.69014085	1.615	.55
57	4.38456642	-11.7142657	14.5384615	-10.0312500 -10.0038911	2.68539326	1.618 1.621	.56 .57
58	4.25318905	-11.3448276	14.3924051	- 9.97674419	2.67597765	1.624	.58
.59	4.12723457	-11.1694915	14.3207547	- 9.94980695	2.67130919	1.627	.59
.60	4.00641026	-11.0000000	14.2500000	- 9.92307692	2.66666667	1 630	60
.61	3.89044321	-10.8360656	14.1801242	- 9.89655172	2.66204986	1.630 1.633	.60
.62	3.77907869	-10.6774194	14.1111111	- 9.87022901	2.65745856	1.636	.62
63	3.67207864	~10.5238095	14.0429448	- 9.84410646	2.65289256	1.639	. 63
64	3.56922041	-10.3750000	13.9756098	- 9.81818182	2.64835165	1.642	.64
65	3.47029554	-10.2307692	13.9090909	- 9.79245283	2.64383562	1.645	. 65
.66	3.37510863	-10.0909091	13.8433735	- 9.76691729	2.63934426	1.648	.66
67	3.28347642	- 9.95522388	13.7784431	- 9.74157303	2.63487738	1.651	.67
68	3.19522683 3.11019815	- 9.82352941 - 9.69565217	13.7142857	- 9.71641791	2.63043478	1.654	.68
-	0,11010010	7.0000217	13,6508876	- 9.69144981	2.62601626	1.657	.69
	- 3CO	- 3C0	- 3CO	_ 3c0	~ 3C0	3E0	p_d_d_
	404	- , 0		U.			V

 $(0^3y)_{x=x_1} = \frac{1}{b^3} \sum_{j=0}^{4} {}_{4}^{3}C_{j}^{i} y_j + {}_{4}^{3}R^{i}$  (i=4.0)

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-						*3E4	
222	2.4	3-4	3-4	3.04	304		
<u>aaa</u> bcd	3C4	<sup>3</sup> C <sup>4</sup> .	3C2	3C4 4C3	3C 4	b2f(5)	i
		0 583 40058	37 5000353	0 6666667	9 69169169	1.660	0.70
0.70	3.02823832	- 9.57142857	13.5882353	- 9.66666667 - 9.64206642	2.62162162	1.663	.71
.71	2.94920418	- 9.45070423	13.5263158		2.61290323	1.666	.72
.72	2.87296089	- 9.33333333		- 9.61764706	2.60857909	1.669	.73
.73	2.79938131	- 9.21917808	13.4046243	- 9.59340659		1.672	.74
.74	2.72834551	- 9.10810811	13.3448276	- 9.56934307	2.60427808	1.072	• / •
.75	2.65974026	- 9.00000000	13.2657143	- 9.54545455	2.60000000	1.675	.75
.76	2.59345856	- 8.89473684	13.2272727	- 9.52173913	2.59574468	1.678	.76
.77	2.52939928	- 8.79220779	13.1694915	- 9.49819495	2.59151194	1.681	.77
.78	2.46746670	- 8.69230769	13.1123596	- 9.47482014	2.58730159	1.684	.78
.79	2.40757023	- 8.59493671	13.0558659	- 9.45161290	2.58311346	1.687	.79
				0 400577.47	2.57894737	1.690	.80
. 80	2.34962406	- 8.50000000	13.00000000	- 9.42857143		1.693	.81
. 81	2.29354683	- 8.40740741	12.9447514	- 9.40569395	2,57480315	1.696	.82
. 82	2.23926137	- 8.31707317	12.8901099	- 9.38297872	2.57068068		
. 83	2.18669449	- 8.22891566	12,8360656	- 9.36042403	2.56657963	1.699	.83
. 84	2.13577661	- 8.14285714	12.7826087	- 9.33802817	2,56250000	1.702	.84
.85	2.08644172	- 8,05882353	12.7297297	- 9.31578947	2.55844156	1.705	.85
.86	2.03862697	- 7.97674419	12.6774194	- 9.29370629	2.55440415	1.708	.86
.87	1.99227268	- 7.89655172	12.6256685	- 9.27177700	2,55038760	1.711	. 87
.88	1.94732198	- 7.81818182	12.5744681	- 9.25000000	2.54639175	1.714	.88
. 89	1.90372076	- 7.74157303	12.5238095	- 9.22837370	2.54241645	1.717	.89
	3 003 43 7 47	n ccccccen	12.4736842	- 9.20689655	2.53846154	1.720	.90
.90	1.86141747	- 7.66666667	12.4240838	- 9.18556701	2.53452685	1.723	.91
.91	1.82036298	- 7.59340659	12.3750000	- 9.16438356	2.53061225	1.726	.92
. 92	1.78051045	- 7.52173913		- 9.14334471	2.52671756	1.729	.93
. 93	1.74181519	- 7.45161290	12.3264249	- 9.12244898	2.52284265	1.732	.94
.94	1.70423455	- 7.38297872	12.2783505	- 9.12244090	2.022G42GG	1	•••
.95	1.66772782	- 7.31578947	12.2307692	- 9.10169492	2.51898734	1.735	.95
.96	1.63225609	- 7.25000000	12.1836735	- 9.08108108	2.51515152	1.738	.96
.97	1.59778222	- 7.18556701	12.1370558	- 9.06060606	2.51133501	1.741	.97
.98	1.56427066	- 7.12244898	12.0909091	- 9.04026846	2.50753769	1.744	.98
.99	1.53168742	- 7.06060606	12.0452261	- 9.02006689	2.50375940	1.747	.99
1.00	1.50000000	- 7.00000000	12.0000000	- 9.00000000	2.50000000	1.750	1.00
1.01	1.46917727	- 6.94059406	11.9552239	- 8.98006645	2.49625935	1.753	1.01
1.02	1.43918944	- 6.88235294	11.9108911	- 8.96026490	2.49253731	1.756	1.02
1.03	1.41000796	- 6.82524272	11.8669951	- 8.94059406	2.48883375	1.759	1.03
1.04	1.38160547	- 6.76923077	11.8235294	- 8.92105263	2.48514852	1.762	1.04
		6 m3 4005m3	11 7004070	0.00167074	2.48148148	1.765	1.05
1.05	1.35395577	- 6.71428571	11,7804878	- 8.90163934 - 8.88235294	2.47783257	1.768	1.06
1.06	1.32703371	- 6.66037736	11.7378641	- 8.86319218	2.47420147	1.771	1.07
1.07	1.30081517	- 6.60747664	11.6956522	- 8.84415584	2.47058824	1.774	1.08
1.08	1.27527701	- 6.5555556 - 6.50458716	11.6538462	- 8.82524272	2,46699267	1.777	1.09
1.09	1.25039702	- 6.30458710	11.0124402	- 0.02024212	2,10000000	20	
1.10	1.22615386	- 6.45454545	11.5714286	- 8.80645161	2.46341463	1.780	1.10
1.11	1.20252706	- 6,40540541	11.5308057	- 8.78778135	2.45985401	1.783	1.11
1.12	1.17949691	- 6.35714286	11.4905660	- 8.76923077	2.45631068	1.786	1.12
1.13	1.15704451	- 6.30973451	11.4507042	- 8.75079872	2.45278450	1.789	1.13
1.14	1.13515164	- <b>6.</b> 26315789	11.4112150	- 8.73248408	2.44927536	1.792	1.14
. 16	1 11300006	- 6,21739130	11.3720930	- 8.71428571	2.44578313	1.795	1.15
1.15	1,11380086	- 6.17241379	11.3333333	- 8.69620253	2.44230769	1.798	1.16
1.16	1.09297530	- 6.12820513	11.2949309	- B.67823344	2.43884892	1.801	1.17
1.17	1.05283569	- 6.08474576	11.2568807	- 8.66037736	2.43540670	1.804	1.18
L.18 L.19	1.03349105	- 6.04201681	11.2191781	- 8.64263323	2.43198091	1.807	1.19
				B 6050000	2.42857143	1 910	1.20
1.20	1.01461039	- 6.00000000 - 5.05967769	11.1818182 11.1447964	- 8.62500000 - 8.60747664	2.42517815	1.810	1.21
1.21	.996179794	- 5.95867769 - 5.91803279	11.1081081	- 8.59006211	2.42180095	1.816	1.22
L.22	.978185841	- 5.87804878	11.0717489	- 8.57275542	2.41843972	1.819	1.23
1.23	.960615603 .943456607	- 5.83870968	11.0357143	- 8.5555556	2.41509434	1.822	1.24
					0 4337764773		7 25
1.25	.926696834	- 5.80000000	11.0000000	- 8.53846154	2.41176471	1.825	1.25
1.26	.901324679	- 5.76190476	10.9646018	- 8.52147239	2.40845070	1.831	1.27
1.27	.894328962	- 5.72440945	10.9295154	- 8.50458716	2.40515222	1.834	1.28
1.28	.878698876 .863424004	- 5.68750000 - 5.65116279	10.8947368 10.8602620	- 8.48780488 - 8.47112462	2.40186916 2.39860140	1.837	1.29
1.29	\$0024240U\$	- 0.00110219	20,0002020	0.1,110,100		3E0	
l	3C0	300	- 3CO	- 3C0	- 3CO	4 <sup>E</sup>	p_d_d_d c_b_a
	4 4	- 3C <sub>3</sub>	- <sup>3</sup> C <sub>2</sub>	4	- <sup>3</sup> C 0	b <sup>2</sup> f <sup>(5)</sup> (ξ)	cba
1			1			1- ' ''	

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$r = \frac{a}{b} \cdot \frac{a}{c} \cdot \frac{a}{d}$	4℃ i	4c i	4Ci	4Ci 4C3
0.10 .11 .12 .13	33.5148722 29.9538558 26.9973736 24.5056092 22.3787040	-40,0000000 -36,3636364 -33,333333 -30,7692308 -28,5714286	10.9090909 10.8108108 10.7142857 10.6194690 10.5263158	-5.71428571 -5.68720379 -5.66037736 -5.63380282 -5.60747664
.15 .16 .17 .18	20.5434382 18.9449052 17.5411258 16.2994562 15.1941315	-26.6666667 -25.0000000 -23.5294118 -22.222222 -21.0526316	10.4347826 10.3448276 10.2564103 10.1694915 10.0840336	-5.58139535 -5.5555556 -5.52995392 -5.50458716 -5.47945205
.20 .21 .22 .23	14.2045454 13.3140220 12.5089220 11.7779826 11.1118223	-20.0000000 -19.0476190 -18.1818182 -17.3913043 -16.6666667	10.000000 9.9173537 9.83606557 9.75609756 9.67741935	-5.45454545 -5.42986425 -5.40540541 -5.38116592 -5.35714286
.25 .26 .27 .28 .29	10.5025641 9.94354652 9.42909794 8.95436000 8.51514708	-16.0000000 -15.3846154 -14.8148148 -14.2857143 -13.7931034	9.6000000 9.52380952 9.44881890 9.3750000 9.30232558	-5.33333333 -5.30973451 -5.28634361 -5.26315789 -5.24017467
.30 .31 .32 .33	8.10783420 7.72926644 7.37668544 7.04766912 6.74008232	-13.3333333 -12.9032258 -12.5000000 -12.1212121 -11.7647059	9.23076923 9.16030534 9.09090909 9.02255639 8.95522388	-5.21739130 -5.19480519 -5.17241379 -5.15021459 -5.12820513
.35 .36 .37 .38 .39	6.45203568 6.18185128 5.92803424 5.68924848 5.46429624	-11.4285714 -11.1111111 -10.8108108 -10.5263158 -10.2564103	8.8888889 8.82352941 8.75912409 8.69565217 8.63309353	-5.10638298 -5.08474576 -5.06329114 -5.04201681 -5.02092050
.40 .41 .42 .43	5.25210084 5.05169184 4.86219236 4.68280804 4.51281784	-10.0000000 - 9.75609756 - 9.52380952 - 9.30232558 - 9.09090909	8.57142857 8.51063830 8.45070423 8.39160839 8.33333333	-5.00000000 -4.97925311 -4.95867769 -4.93827160 -4.91803279
. 45 . 46 . 47 . 48 . 49	4.35156571 4.19845351 4.05293484 3.91450962 3.78271933	- 8.8888889 - 8.69565217 - 8.51063830 - 8.33333333 - 8.16326531	8.27586207 8.21917808 8.16326531 8.10810811 8.05369128	-4.89795918 -4.87804878 -4.85829960 -4.83870968 -4.81927711
.50 .51 .52 .53	3.65714286 3.53739274 3.42311198 3.31397108 3.20966556	- 8.00000000 - 7.84313725 - 7.69230769 - 7.54716981 - 7.40740741	8.00000000 7.94701987 7.89473684 7.84313725 7.79220779	-4.8000000 -4.78087649 -4.76190476 -4.74308300 -4.72440945
.55 .56 .57 .58	3.10991358 3.01445394 2.92304428 2.83545937 2.75148971	- 7.27272727 - 7.14285714 - 7.01754386 - 6.89655172 - 6.77966102	7.74193548 7.69230769 7.64331210 7.59493671 7.54716981	-4.70588235 -4.68750000 -4.66926070 -4.65116279 -4.63320463
.60 .61 .62 .63	2.67094017 2.59362881 2.51938579 2.44805242 2.37948028	- 6.66666667 - 6.55737705 - 6.45161290 - 6.34920635 - 6.25000000	7.5000000 7.45341615 7.40740741 7.36196319 7.31707317	-4.61538462 -4.59770115 -4.58015267 -4.56273764 -4.54545455
.65 .66 .67 .68	2.31353036 2.25007242 2.18898428 2.13015122 2.07346544	- 6.15384615 - 6.06060606 - 5.97014925 - 5.88235294 - 5.79710145	7.27272727 7.22891566 7.18562874 7.14285714 7.10059172	-4.52830189 -4.51127820 -4.49438202 -4.47761194 -4.46096654
	‡ċ[	4C1	4C1 4 C2	‡c!

29(a)

$(D^4y)_{x=x_i} = \frac{i}{b^4}$	$\sum_{i=0}^{4} {}_{4}^{4}C_{j}^{i} y_{i} + {}_{4}^{4}R^{i}$	(i = 0, 1, 2, 3, 4)
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		- J=0				
					NA	CA
4C i	4E <sup>0</sup> bf <sup>(5)</sup> (ε)	4E <sup>1</sup> bf <sup>(5)</sup> (ξ)	bf <sup>(5)</sup> (£)	4E <sup>3</sup> bf <sup>(5)</sup> (ξ)	4E <sup>4</sup> bf (5)(ξ)	
1.29032258 1.28617363 1.28205128 1.27795527 1.27388535	-1.280 -1.288 -1.296 -1.304 -1.312	-1.180 -1.178 -1.176 -1.174 -1.172	-0.1800 1780 1760 1740 1720	0.820 .822 .824 .826 .828	1.820 1.822 1.824 1.826 1.828	0.10 .11 .12 .13 .14
1.26984127 1.26582278 1.26182965 1.25786164 1.25391850	-1.320 -1.328 -1.336 -1.344 -1.352	-1.170 -1.168 -1.166 -1.164 -1.162	1700 1680 1660 1640 1620	.830 .832 .834 .836	1.830 1.832 1.834 1.836 1.838	.15 .16 .17 .18
1.25000000 1.24610592 1.24223602 1.23839009 1.23456790	-1.360 -1.368 -1.376 -1.384 -1.392	-1.160 -1.158 -1.156 -1.154 -1.152	1600 1580 1560 1540 1520	.840 .842 .844 .846 .848	1.840 1.842 1.844 1.846 1.848	.20 .21 .22 .23 .24
1.23076923 1.22699387 1.22324159 1.21951220 1.21580547	-1.400 -1.408 -1.416 -1.424 -1.432	-1.150 -1.148 -1.146 -1.144 -1.142	1500 1480 1460 1440 1420	.850 .852 .854 .856 .858	1.850 1.852 1.854 1.856 1.858	.25 .26 .27 .28 .29
1.21212121 1.20845921 1.20481928 1.20120120 1.19760479	-1.440 -1.448 -1.456 -1.464 -1.472	-1.140 -1.138 -1.136 -1.134 -1.132	1400 1380 1360 1340 1320	.860 .862 .864 .866	1.860 1.862 1.864 1.866 1.868	.30 .31 .32 .33
1.19402985 1.19047619 1.18694362 1.18343195 1.17994100	-1.480 -1.488 -1.496 -1.504 -1.512	-1.130 -1.128 -1.126 -1.124 -1.122	1300 1280 1260 1240 1220	.870 .872 .874 .876 .878	1.870 1.872 1.874 1.876 1.878	.35 .36 .37 .38 .39
1.17647059 1.17302053 1.16959064 1.16618076 1.16279070	-1.520 -1.528 -1.536 -1.544 -1.552	-1.120 -1.118 -1.116 -1.114 -1.112	1200 1180 1160 1140 1120	.880 .882 .884 .886	1.880 1.882 1.884 1.886 1.888	.40 .41 .42 .43 .44
1.15942029 1.15606936 1.15273775 1.14942529 1.14613181	-1.560 -1.568 -1.576 -1.584 -1.592	-1.110 -1.108 -1.106 -1.104 -1.102	1100 1080 1060 1040 1020	.890 .892 .894 .896 .898	1.890 1.892 1.894 1.896 1.898	. 45 . 46 . 47 . 48 . 49
1.14285714 1.13960114 1.13636364 1.13314448 1.12994350	-1.600 -1.608 -1.616 -1.624 -1.632	-1.100 -1.098 -1.096 -1.094 -1.092	1000 0980 0960 0940 0920	.900 .902 .904 .906 .908	1.900 1.902 1.904 1.906 1.908	.50 .51 .52 .53
1.12676056 1.12359551 1.12044818 1.11731844 1.11420613	-1.640 -1.648 -1.656 -1.664 -1.672	-1.090 -1.088 -1.086 -1.084 -1.082	0900 0880 0860 0840 0820	.910 .912 .914 .916 .918	1.910 1.912 1.914 1.916 1.918	.55 .56 .57 .58
1.1111111 1.10803324 1.10497238 1.10192837 1.09890110	-1.680 -1.688 -1.696 -1.704 -1.712	-1.080 -1.078 -1.076 -1.074 -1.072	0800 0780 0760 0740 0720	.920 .922 .924 .926 .928	1.920 1.922 1.924 1.926 1.928	.60 .61 .62 .63
1.09589041 1.09289617 1.08991826 1.08695652 1.08401084	-1.720 -1.728 -1.736 -1.744 -1.752	-1.070 -1.068 -1.066 -1.064 -1.062	0700 0680 0660 0640 0620	.930 .932 .934 .936 .938	1.930 1.932 1.934 1.936 1.938	.65 .66 .67 .08 .69
4C i	-4E4	-4E <sup>3</sup>	$-\frac{{}^{4}E^{2}}{{}^{6}f^{(5)}(E)}$	- 4E hf (5) (5)	$-\frac{{}^{4}E^{0}}{{}^{6}}$	p=c=b=a

$(D^4y)_{x=x_1} = \frac{1}{b^4}$	$\sum_{j=0}^{4} {}^{4}C_{j}^{i} y_{i} + {}^{4}R^{i}$	(i=0,1,2,3,4)
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				~ NACA
$r = \frac{a}{b} = \frac{a}{c} = \frac{a}{d}$	4ci	4ci	4C1	4Ci
0.70	2.01882554	- 5.71428571	7.058 <b>82353</b> 7.01754386 6.97674419 6.93641618 6.89655172	-4.4444444
.71	1.96613612	- 5.63380282		-4.42804428
.72	1.91530726	- 5.5555556		-4.41176471
.73	1.86625421	- 5.47945205		-4.39560440
.74	1.81889701	- 5.40540541		-4.37956204
.75 .76 .77 .78	1.77316017 1.72897238 1.68626618 1.64497780 1.60504682	- 5.33333333 - 5.26315789 - 5.19480519 - 5.12820513 - 5.06329114	6.85714286 6.81818182 6.77966102 6.74157303 6.70391061	-4.36363636 -4.34782609 -4.33212996 -4.31654676 -4.30107527
.80 .81 .82 .83	1.56641604 1.52903122 1.49284091 1.45779632 1.42385107	- 5.00000000 - 4.93827160 - 4.87804878 - 4.81927711 - 4.76190476	6.6666667 6.62983425 6.59340659 6.55737705 6.52173913	-4.28571429 -4.27046263 -4.25531915 -4.24028269 -4.22535211
. 85	1.39096115	- 4.70588235	6.48648649	-4.21052632
. 86	1.35908465	- 4.65116279	6.45161290	-4.19580420
. 87	1.32818179	- 4.59770115	6.41711230	-4.18118467
. 88	1.29821465	- 4.54545455	6.38297872	-4.16666667
. 89	1.26914717	- 4.49438202	6.34920635	-4.15224913
.90 .91 .92 .93	1.24094498 1.21357532 1.18700696 1.16121012 1.13615636	- 4.4444444 - 4.39560440 - 4.34782609 - 4.30107527 - 4.25531915	6.31578947 6.28272251 6.25000000 6.21761658 6.18556701	-4.13793103 -4.12371134 -4.10958904 -4.09556314 -4.08163265
.95 .96 .97 .98	1.11181855 1.08817073 1.06518815 1.04284710 1.02112495	- 4.21052632 - 4.16666667 - 4.12371134 - 4.08163265 - 4.04040404	6.15384615 6.12244898 6.09137056 6.06060606 6.03015075	-4.06779661 -4.05405405 -4.04040404 -4.02684564 -4.01337792
1.00	1.00000000	- 4.0000000	6.00000000	-4.00000000
1.01	.979451516	- 3.96039604	5.97014925	-3.98671096
1.02	.959459628	- 3.92156863	5.94059406	-3.97350993
1.03	.940005304	- 3.88349515	5.91133005	-3.96039604
1.04	.921070316	- 3.84615385	5.88235294	-3.94736842
1.05	.902637180	- 3.80952381	5.85365854	-3.93442623
1.06	.884689140	- 3.77358491	5.82524272	-3.92156863
1.07	.867210112	- 3.73831776	5.79710145	-3.90879479
1.08	.850184672	- 3.70370370	5.76923077	-3.89610390
1.09	.833598012	- 3.66972477	5.74162679	-3.88349515
1.10	.817435908	- 3.63636364	5.71428571	-3.87096774
1.11	.801684704	- 3.60360360	5.68720739	-3.85852090
1.12	.786331272	- 3.57142857	5.66037736	-3.84615385
1.13	.771363004	- 3.53982301	5.63380282	-3.83386581
1.14	.756767769	- 3.50877193	5.60747664	-3.82165605
1.15	.742533910	- 3.47826087	5.58139535	-3.80952381
1.16	.728650199	- 3.44827586	5.5555556	-3.79746835
1.17	.715105847	- 3.41880342	5.52995392	-3.78548896
1.18	.701890458	- 3.38983051	5.50458716	-3.77358491
1.19	.688994031	- 3.36134454	5.47945206	-3.76175549
1.20	.676406926	- 3.33333333	5.45454545	-3.75000000
1.21	.664119863	- 3.30598512	5.42986425	-3.73831776
1.22	.652123894	- 3.27868852	5.40540541	-3.72670807
1.23	.640410402	- 3.25203252	5.38116592	-3.71517028
1.24	.628971071	- 3.22580645	5.35714286	-3.70370370
1.25	.617797889	- 3.20000000	5.3333333	-3.69230769
1.26	.606883120	- 3.17460317	5.30973451	-3.68098160
1.27	.596219308	- 3.14960630	5.28634361	-3.66972477
1.28	.585799251	- 3.12500000	5.26315789	-3.65853659
1.29	.575616002	- 3.10077519	5.24017467	-3.64741641
	4ci	4C i	4Ci	4Ci

$(D^4y)_{x=x_1=\frac{1}{b^4}}$	$\sum_{j=0}^{4} {}^{4}C_{j}^{j} y_{i} + {}^{4}R^{i}$	(i 0,1,2,3,4)
U	j=0	NACA

					200	
40 i	bf <sup>(5)</sup> (£)	4Ε <sup>1</sup> bf <sup>(5)</sup> (ε)	4E <sup>2</sup> bf <sup>(5)</sup> (ξ)	4E <sup>3</sup> bf <sup>(5)</sup> (ε)	4E <sup>4</sup> bf <sup>(5)</sup> (ξ)	
1.08108108	-1.760	-1.060	-0.0600	0.940	1.940	0.70
1.07816712	-1.768	-1.058	0580	.942	1.942	.71
1.07526882	-1.776	-1.056	0560	.944	1.944	.72
1.07238606	-1.784	-1.054	0540	.946	1.946	.73
1.06951872	-1.792	-1.052	0520	.948	1.948	.74
1.06666667	-1.800	-1.050	0500	.950	1.950	.75
1.06382979	-1.808	-1.048	0480	.952	1.952	.76
1.06100796	-1.816	-1.046	0460	.954	1.954	.77
1.05820106	-1.824	-1.044	0440	.956	1.956	.78
1.05540897	-1.832	-1.042	0420	.958	1.958	.79
1.05263158 1.04986877 1.04712042 1.04438642 1.04166667	-1.840 -1.848 -1.856 -1.864 -1.872	-1.040 -1.038 -1.036 -1.034 -1.032	0400 0380 0360 0340 0320	.960 .962 .964 .966 .968	1.960 1.962 1.964 1.966 1.968	.80 .81 .82 .83
1.03896104	-1.880	-1.030	0330	.970	1.970	. 85
1.03626943	-1.888	-1.028	0280	.972	1.972	. 86
1.03359173	-1.896	-1.026	0260	.974	1.974	. 87
1.03092784	-1.904	-1.024	0240	.976	1.976	. 88
1.02827763	-1.912	-1.022	0220	.978	1.978	. 89
1.02564103 1.02301790 1.02040816 1.01781170 1.01522843	-1.920 -1.928 -1.936 -1.944 -1.952	-1.020 -1.018 -1.016 -1.014 -1.012	0200 0180 0160 0140	.980 .982 .984 .986 .988	1.980 1.982 1.984 1.986 1.988	.90 .91 .92 .93
1.02165823	-1.960	-1.010	0100	.990	1.990	.95
1.01010101	-1.968	-1.008	0080	.992	1.992	.96
1.00755668	-1.976	-1.006	0060	.994	1.994	.97
1.00502513	-1.984	-1.004	0040	.996	1.996	.98
1.00250627	-1.992	-1.002	0020	.998	1.998	.99
1.0000000 .997506234 .995024876 .992555831 .990099010	-2.000 -2.008 -2.016 -2.024 -2.032	-1.000 998 996 994 992	.0020 .0040 .0060 .0080	1.000 1.002 1.004 1.006 1.008	2.000 2.002 2.004 2.006 2.008	1.00 1.01 1.02 1.03 1.04
.987654321	-2.040	990	.0100	1.010	2.010	1.05
.985221675	-2.048	988	.0120	1.012	2.012	1.06
.982800983	-2.056	986	.0140	1.014	2.014	1.07
.980392157	-2.064	984	.0160	1.016	2.016	1.08
.977995110	-2.072	982	.0180	1.018	.2.018	1.09
.975609756	-2.080	980	.0200	1.020	2.020	1.10
.973236010	-2.088	978	.0220	1.022	2.022	1.11
.970873786	-2.096	976	.0240	1.024	2.024	1.12
.968523002	-2.104	974	.0260	1.026	2.026	1.13
.966183575	-2.112	972	.0280	1.028	2.028	1.14
.963855422	-2.120	970	.0300	1.030	2.030	1.15
.961538462	-2.128	968	.0320	1.032	2.032	1.16
.959232614	-2.136	966	.0340	1.034	2.034	1.17
.956937799	-2.144	964	.0360	1.036	2.036	1.18
.954653938	-2.152	962	.0380	1.038	2.038	1.19
.952380952	-2.160	960	.0400	1.040	2.040	1.20
.950118765	-2.168	958	.0420	1.042	2.042	1.21
.947867299	-2.176	956	.0440	1.044	2.044	1.22
.945626478	-2.184	954	.0460	1.046	2.046	1.23
.943396226	-2.192	952	.0480	1.048	2.048	1.24
.941176471	-2.200	950	.0500	1.050	2.050	1.25
.938967136	-2.208	948	.0520	1.052	2.052	1.26
.936768150	-2.216	946	.0540	1.054	2.054	1.27
.934579439	-2.224	944	.0560	1.056	2.056	1.28
.932400932	-2.232	942	.0580	1.058	2.058	1.29
4ci	$-\frac{{}_{4}^{4}E^{4}}{bf^{(5)}(\xi)}$	$-\frac{{}^{4}E^{3}}{bf^{(5)}(\xi)}$	$-\frac{{}^{4}_{4}E^{2}}{bf^{(5)}(\xi)}$	- 4E <sup>1</sup> bf (ξ)	- 4E <sup>0</sup> bf <sup>(5)</sup> (ε)	p= d d d c = b = a

<sup>a</sup>The next order remainder term is  $-0.1667 \text{ b}^2 \left[f^{(6)}(x)\right]_{x=x_2}$ 

29(d)

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